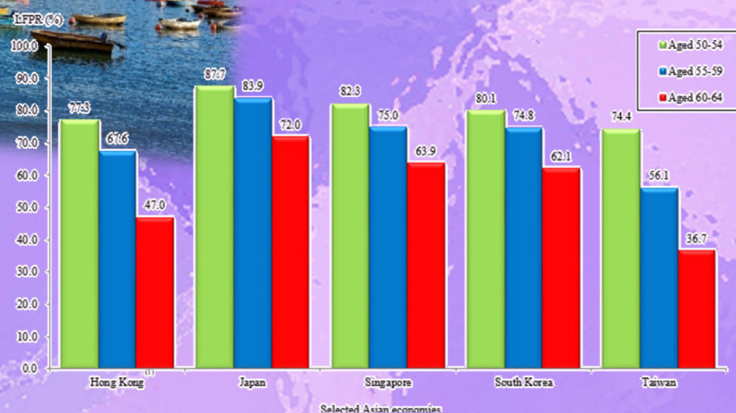


Living with Statistics

2021



Census and Statistics Department
Hong Kong Special Administrative Region



Living with Statistics

2021 Edition

Enquiries about this teaching kit can be directed to :

General Statistics Section (1)

Census and Statistics Department

Address : 21/F, Wanchai Tower, 12 Harbour Road, Wan Chai, Hong Kong.

Tel. : (852) 2582 5054 Fax : (852) 2119 0161

E-mail : train@censtatd.gov.hk

Website of the Census and Statistics Department

www.censtatd.gov.hk

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Introduction

As part of the programme for promoting statistical literacy, the Census and Statistics Department (C&SD) releases annually the teaching kit entitled “*Living with Statistics*”. The teaching kit aims mainly at providing secondary school teachers and students with a convenient means of accessing reference materials on commonly used statistical methods and official statistics in Hong Kong. It also touches upon statistical methods as well as possible pitfalls that should be avoided in applying statistics.

With a better understanding of official statistics and proper statistical methods, students will be able to enhance their awareness and appreciation of statistical information in interpreting the social and economic situations of our society in an objective and effective manner.

The following symbols are used throughout the teaching kit :

Provisional figures

@ Figures are subject to revision later on

Part I

Official statistics

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1 Population size and growth



Introduction

Population estimates are widely used by the Government for planning and policy formulation. The private sector and the academia also use population estimates for business or research purposes.

Births, deaths and net movements⁽¹⁾ are the three factors that affect population growth. This chapter describes how the size of a population and its change can be measured. Various statistical indicators of their trends are also introduced. Finally, a few general characteristics of population growth are outlined in relation to these determining factors.

Concepts of compiling population estimates

Basically, there are two enumeration concepts to count the population of a country / territory, namely the “de jure” concept and the “de facto” concept.

Under the “de jure” concept, all persons who usually live in a country / territory at a particular reference time-point (usually taken as the middle of a year) will be counted as the population of the country / territory.

Under the “de facto” concept, the population includes all persons who are in the country / territory at the reference time-point. This method is equivalent to taking a “snapshot” of the population at a reference time-point.

In practice, the two concepts can be used in conjunction.

Previous method of compiling population estimates in Hong Kong

The “extended de facto” method was used for compiling the series of population estimates for Hong Kong up to 1995. Under the “extended de facto” approach, the Hong Kong population covers all persons who are physically in Hong Kong at the reference time-point, including Hong Kong Permanent Residents and Hong Kong Non-permanent Residents as well as visitors. “Extended” relates to the fact that for a Hong Kong Permanent Resident, he / she will still be counted as part of the

Note :

- (1) In the case of Hong Kong, movements of people from Hong Kong to overseas countries, the mainland of China (the Mainland) or Macao for living, studying or working, and vice versa, are all regarded as movements.

1 Population size and growth

Hong Kong population if, at the reference time-point, he / she is not in Hong Kong but is temporarily in the mainland of China (the Mainland) or Macao.

The application of the “extended” compilation method in the past was intended to avoid fluctuations in the population estimates around major public holidays when there were enormous temporary movements of people between Hong Kong and the Mainland / Macao.

Current method of compiling population estimates in Hong Kong

As from August 2000, the “resident population” method has been adopted in compiling the population estimates in Hong Kong in view of the changing residency and mobility patterns of Hong Kong people. Population figures have been compiled with the new method to 1996 retrospectively.

“Resident population” is a relatively clear-cut concept according to international statistical standards. However, the practical definitions adopted vary from place to place, as the residency and mobility patterns unique to each place need to be given adequate consideration. International statistical organisations have particularly pointed out that, owing to business and social developments, the mobility of residents of certain countries / territories is rather high. In handling the population statistics of these countries / territories, the authorities concerned should consider the situation in depth. In the case of Hong Kong, studies have shown that the “resident population” of Hong Kong (which is referred to as the “Hong Kong Resident Population”) should be defined to include “Usual Residents” and “Mobile Residents”.

“Usual Residents” include two categories of people : (1) Hong Kong Permanent Residents who have stayed in Hong Kong for at least three months during the six months before the reference time-point, or for at least three months during the six months after the reference time-point, regardless of whether they are in Hong Kong or not at the reference time-point; and (2) Hong Kong Non-permanent Residents who are in Hong Kong at the reference time-point.

Hong Kong Non-permanent Residents (such as foreign domestic helpers and persons of Chinese or foreign nationalities entering Hong Kong for work or study) are grouped under “Usual Residents”. This is because for the duration that they hold the status of “Non-permanent Resident”, they can be expected to be usually staying in Hong Kong.

For those Hong Kong Permanent Residents who are not “Usual Residents”, they are classified as “Mobile Residents” if they have stayed in Hong Kong for at least one month but less than three months during the six months before the reference time-point, or for at least one month but less than three months during the six months after the reference time-point, regardless of whether they are in Hong Kong or not at the reference time-point.

1 Population size and growth

The amount of time of stay in Hong Kong of “Mobile Residents” (such as persons who usually work or study outside Hong Kong but occasionally return to Hong Kong) is less than that of “Usual Residents”. Nevertheless, the “Mobile Residents” have a close link with Hong Kong and most probably they have a regular residence in Hong Kong and utilise much of Hong Kong’s facilities and services. In this regard, they should be considered as part of the Hong Kong population.

Under the “resident population” approach, visitors are not included in the Hong Kong population.

For details of the compilation methodology of population estimates, please see the feature article “[Compiling Population Estimates of Hong Kong](#)” published in the February 2002 issue of *Hong Kong Monthly Digest of Statistics* released by the Census and Statistics Department (C&SD).

Population data system

To furnish data users with the latest information on the position of the Hong Kong population, it is the standing practice of C&SD to update and release the population estimates every half-year. The updated estimates relate to the mid-year and year-end positions.

In Hong Kong, the compilation of population estimates is supported by a comprehensive population data system. The main component of the system is the population censuses and by-censuses which provide benchmarking population data, as well as the prime sources of data for small geographical areas and population sub-groups. Apart from population censuses and by-censuses, the population data system also covers sample surveys as well as statistical data compiled based on administrative systems such as birth, death and passenger movement records. Taking all information together, they provide a population statistical database for compiling various types of population figures.

Population censuses and by-censuses taken in Hong Kong

It is an established practice in Hong Kong to conduct a population census every ten years and a population by-census in the middle of the intercensal period. Population censuses were conducted in 1961, 1971, 1981, 1991, 2001, 2011 and 2021 and population by-censuses in 1966, 1976, 1986, 1996, 2006 and 2016.

The aim of conducting population censuses / by-censuses is to obtain up-to-date benchmark information on the socio-economic characteristics of the population and its geographical distribution. They provide benchmark data for studying the direction and trend of population changes. The data are key inputs for compiling projections concerning population, household, labour force and employment.

1 Population size and growth

Population censuses / by-censuses differ from other general sample surveys of households in their sizable scale, which enable them to provide statistics of high precision, even for population sub-groups and small geographical areas. Such information is vital to the Government for planning and policy formulation and important to the private sector for business and research purposes.

For both the 1961 and 1971 Population Censuses, all persons in the population were counted and enquired of their socio-economic characteristics. In the 1981, 1991, 2001, 2011 and 2021 Population Censuses, there was a complete headcount of all persons by age and sex while the detailed characteristics of households and persons were collected from a large sample. Through the use of appropriate computation methods, statistics on the size and characteristics of the population can be compiled by combining the data from the simple enumeration and the detailed enquiry.

A by-census differs from a census in not having a complete headcount of the population but simply focusing enquiry on the detailed characteristics of a large sample of the population. The size and characteristics of the entire population are inferred from the sample results in accordance with appropriate statistical theory.

The 2021 Population Census

In the 2021 Population Census (21C), about nine-tenths of the households in Hong Kong were subject to simple enumeration to provide basic demographic information using a “Short Form” questionnaire, and the remaining one-tenth of the households were subject to more detailed enquiry on a broad range of demographic and socio-economic characteristics using a “Long Form” questionnaire.

The 21C covers the Hong Kong Resident Population under the “resident population” approach. The “resident population” approach has been adopted to compile the population estimates of Hong Kong since August 2000, so as to take into account the changing residency and mobility patterns of the Hong Kong population (see also the previous section on the “resident population” method).

1 Population size and growth

A multi-modal data collection approach was adopted in the 21C. Under this approach, data were collected through different means including online questionnaires, telephone interviews and postal returns with pre-paid envelopes (for “Short Form” only). Census officers from C&SD then conducted face-to-face interviews with households that had not submitted their questionnaires and used mobile tablets to record information of the households at the later stage of the data collection period.



Computer-assisted Telephone Interviewing



A poster on how to verify the identity of census officers of the 2021 Population Census

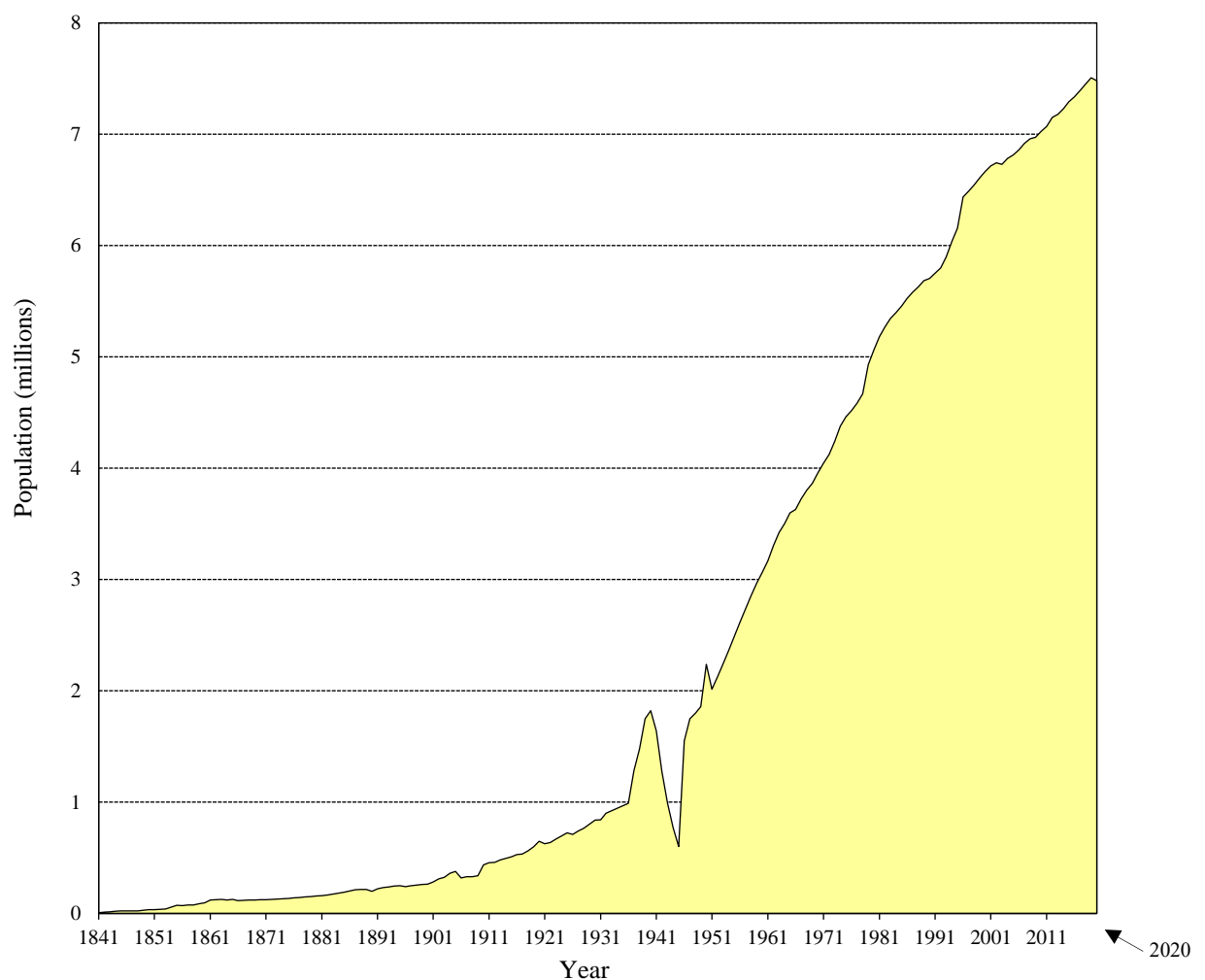
1 Population size and growth

Population size

In mid-2020, the population of Hong Kong was 7.48 million. In 1841, the population was only 7 500. During the past century or so, the population experienced a substantial increase.

Amidst the continuously increasing trend (in sharp contrast to the trend occurred during the Second World War), the rate of change in the population was not always the same.

Chart 1.1 Mid-year population of Hong Kong, 1841 – 2020



1 Population size and growth

Growth rate of the population

To measure the speed of population change, the growth rate can be calculated by dividing the increase in population during a period by the population size at the beginning of that period.

Thus, given that the population decreased from 7 507 400 at mid-2019 to 7 481 800 at mid-2020, the population grew at a rate of

$$\frac{7\,481\,800 - 7\,507\,400}{7\,507\,400} \times 100\% = \underline{\underline{-0.3\%^}}$$

during the period from mid-2019 to mid-2020.

If the population increased in the period, the growth rate would have been a positive number.

Compound average growth rate of the population

For a span of time over a number of years, it is a common practice to measure the average annual growth rate on a compound basis.

The population was 7 481 800 at mid-2020 and 7 291 300 at mid-2015 (i.e. five years ago). If the unknown compound average growth rate is $r\%$ per annum during the 5-year period from mid-2015 to mid-2020, then

$$\left[\begin{array}{c} \text{Population} \\ \text{at mid-2020} \end{array} \right] = \left[\begin{array}{c} \text{Population} \\ \text{at mid-2015} \end{array} \right] \times \left(1 + \frac{r}{100} \right)^5$$

$$\text{or} \quad 7\,481\,800 = 7\,291\,300 \times \left(1 + \frac{r}{100} \right)^5$$

$$\text{Hence} \quad r = \left(\sqrt[5]{\frac{7\,481\,800}{7\,291\,300}} - 1 \right) \times 100 = \underline{\underline{0.5\%^}}$$

That is, the compound average growth rate of the population was 0.5% per annum during the 5-year period from mid-2015 to mid-2020.

1 Population size and growth

Three factors affecting population growth

There are three factors affecting the population growth, namely births, deaths and net movements.

At different times, some factors may have greater effects than the others. To study their contributions to population growth, it is useful to express the change in population size in terms of its components :

$$P_1 - P_0 = (B - D) + (E - L)$$

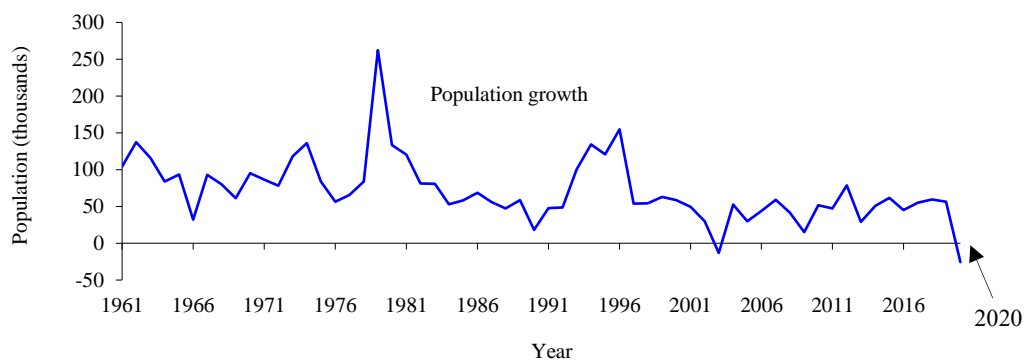
where P_1	=	population at end of the period
P_0	=	population at beginning of the period
B	=	live births during the period
D	=	deaths during the period
$(B - D)$	=	natural change during the period
E	=	number of entrants during the period
L	=	number of leavers during the period
$(E - L)$	=	net movement during the period

1 Population size and growth

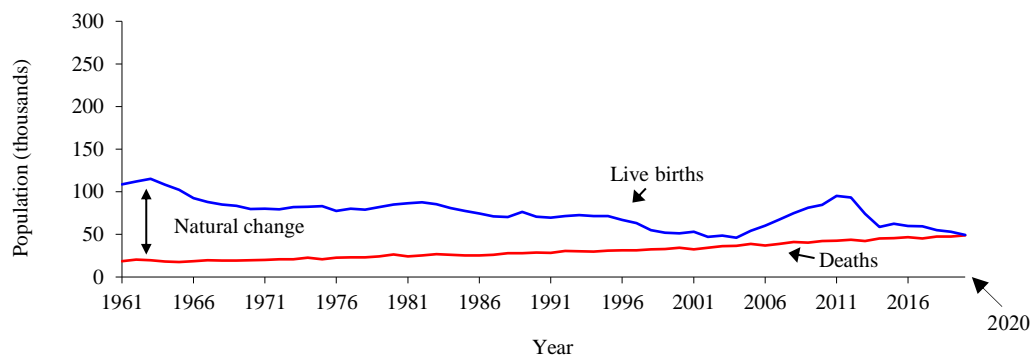
Chart 1.2 Annual change in population of Hong Kong, mid-1961 to mid-2020⁽²⁾

(a) Annual change in population size

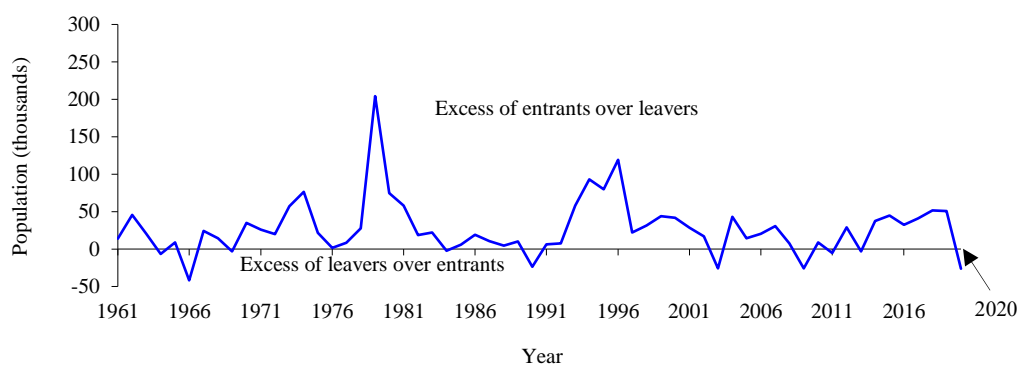
[= (b) Natural change + (c) Net movement]



(b) Natural change



(c) Net movement



Note :

- (2) Population figures from 1996 onwards are compiled based on the “resident population” method and are broadly comparable with figures for 1995 and before. Notwithstanding this, the population figure for 1996 compiled based on the old method (i.e. 6 311 000) has been used in calculating the population growth and net movement from 1995 to 1996.

1 Population size and growth

Stock-flow relationship

To understand the equation shown in the above section, take the size of population at a point of time as a pool of water (i.e. the population “stock”), its level being raised by adding water from the tap (i.e. inflows of births and entrants) and lowered by draining water away through the plughole (i.e. outflows of deaths and leavers). Thus, the population size measures the stock at a particular point of time, whereas changes in all the components, or “flows”, contribute to changes in the stock size during an interval of time.

Crude birth rate

The childbearing trend in the population is measured by the birth rate, which is expressed in terms of number of births per 1 000 population.

The crude birth rate is calculated by dividing the number of known “live births⁽³⁾” born in a calendar year by the average population size during the calendar year. Usually the mid-year population is taken as the average population size.

Thus, in 2020, with 43 000 live births and a mid-year population of 7 481 800, the crude birth rate is equal to

$$\left(\frac{43\,000}{7\,481\,800} \times 1\,000 \right) = \underline{\underline{5.8^{\wedge}}}$$

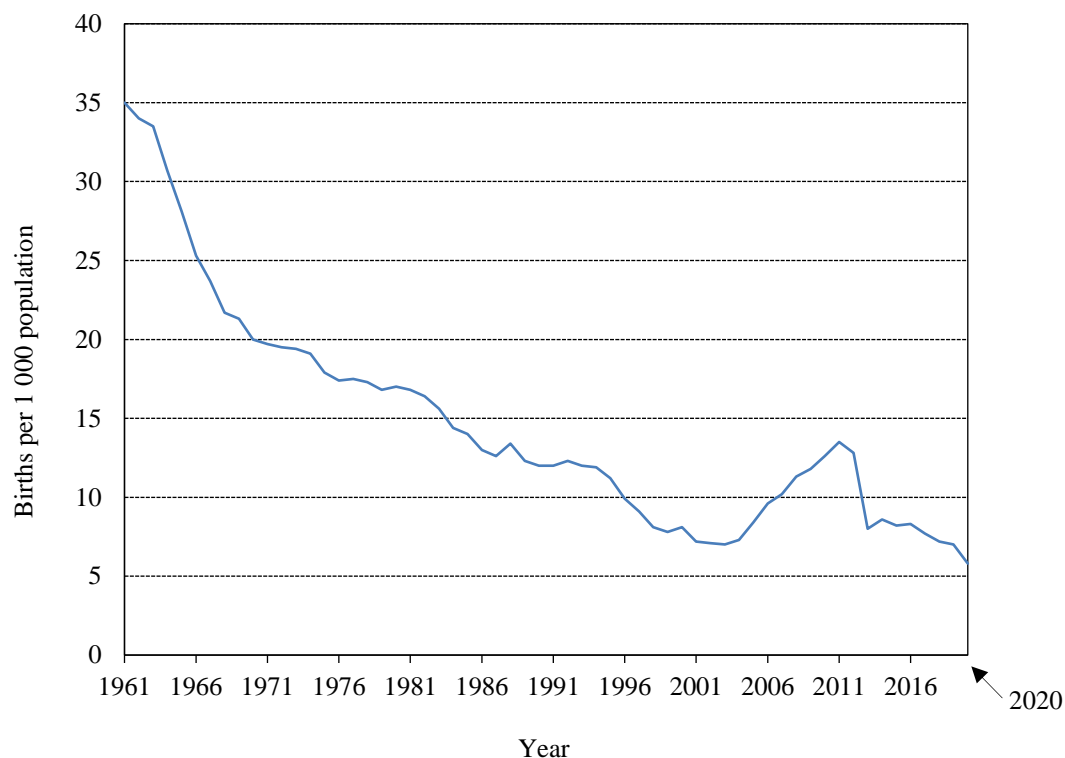
or 5.8[^] per 1 000 population.

Note :

- (3) Live births are defined as babies born with evidence of life, such as respiration, movement of voluntary muscles or heartbeat after complete expulsion or extraction.

1 Population size and growth

Chart 1.3 Crude birth rate, 1961 – 2020



General fertility rate

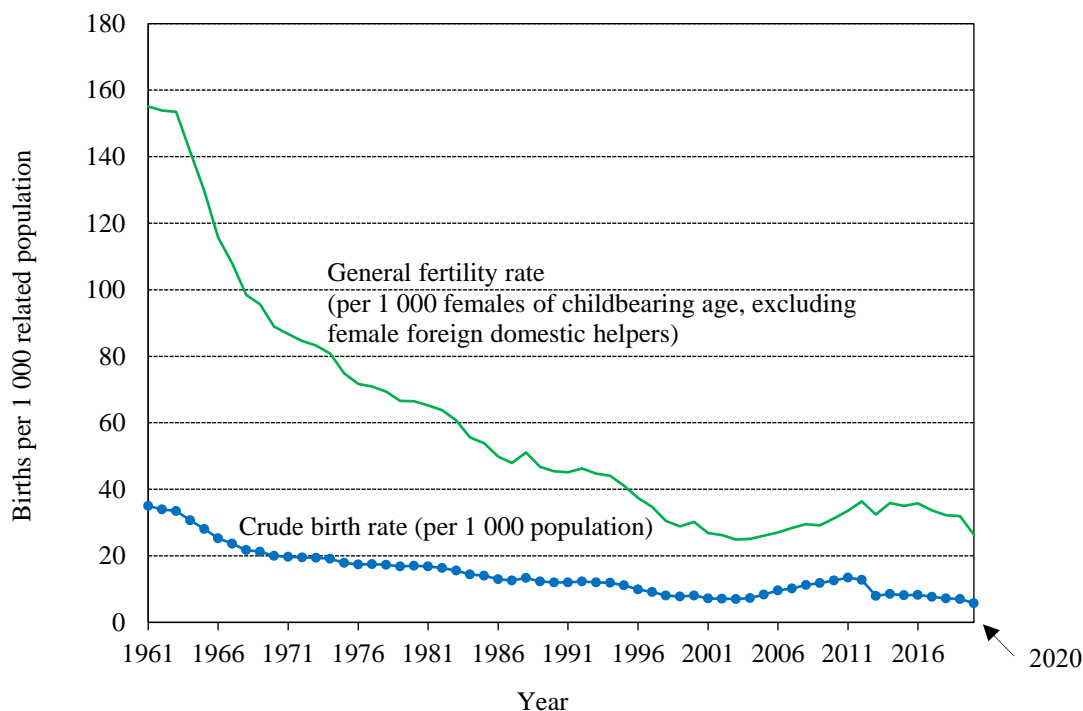
Sometimes, the crude birth rate does not reflect correctly the birth trend. For instance, an inflow of male immigrants increases the population size, leading to a lowered birth rate, but the birth trend may not have changed actually.

This pitfall can be avoided by using the general fertility rate, which relates the number of births to the number of women of childbearing age (i.e. those aged 15 to 49) in the population. The rate is usually expressed in terms of number of births per 1 000 females of childbearing age.

There is a special issue for Hong Kong. There are a large number of female foreign domestic helpers working in Hong Kong, yet the great majority of whom will not give birth to children here. To better reflect the fertility situation in Hong Kong, female foreign domestic helpers are excluded from the number of women of childbearing age in computing the general fertility rate.

1 Population size and growth

Chart 1.4 General fertility rate and crude birth rate, 1961 – 2020



Decline in birth trend

Since the 1970's, the birth rate in Hong Kong has been falling rapidly. This is mainly because of late marriage. The median age of women who got married for the first time⁽⁴⁾ was 22.9 in 1971, while that in 2020 was 30.4.

Over the same period, there is also a significant increase in the prevalence of spinsterhood. In 1971, the percentage of never married women in the age group 40-44 was 3%. In 2016, this percentage reached 16%.

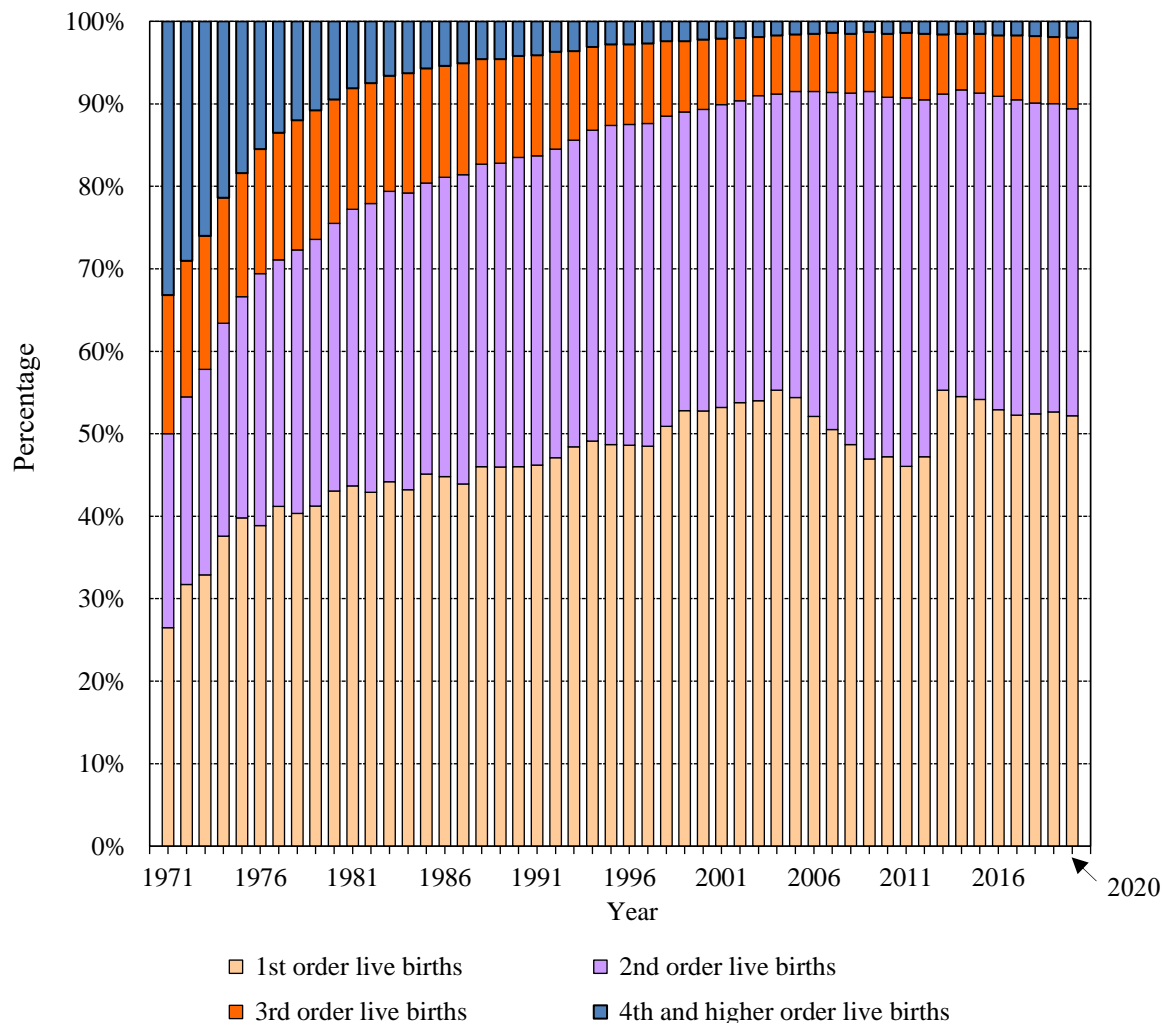
Furthermore, people tend to have children later after marriage and have fewer children than before. Among all the births recorded in 2020, 89.3% were the first or second births to their mothers as compared with 83.5% in 1990. Correspondingly, the average size of domestic households dropped from 3.6 persons per household in 1990 to 2.8 in 2020, indicating a tendency towards the formation of smaller households.

Note :

- (4) Median age at first marriage is an indicator of the average age of persons at their first marriage such that 50% of these persons are above this age while the other 50% are below it.

1 Population size and growth

Chart 1.5 Live births by order, 1971 – 2020



Crude death rate

To measure the death trend, the crude death rate is calculated by dividing the number of known deaths in a calendar year by the average population size during the calendar year. Usually the mid-year population is taken as the average population size and the crude death rate is expressed in terms of number of deaths per 1 000 population.

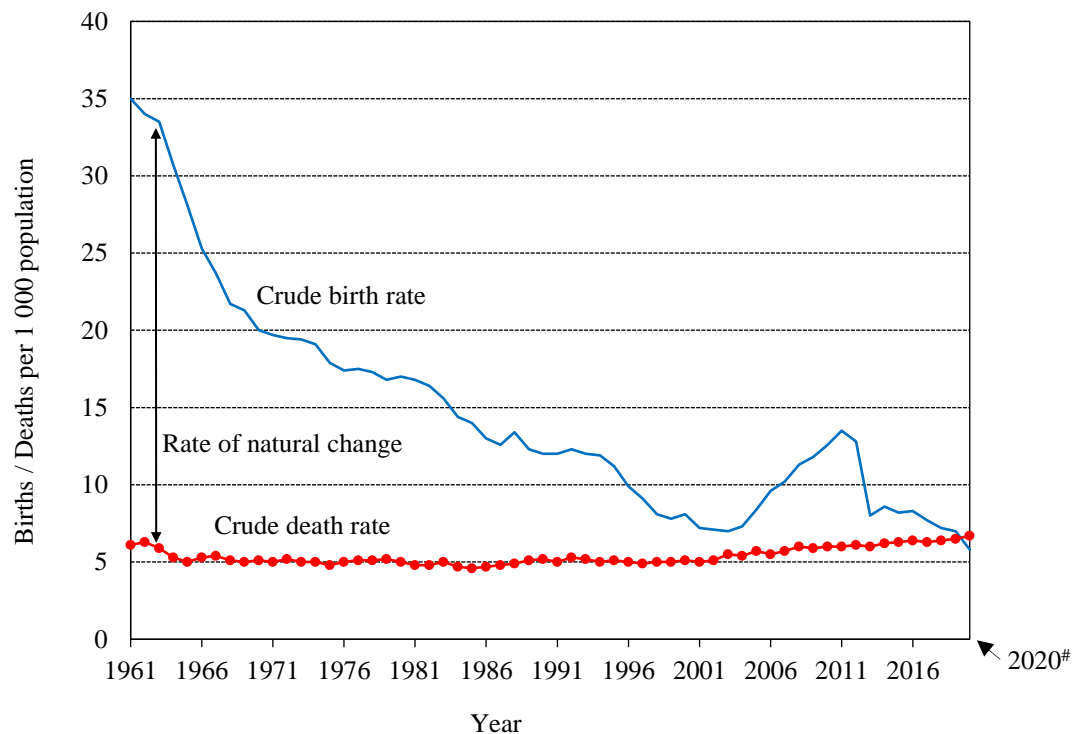
In 2020, with 49 800[#] deaths and a mid-year population of 7 481 800, the crude death rate equals

$$\frac{49\,800^{\#}}{7\,481\,800} \times 1\,000 = \underline{\underline{6.7^{\#}}}$$

or 6.7[#] per 1 000 population.

1 Population size and growth

Chart 1.6 Crude birth rate and crude death rate, 1961 – 2020



Rate of natural change

The excess of known live births over known deaths occurring in a year is called the natural change in population.

The rate of natural change is given as the excess of known live births over known deaths occurring in a year per 1 000 mid-year population of that year. This indicator shows that the rate at which the population growth is due to vital events (viz. births and deaths) only. The gain or loss in population due to net movement is not taken into account.

During the year 2020, there were 43 000 known live births and 49 800[#] known deaths. With a mid-year population of 7 481 800, the rate of natural change during the year equals

$$\left(\frac{43\,000 - 49\,800^{\#}}{7\,481\,800} \times 1\,000 \right) = \underline{\underline{-0.9^{\#}}}$$

or $-0.9^{\#}$ per 1 000 population.

1 Population size and growth

Alternatively, the rate of natural change may be computed by the difference between the crude birth rate and the crude death rate. For the above example, the rate of natural change may also be calculated as crude birth rate for 2020 minus crude death rate for 2020 (i.e. $5.8^{\wedge} - 6.7^{\#} = -0.9^{\wedge}$) or -0.9^{\wedge} per 1 000 population (see Chart 1.6).

Effect of age structure on birth and death rates

For a population with more women at childbearing age, the crude birth rate will normally be higher. For a population with more old people, the crude death rate can be expected to be higher. It is therefore necessary to study the age composition of a population before definitive statements can be made about its birth and death trends. More in-depth studies of the population will adopt appropriate methods to isolate the age composition effects such that the birth and death trends at different points of time or among different countries can be meaningfully compared.

Expectation of life at birth

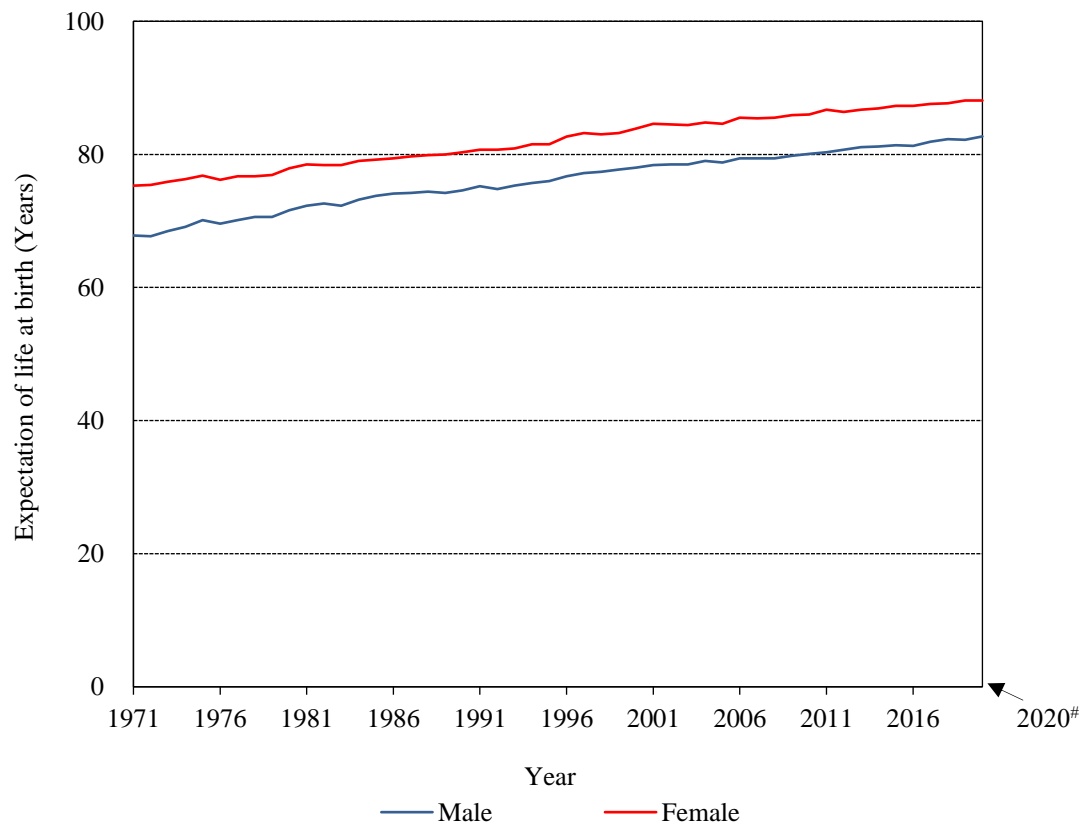
The crude death rate for the population of Hong Kong has been greatly reduced since the 1950's, which fell from 10.2 per 1 000 population in 1951 to 5.0 per 1 000 population in 1971. The rate has remained rather stable since then. It has to be noted, however, that at a time when the population of old persons is increasing, a stable crude death rate actually suggests an overall improvement in the death trend.

A lower death trend would mean that people can expect a longer life. Thus, the death trend may also be measured by the “expectation of life at birth”. This indicates how long a child born in a year, say 2020, would expect to live, assuming that upon reaching various ages in his / her life, he / she would be subject to the same death risks as those faced by people of the respective ages in 2020.

The expectation of life at birth in 2020 was 82.7[#] years for males and 88.1[#] years for females, representing a substantial increase of 8.1[#] years for males and 7.9[#] years for females since 1990.

1 Population size and growth

Chart 1.7 **Expectation of life at birth, 1971 – 2020**

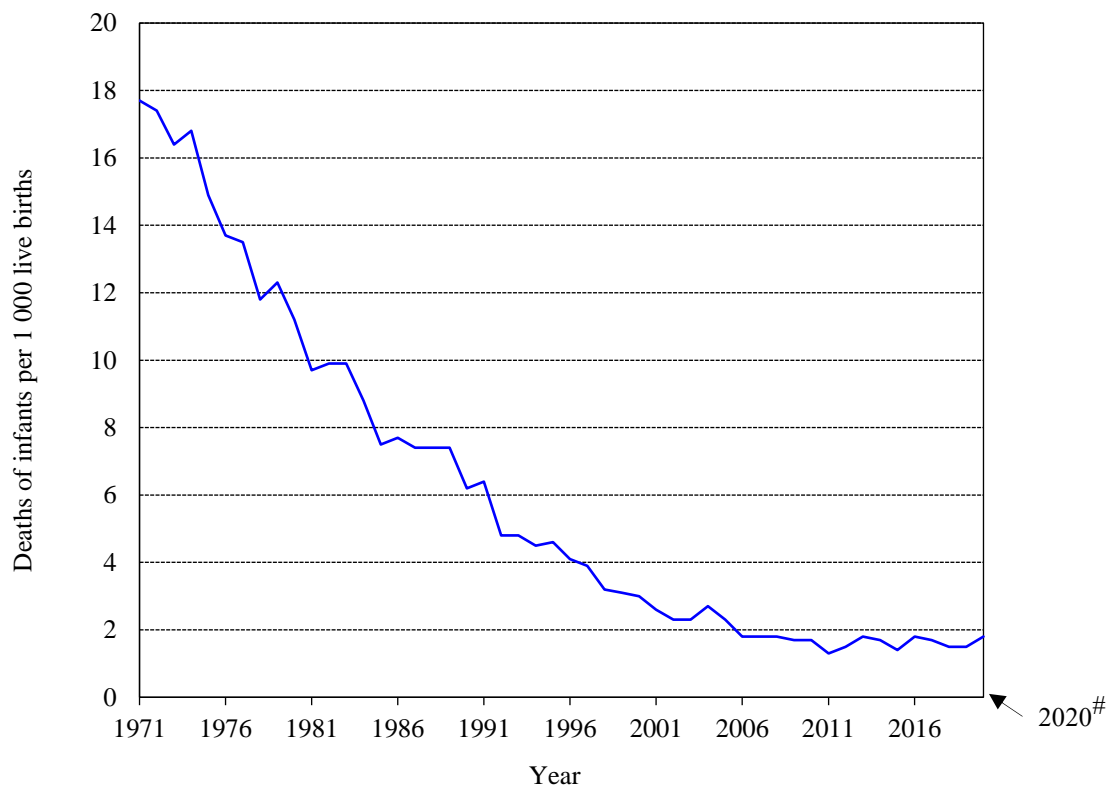


1 Population size and growth

Infant mortality rate

The decline in death rate in the past 49 years was partly due to improvements in birth care and child health, which reduced deaths of infants. The relevant indicator to study the phenomenon is the infant mortality rate, which is obtained by dividing the number of deaths of infants aged under one year by the total number of live births. The rate is usually expressed in terms of deaths per 1 000 live births.

Chart 1.8 Infant mortality rate, 1971 – 2020

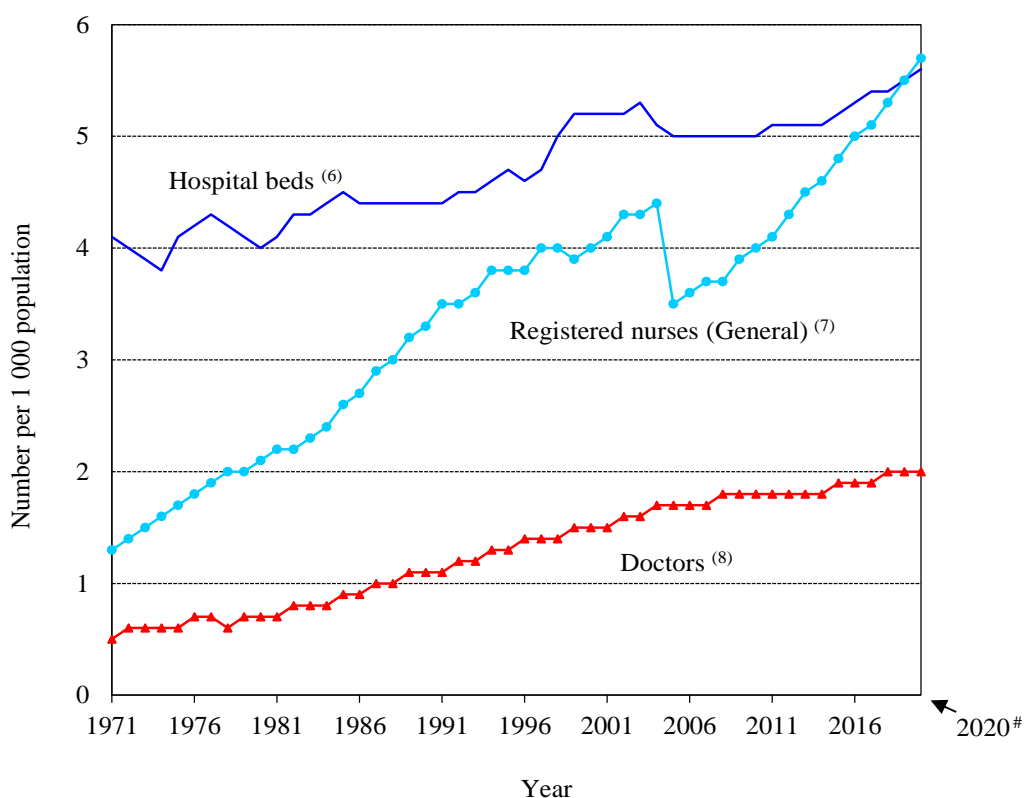


1 Population size and growth

Better medical and health services

The general decline in death trend can also be associated with better medical and health services. Besides, people are having more knowledge about health and are more health conscious now.

Chart 1.9 Rate of hospital beds and selected types of registered healthcare professionals, 1971 – 2020⁽⁵⁾



Notes :

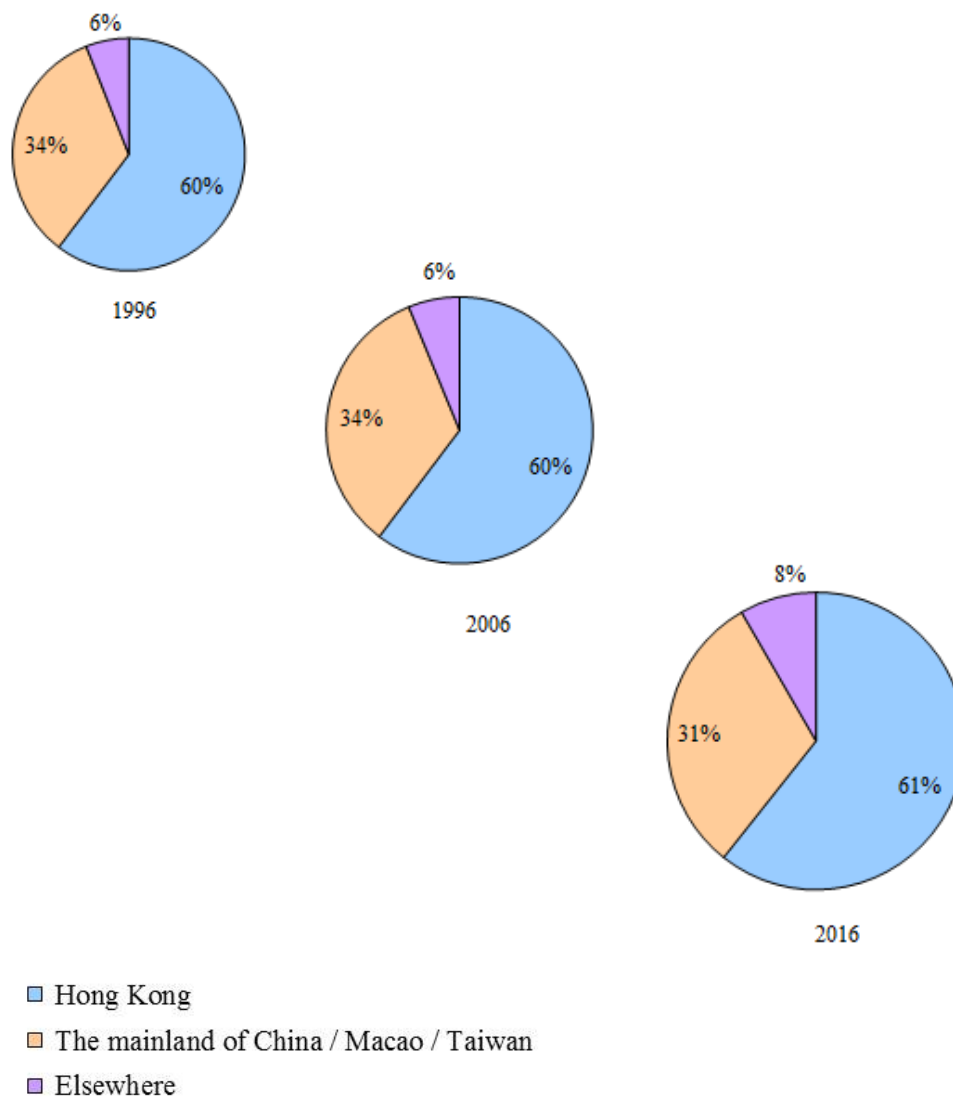
- (5) Figures are as at end of the year.
- (6) Figures include all hospital beds in Hospital Authority hospitals, private hospitals, nursing homes and correctional institutions, which follow the coverage of the Hospitals, Nursing Homes and Maternity Homes Registration Ordinance, Cap. 165, Laws of Hong Kong. Prior to 2019, the number of private hospital beds included inpatient beds only. Starting from 2019, the total number of private hospital beds included both inpatient beds and day beds.
- (7) The drop in 2005 was due to the removal of names of more than 6 000 registered nurses (General) from the register / roll in accordance with Section 7(3)(e) and Section 13(3)(e) of the Nurses Registration Ordinance, Cap. 164, Laws of Hong Kong.
- (8) Figures refer to doctors with full registration on the local and overseas lists.

1 Population size and growth

Movement of population

A substantial part of the Hong Kong population are entrants from the Mainland. Nevertheless the locally born population remains the largest group. This can be seen by comparing the proportion of the population by their place of birth.

Chart 1.10 Distribution of population by place of birth, 1996, 2006 and 2016⁽⁹⁾



Note :

- (9) Statistics shown in the charts above refer to information collected via population by-censuses. Areas of the pie charts are proportional to the population sizes in the corresponding years.

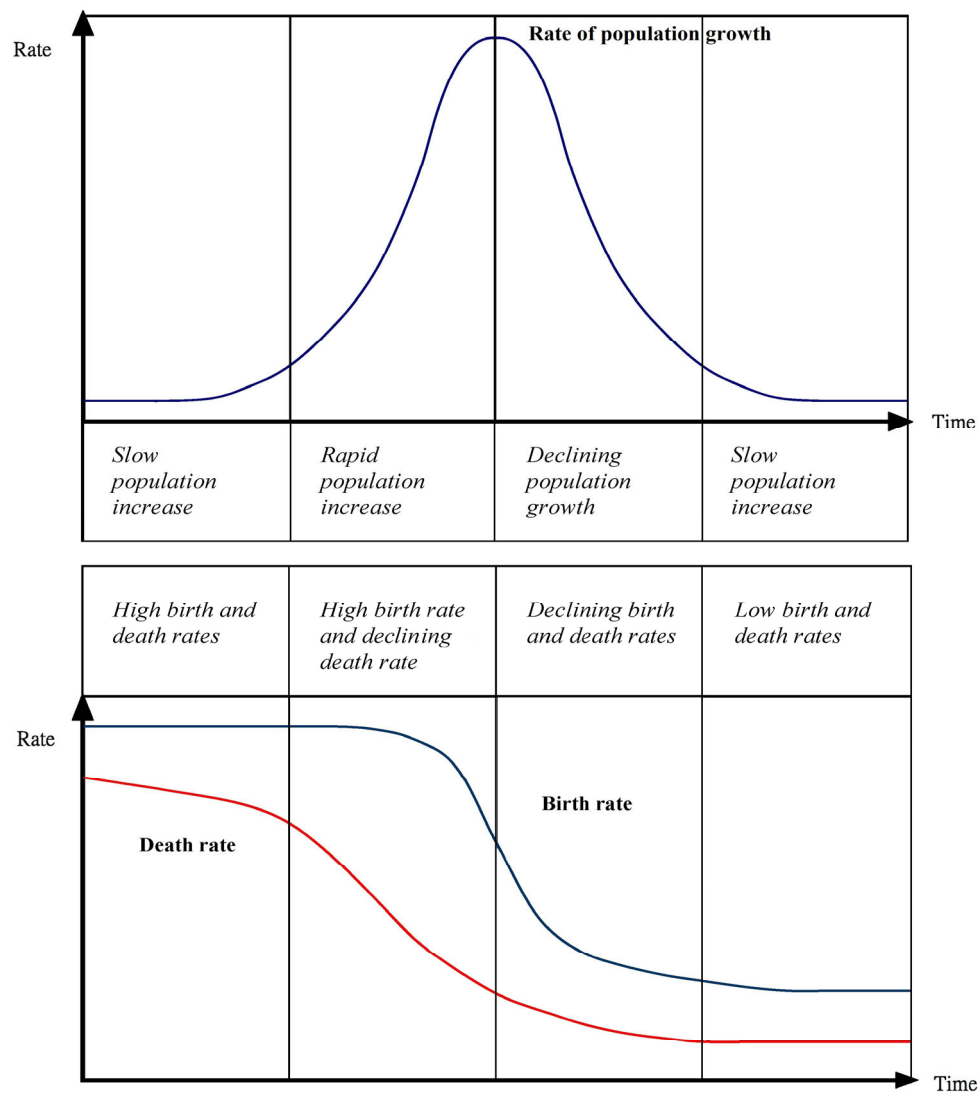
1 Population size and growth

Demographic transition model as a general pattern of population growth

The demographic transition model describes changes in birth and death rates as a population passes from a traditional society to an urbanised and industrialised one. Generally, birth and death rates are high in traditional societies and low in modern societies. According to different rates of birth and death, changes in population are thought to occur in four stages:

- (1) high birth and death rates;
- (2) high birth rate and declining death rate;
- (3) declining birth and death rates; and
- (4) low birth and death rates.

Chart 1.11 Demographic transition model



1 Population size and growth

As the population grows naturally by excess of births over deaths, it would increase at varying speeds in these different stages. This, of course, assumes that flows of movement are not significant. Otherwise, rather different pictures can emerge.

Further information

The above contents present only part of the information produced by C&SD on the topics concerned. For further information regarding the topics discussed in this chapter (e.g. latest statistics, statistical reports, concepts and methods), please visit the following sections of the C&SD website :

[Population estimates](#)

[Population censuses and by-censuses](#)

[Demographics](#)

[Health](#)

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

Note :

- ^ Growth rates of the population, crude birth rate, crude death rate and rate of natural change are calculated based on unrounded population figures.

1 Population size and growth

Exercise

Growth patterns of different countries

Births, deaths and net movements are the three factors affecting population growth. Annual growth rates, rates of natural change, crude birth rates and crude death rates are useful indicators of the growth pattern.

Readers may try to calculate these rates from the table below where data on population size, births and deaths are given for different countries.

The aim of this exercise is to enable readers to get familiarised with the fundamental concepts in population growth.

Generally speaking, the rate of natural change may be taken as the difference between the crude birth rate and the crude death rate.

To further test one's understanding of the demographic transition model as a general pattern of population growth, the second part of this exercise is to classify those countries into different transitional stages based on the birth and death rates computed in the first part. There are no universal rules to classify such rates as high or low. However, as a practical guide, a crude birth rate of 25 per 1 000 population or above may be regarded as high; and a crude death rate of 15 per 1 000 population or above can be considered as high.

- (1) From the data given below, complete the table.
(Figures are given in thousands; rates are expressed in “per 1 000 population”.)

Country	Mid-year population at year T	No. of births in year T	No. of deaths in year T	Crude birth rate	Crude death rate	Rate of natural change
Country A	29 863	1 322	525			
Country B	15 941	723	332			
Country C	20 155	249	132			
Country D	32 268	332	226			
Country E	9 749	433	181			
Country F	1 315 844	17 558	8 795			
Country G	74 033	1 860	421			
Country H	1 517	51	17			
Country I	82 689	702	853			
Country J	10 098	96	132			

1 Population size and growth

- (2) From the rates obtained in part (1), classify the countries into various stages of the demographic transition model.

Stage (1) (High birth and death rates)	Stage (4) (Low birth and death rates)

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2 Population structure



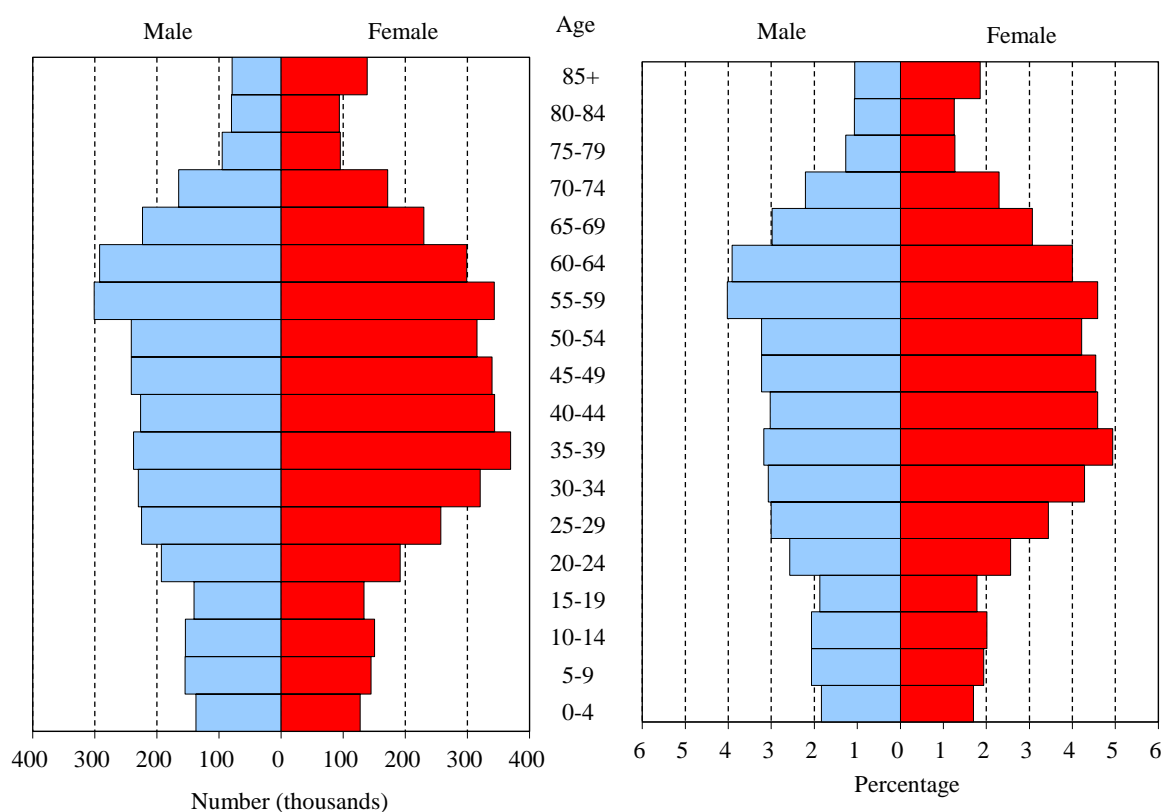
Introduction

Individuals differ in terms of their sex, age, employment, and so on. A population, made up of individuals, is characterised by the distribution of individuals in regard to these features. This chapter introduces various measures for describing population characteristics and their changes over time.

Population pyramid

The age-sex distribution of a population is most clearly presented in the graphical form of a “population pyramid”. The pyramid can be scaled in either population numbers or percentages. The percentage distribution is more appropriate for comparison of two or more populations.

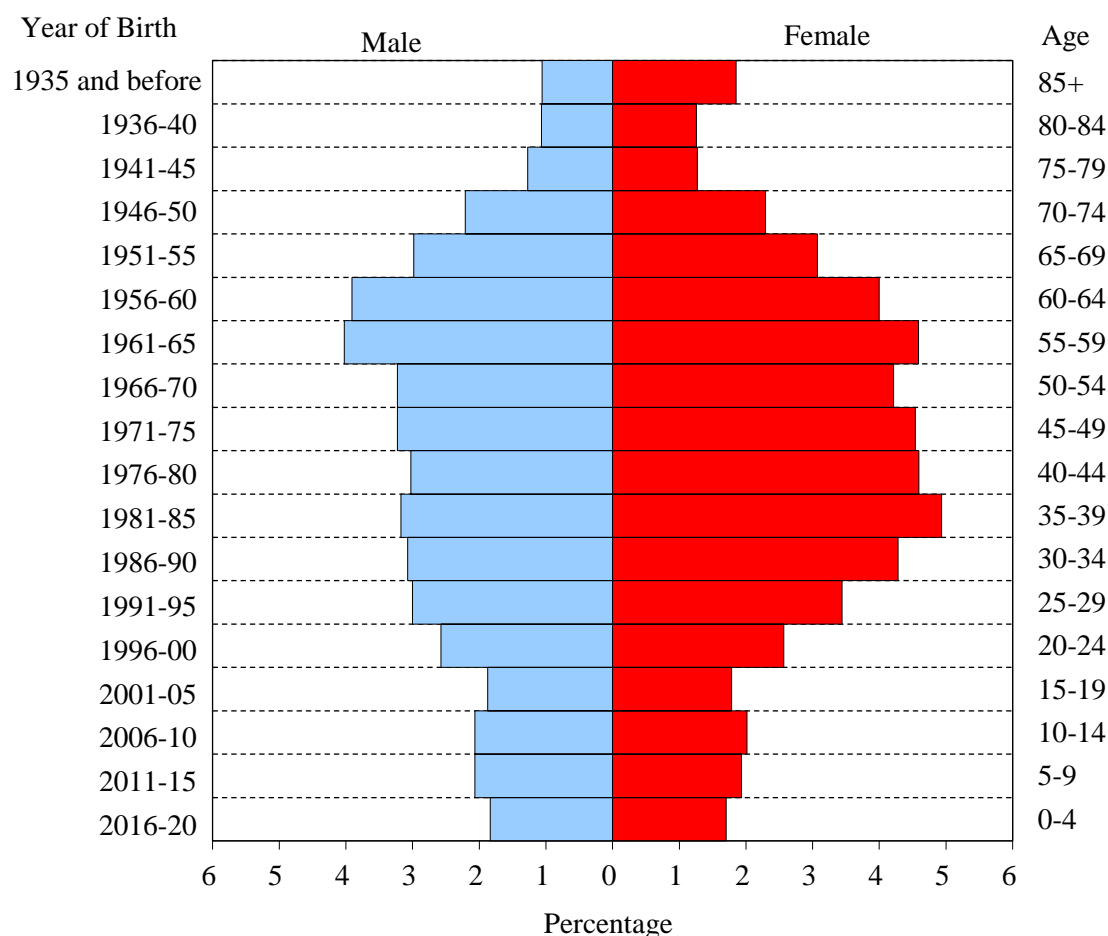
Chart 2.1 Population of Hong Kong by age and sex, mid-2020



2 Population structure

The age-sex distribution reflects the combined effects of the past and recent trends in births, deaths and net movements. It is a rather persistent feature, and will not change drastically in a short span of time. Irregularities, like age or sex groups of exceptional size, reflect unusual numbers of births, deaths or net movements at some points of time in the past. Normally, births and net movements have larger impacts on the age-sex distribution than deaths.

Chart 2.2 Age-sex distribution of Hong Kong population, mid-2020

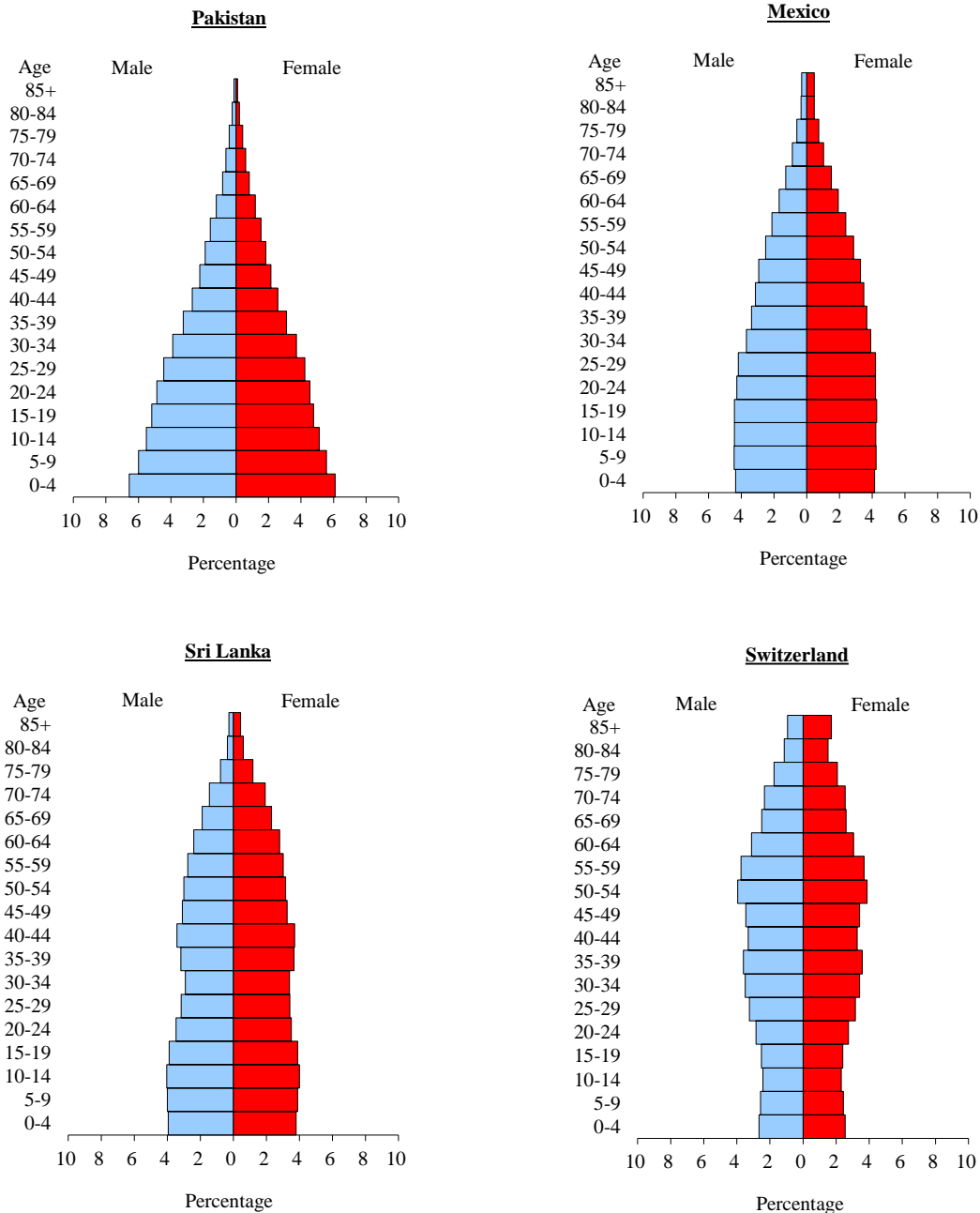


Shape of population pyramid in relation to the growth pattern of a population

In a growing population with high birth rates, the numbers of people in younger age groups are larger and the age structure would take on the shape of a typical pyramid. If death rates are also high, the pyramid, which has a broad base, would narrow rapidly towards the top. Conversely, as the birth trend declines and the death trend improves, the pyramid would have a relatively narrow base and a middle section of nearly the same width; it does not begin to converge to the vertex until after very old age groups.

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Chart 2.3 Population pyramids (in percentage) of selected countries, 2020



Source : *Population Pyramid.net*

The shape of a population pyramid is thus closely related to the growth pattern of a population. Countries in different transitional stages may take on varying shapes of the population pyramid for their age-sex structures. For instance, the pyramid for Pakistan (2020) has a very broad base that narrows upwards very rapidly. It has almost a triangular shape. It results from a very high crude birth rate of 27.4 per 1 000 population⁽¹⁾ and relatively low expectation of life at birth, 66.5 years⁽¹⁾ for males and 68.5 years⁽¹⁾ for females.

In contrast, the pyramid for Switzerland (2020) has a much narrower base, a little bit wider middle section and a slowly converging tip. The shape is almost semi-elliptical. It illustrates the effects of a low crude birth rate of 10.2 per 1 000 population⁽¹⁾ and high expectation of life at birth, 82.0 years⁽¹⁾ for males and 85.7 years⁽¹⁾ for females.

The pyramids for Mexico (2020) and Sri Lanka (2020) illustrate configurations intermediate between those for Pakistan and Switzerland; their crude birth rates were 17.0 and 15.3 per 1 000 population⁽¹⁾ respectively and their respective expectations of life at birth were 75.1 and 73.8 years⁽¹⁾ for males and 77.9 and 80.4 years⁽¹⁾ for females.

Expectation of life at birth is preferred to crude death rate as an indicator of death trend here because the crude death rates for the four countries are found highly distorted by the different age structures of their populations.

Apart from the natural effect of births and deaths, it should be noted that these four pyramids are affected by other irregular variations and therefore may deviate from the theoretical triangular and semi-elliptical shapes that the demographic transition model prescribes.

Besides the detailed description of age-sex structure provided by the population pyramid, the age-sex distribution of a population can also be given by other summary measures.

Sex ratio

To compare the relative size of the male group and female group in the population, the sex ratio is calculated. The ratio is obtained by dividing the number of males in the population by the number of females. The sex ratio is usually expressed as the number of males per 1 000 females.

At mid-2020, there were 3 416 300 males and 4 065 500 females in Hong Kong. Thus the sex ratio was

$$\frac{3\,416\,300}{4\,065\,500} \times 1\,000 = 840$$

or 840 males per 1 000 females.

Note :

(1) Source – World Data Atlas

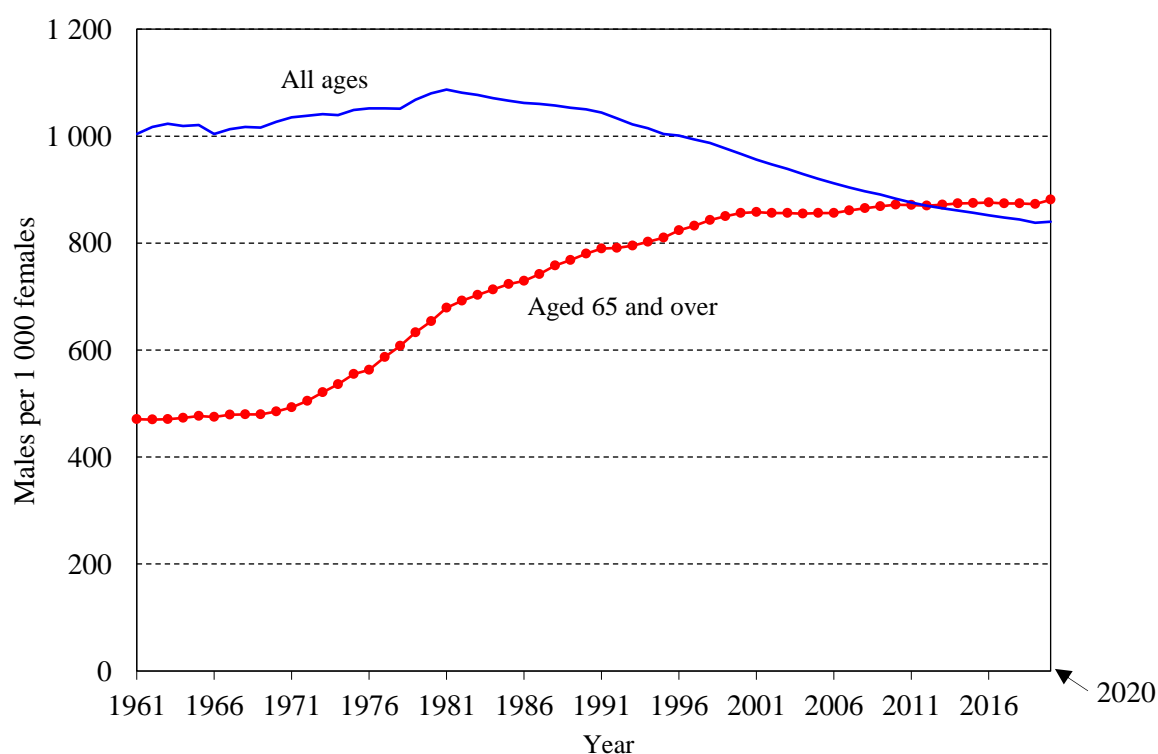
2 Population structure

Sex ratio by age group

Sex ratio may also be calculated separately for various age groups. For instance, the sex ratio at birth compares the number of male births to female births. Usually, as a biological norm, slightly more male babies are born than female babies.

<u>Age group</u>	Sex ratio (number of males per 1 000 females)		
	<u>Mid-2010</u>	<u>Mid-2015</u>	<u>Mid-2020</u>
0-14	1 072	1 070	1 055
15-19	1 061	1 062	1 049
20-24	949	984	1 004
25-29	756	786	873
30-34	707	678	717
35-39	719	674	643
40-44	758	706	659
45-49	859	760	711
50-54	968	865	765
55-59	985	972	878
60-64	1 007	976	978
65 and over	872	875	881
All ages	883	857	840

Chart 2.4 Sex ratio of Hong Kong population by age group, mid-1961 to mid-2020



2 Population structure

As revealed by the above chart, the sex ratio for the older ages was on the rise over the years. This reflects a greater improvement in the death trend for males than for females in recent years.

Increasing proportion of females in Hong Kong population

In Hong Kong, the proportion of females in the total Hong Kong population increased continuously in the past 10 years. The sex ratio of the population remained below parity and was consistently on a decreasing trend. The ratio dropped from 883 in mid-2010 to 840 in mid-2020.

The increase in the proportion of females in the population was brought about by three major factors.

Effect of foreign domestic helpers

Firstly, there was a significant number of foreign domestic helpers in Hong Kong, who were mostly young and middle-aged females. Owing to this factor, the number of females in the age group of 20-39 was relatively large, with the corresponding sex ratio at mid-2020 being 777 males per 1 000 females.

<u>Age group</u>	Sex ratio (number of males per 1 000 females)		
	<u>Mid-2010</u>	<u>Mid-2015</u>	<u>Mid-2020</u>
0-19	1 068	1 068	1 054
20-39	770	761	777
40-64	901	847	794
65 and over	872	875	881
All ages	883	857	840

After excluding foreign domestic helpers, the sex ratio for the age group of 20-39 at mid-2020 rose to 940. The sex ratio for the entire population was 913.

<u>Age group</u>	Sex ratio excluding foreign domestic helpers (number of males per 1 000 females)		
	<u>Mid-2010</u>	<u>Mid-2015</u>	<u>Mid-2020</u>
0-19	1 068	1 069	1 054
20-39	928	934	940
40-64	946	900	859
65 and over	872	875	882
All ages	952	932	913

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Effect of one-way permit holders from the Mainland

The second factor contributing to the increasing proportion of females in the population was that a large proportion of the one-way permit holders from the Mainland were women who came to Hong Kong to join their husbands. In 2020, there were 10 134 one-way permit holders from the Mainland and about 58% of these new entrants were females.

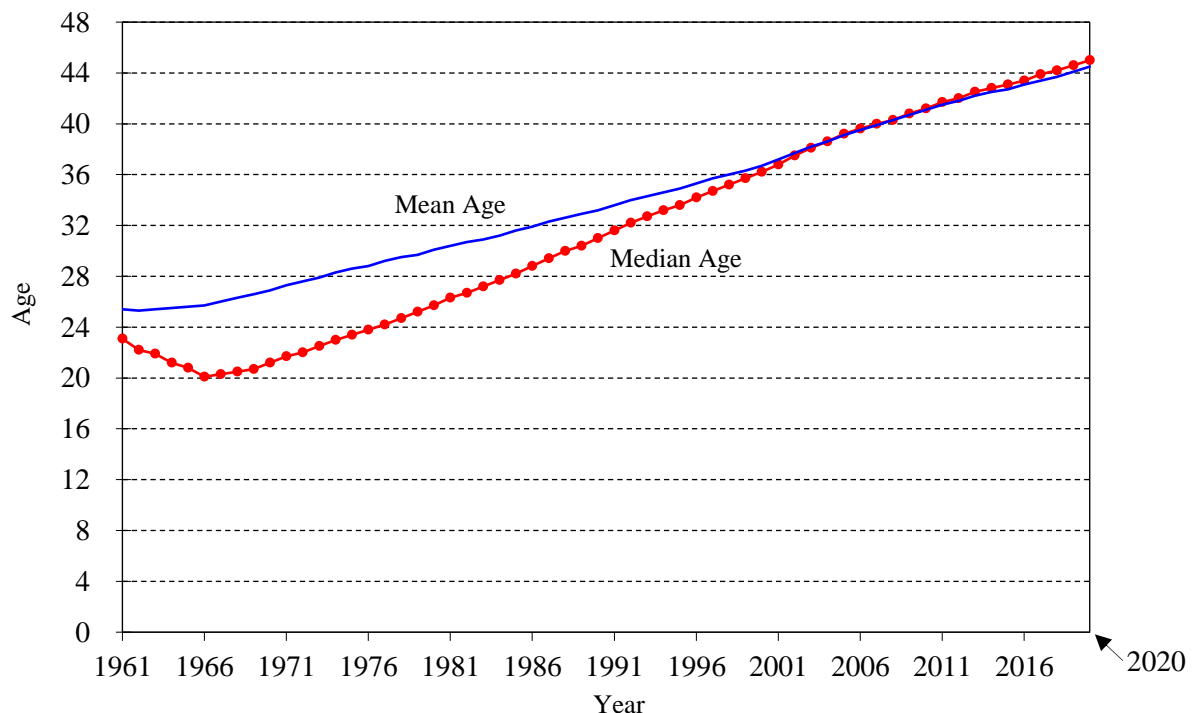
Effect of higher expectation of life for females

The third factor is that females generally live longer than males. The expectation of life at birth of females was 88.1[#] years while that for males was only 82.7[#] years in 2020.

Mean and median ages

To describe the age structure of a population, its average age can be used. A simple average, or the “mean”, can be obtained by dividing the sum of ages of the total population by the population size. Alternatively, a measure is provided by the “median” age of the population. Median age of the population is an indicator of the average age of the population such that 50% of the total population are above this age while the other 50% are below it.

Chart 2.5 Mean and median ages of Hong Kong population, mid-1961 to mid-2020



“Median” is normally a better measure of its average value in a set of data if there are extreme values, since the “mean” will be much affected by those extreme values. In the case of age, the general experience is that the median age is considered more preferable.

“Young” and “old” populations

A population may be described as “young” or “old”.

A population may be considered as “ageing” when its median age is on the rise.

Dependency ratios

It is interesting and useful to divide the population into three groups by age, namely the young (i.e. those aged 0 to 14), those in the working age (i.e. aged 15 to 64) and the elderly (i.e. aged 65 and over) and study their relative sizes.

The overall dependency ratio is computed by dividing the number of the young and the elderly in the population by those in the working age. The components of this measure may be calculated separately as the “child dependency ratio” and “elderly dependency ratio”.

Given the following population data for Hong Kong in mid-2020, the various dependency ratios are computed accordingly:

<u>Age group</u>	<u>Population at mid-2020</u>
0-14	869 300
15-64	5 240 700
65 and over	1 371 800

Child dependency ratio

$$= \frac{869\,300}{5\,240\,700} \times 1\,000 = \underline{\underline{166}}$$

or 166 persons aged under 15 per 1 000 population of working age.

2 Population structure

Elderly dependency ratio

$$= \frac{1\,371\,800}{5\,240\,700} \times 1\,000 = \underline{\underline{262}}$$

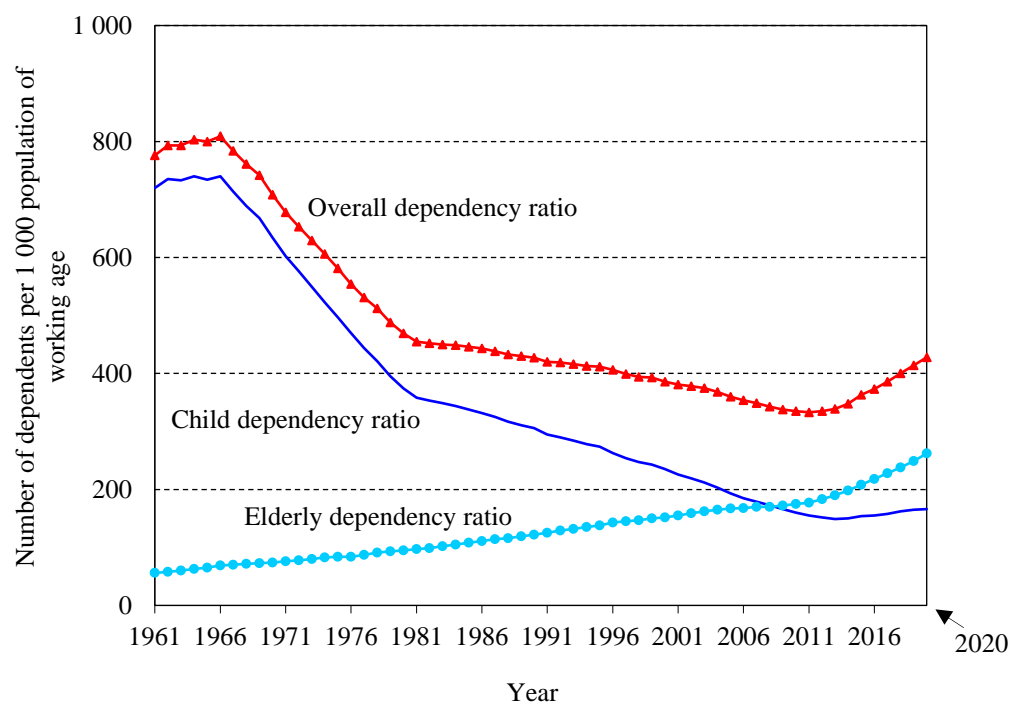
or 262 persons aged 65 and over per 1 000 population of working age.

Overall dependency ratio

$$= \frac{869\,300 + 1\,371\,800}{5\,240\,700} \times 1\,000 = \underline{\underline{428}}$$

or 428 persons aged under 15 or aged 65 and over per 1 000 population of working age.

Chart 2.6 Dependency ratios of Hong Kong population, mid-1961 to mid-2020



2 Population structure

Geographical distribution of the population

Hong Kong is delineated into 18 geographical districts: 4 on Hong Kong Island; 5 in Kowloon and 9 in the New Territories (including Islands). These geographical districts are called District Council districts. The numbers of people living in different districts vary considerably. Geographical distribution of the land-based non-institutional population is analysed in the ensuing paragraphs.

In 2020, 686 700 persons lived in the Kwun Tong district. It was the most populated district. There were only 173 300 persons living in the Wan Chai district, which was the least populated district.

The proportion of the population living on Hong Kong Island decreased from 18.3% in 2010 to 16.3% in 2020 while the proportion living in the New Territories increased from 52.1% to 52.9%. This change in the geographical distribution of the population reflects the effectiveness of the Government's policy in regard to the development of new towns in the New Territories.

Land-based non-institutional population by District Council district, 2020

District Council district	Land-based non-institutional population
Central and Western	236 000
Wan Chai	173 300
Eastern	537 900
Southern	260 800
Yau Tsim Mong	323 000
Sham Shui Po	433 500
Kowloon City	419 200
Wong Tai Sin	414 200
Kwun Tong	686 700
Kwai Tsing	500 900
Tsuen Wan	310 000
Tuen Mun	495 000
Yuen Long	640 600
North	314 500
Tai Po	307 900
Sha Tin	684 800
Sai Kung	472 800
Islands	184 700

2 Population structure

Employment structure of the population

“Economically active” persons are those aged 15 and over who are either working or seeking jobs. These people make up the “labour force”. Children at school, the retired and home-makers are economically inactive persons.

The labour force of Hong Kong increased from 3.63 million in 2010 to 3.98 million in 2018, and then decreased gradually to 3.89 million in 2020.

“Labour force participation rates” are used to measure the proportion of economically active persons in the population aged 15 and over. These rates are usually calculated separately for males and females in different age groups. Since more women tend to concentrate on household duties, their labour force participation rates are generally lower than those for males. The age specific labour force participation rates for males are highest at their prime working ages (i.e. 25 to 49) while the rates for females reach the peak at the age group 25-29 and decline gradually in the older age groups.



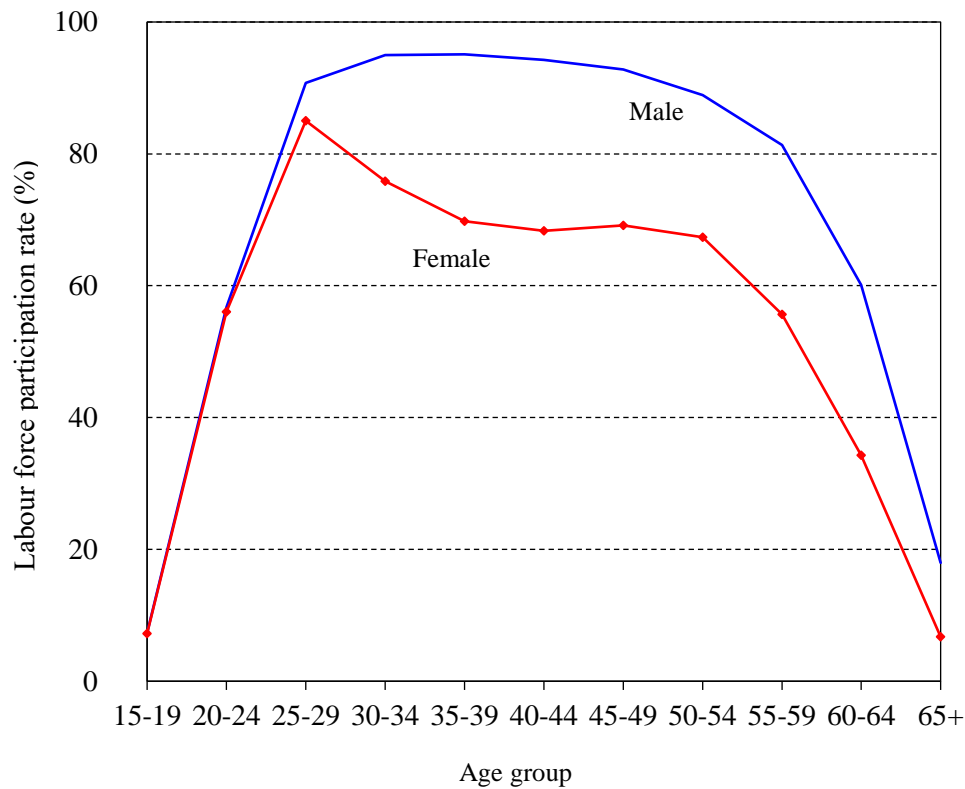
Information on the labour force, employment, unemployment and underemployment is collected through the General Household Survey.

The labour force participation rates in the age groups 15-19 and 65 and over for both sexes in 2020 were substantially lower than those in other age groups, as most members of the former group were still at school while a fair proportion of those in the latter group were retired people.

The characteristics of foreign domestic helpers differ from those of the entire population, particularly in their labour force participation rates. Because of this, the age-sex specific labour force participation rates presented in Chart 2.7 have excluded foreign domestic helpers in order to better reflect the profile of the local population.

2 Population structure

Chart 2.7 Labour force participation rates of Hong Kong population (excluding foreign domestic helpers), 2020



For employed persons who are working, their characteristics can be described in terms of the occupations and industries in which they are engaged.

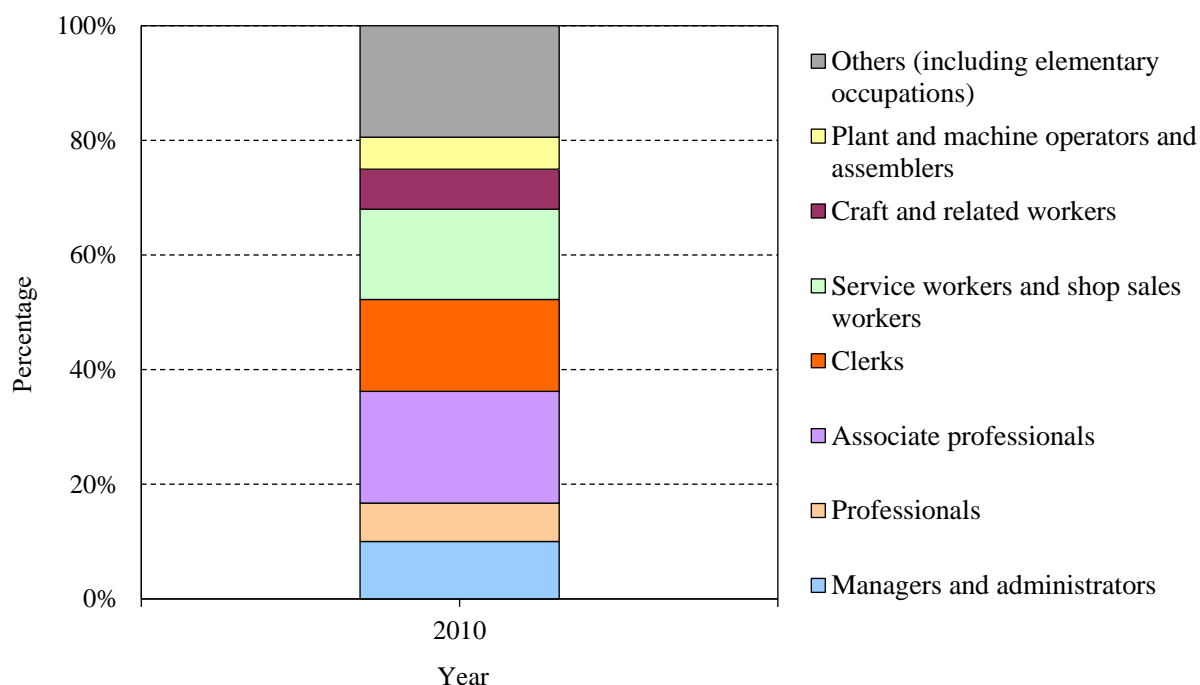
Distribution of employed population by occupation

Occupation refers to the kind of work that a person does. Examples are teachers, doctors, engineers, shop sales workers, security guards, knitting machine operators and clerks.

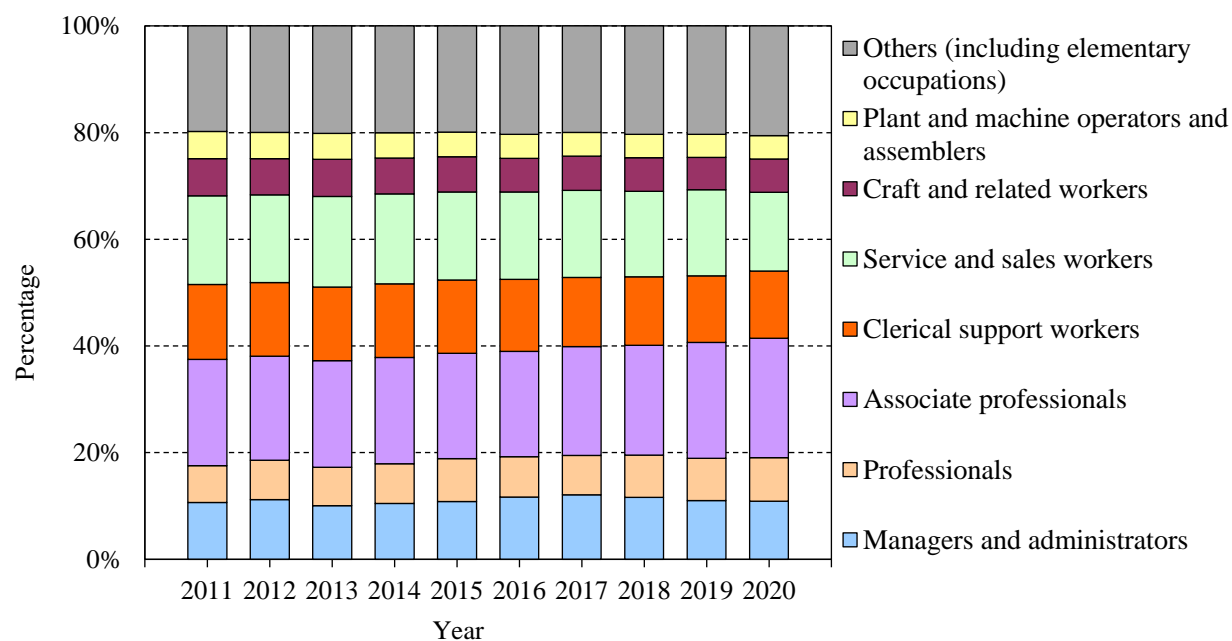
2 Population structure

Chart 2.8 Distribution of employed population by occupation⁽²⁾, 2010 – 2020

(a) Based on International Standard Classification of Occupations 1988 (ISCO-88)



(b) Based on International Standard Classification of Occupations 2008 (ISCO-08)



Note :

(2) Statistics for 2010 are compiled based on ISCO-88. Statistics for 2011 and onwards are compiled based on ISCO-08. Hence, figures for 2011 and onwards are not directly comparable to the figures for 2010.

2 Population structure

Distribution of employed population by industry sector

Industry, on the other hand, refers to the kind of activity carried out by the establishment or enterprise in which a person works. Examples of some establishments are schools, hospitals, shops, construction firms and factories. Examples of “industries” are business services sector, retail sector, construction sector, transportation sector and manufacturing sector.

The economic characteristics of a population reflect the stage of the society’s economic development. In general, the labour force tends to shift away from agriculture to manufacturing industries, and then to services industries.

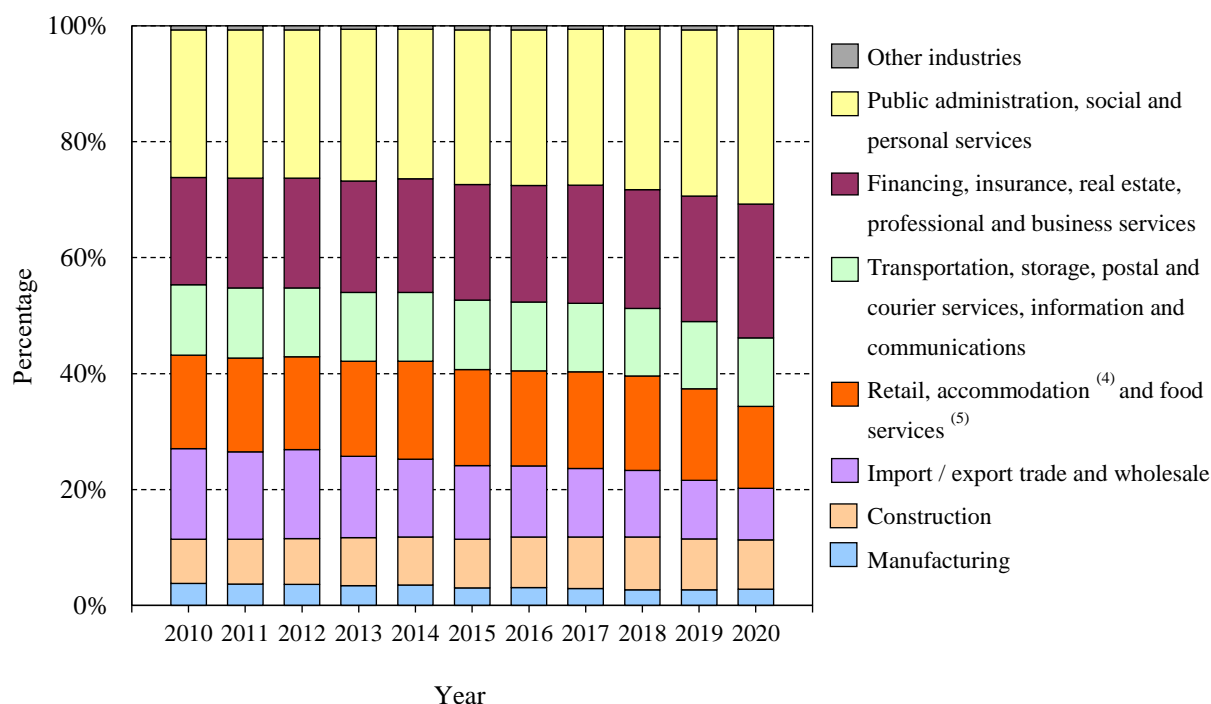
In Hong Kong, the economic characteristics of the population follow this general pattern in economic development. Over these years, the services sector in Hong Kong has been gaining increasing prominence.

Being the industry sector with the largest share of employment, the services sector as a whole engaged 3.2 million[@] persons in 2020, accounting for 88.9%[@] of the overall employment. The corresponding figures for 2015 were 3.3 million persons and 88.4%.

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Chart 2.9 Distribution of employed population by industry⁽³⁾, 2010 – 2020

Based on Hong Kong Standard Industrial Classification (HSIC)



Notes :

- (3) Figures are compiled based on Hong Kong Standard Industrial Classification Version 2.0.
- (4) Accommodation services cover hotels, guesthouses, boarding houses and other establishments providing short term accommodation.
- (5) The retail, accommodation and food services industries as a whole is generally referred to as the consumption- and tourism-related segment.

2 Population structure

Further information

The above contents present only part of the information produced by C&SD on the topics concerned. For further information regarding the topics discussed in this chapter (e.g. latest statistics, statistical reports, concepts and methods), please visit the following sections of the C&SD website :

[Population estimates](#)

[Population censuses and by-censuses](#)

[Demographics](#)

[Labour force, employment and unemployment](#)

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

2 Population structure

Exercise

Age-sex structure of the 18 districts

Population pyramid is a useful tool to depict the age-sex structure of a population.

This exercise demonstrates how to present age-sex data by means of population pyramids. It further shows how age-sex structure differs in different districts of Hong Kong, which has implications for the requirement for social services and facilities in these districts.

- (1) With reference to the age-sex data obtained from the 16BC for the 18 districts shown on pages 44 to 46, please prepare a population pyramid for each of these districts on graph papers according to the formats given on pages 47 to 49.
- (2) Please rank the 18 districts according to their ageing extent, by referring to the median age of the district populations.

District Council district	Median age	Ranking for ageing extent ^(Note) ("1" for the most aged district)
Central and Western	43.8	
Wan Chai	44.9	
Eastern	43.8	
Southern	43.9	
Yau Tsim Mong	43.2	
Sham Shui Po	42.9	
Kowloon City	43.1	
Wong Tai Sin	44.6	
Kwun Tong	43.8	
Kwai Tsing	43.5	
Tsuen Wan	43.2	
Tuen Mun	43.7	
Yuen Long	42.1	
North	42.7	
Tai Po	43.6	
Sha Tin	44.2	
Sai Kung	42.8	
Islands	42.4	

Note : Where there are ties in rank, the tied observations are assigned the mean of the ranks which they jointly occupy.

2 Population structure

- (3) With reference to the statistics shown on pages 44 to 46, please analyse how various districts may differ in their requirements for public services and facilities.

Percentage distribution of population by age and sex, June 2016

<u>Age group</u>	<u>Central and Western</u>			<u>Wan Chai</u>			<u>Eastern</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	1.6	1.5	3.1	1.5	1.5	3.0	2.0	1.9	3.9
5-9	1.7	1.7	3.5	1.8	1.7	3.6	2.0	1.8	3.8
10-14	1.6	1.5	3.1	1.6	1.5	3.1	1.6	1.6	3.3
15-19	2.3	2.1	4.4	1.9	1.9	3.8	2.3	2.2	4.4
20-24	3.2	3.4	6.6	2.2	2.5	4.7	2.8	2.9	5.7
25-29	3.4	4.2	7.6	3.0	4.5	7.6	2.9	3.9	6.8
30-34	3.1	4.9	8.0	3.1	5.5	8.6	3.2	4.9	8.0
35-39	2.9	4.9	7.7	2.8	5.2	8.1	3.1	5.0	8.1
40-44	3.0	4.7	7.7	3.0	4.7	7.7	3.2	4.6	7.7
45-49	3.0	4.8	7.8	3.0	4.9	7.9	3.1	4.5	7.6
50-54	4.0	5.4	9.4	4.3	5.5	9.7	4.0	5.0	8.9
55-59	4.3	4.4	8.7	4.3	4.5	8.9	4.2	4.3	8.5
60-64	3.2	3.2	6.4	3.3	3.5	6.8	3.2	3.4	6.6
65-69	2.6	2.8	5.4	2.6	2.6	5.2	2.8	2.9	5.8
70-74	1.3	1.5	2.8	1.5	1.5	3.0	1.5	1.4	2.9
75-79	1.4	1.4	2.8	1.3	1.5	2.8	1.4	1.5	2.8
80-84	1.0	1.2	2.2	1.1	1.4	2.5	1.0	1.4	2.4
85+	0.9	1.7	2.7	1.0	1.9	2.9	0.9	1.8	2.7
All ages	44.7	55.3	100.0	43.6	56.4	100.0	45.0	55.0	100.0
Median age	43.8			44.9			43.8		

<u>Age group</u>	<u>Southern</u>			<u>Yau Tsim Mong</u>			<u>Sham Shui Po</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	2.2	1.8	4.0	2.1	1.8	3.8	2.2	2.1	4.2
5-9	2.0	1.9	3.9	1.8	2.0	3.8	2.2	1.9	4.1
10-14	1.8	1.6	3.4	1.7	1.6	3.3	1.7	1.7	3.4
15-19	2.3	2.1	4.3	2.4	2.1	4.5	2.3	2.2	4.5
20-24	2.6	2.7	5.3	3.1	3.5	6.6	2.9	3.1	6.0
25-29	2.7	3.8	6.4	3.5	4.3	7.7	3.1	4.0	7.1
30-34	3.0	4.9	7.9	3.1	4.8	7.9	3.4	4.8	8.2
35-39	3.0	5.2	8.2	2.9	4.6	7.5	3.2	4.7	7.9
40-44	3.4	4.7	8.1	3.0	4.5	7.6	3.3	4.5	7.9
45-49	3.2	4.5	7.7	3.0	4.5	7.6	3.3	4.5	7.8
50-54	4.1	4.8	8.9	4.2	5.1	9.3	3.9	4.6	8.5
55-59	4.0	4.3	8.3	4.3	4.4	8.6	4.0	4.1	8.2
60-64	3.3	3.4	6.8	3.6	3.2	6.8	3.2	3.2	6.4
65-69	2.7	2.7	5.4	2.9	2.5	5.5	2.6	2.5	5.1
70-74	1.5	1.4	3.0	1.4	1.2	2.7	1.5	1.4	2.9
75-79	1.3	1.6	2.9	1.2	1.3	2.5	1.4	1.4	2.8
80-84	0.9	1.3	2.3	1.0	1.2	2.2	1.1	1.3	2.4
85+	0.9	2.1	3.0	0.8	1.5	2.3	0.9	1.8	2.7
All ages	45.1	54.9	100.0	46.0	54.0	100.0	46.4	53.6	100.0
Median age	43.9			43.2			42.9		

2 Population structure

Percentage distribution of population by age and sex, June 2016 (cont'd)

<u>Age group</u>	<u>Kowloon City</u>			<u>Wong Tai Sin</u>			<u>Kwun Tong</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	2.1	2.0	4.1	1.7	1.7	3.4	2.0	1.8	3.8
5-9	2.2	2.0	4.2	2.1	1.9	3.9	2.1	1.9	4.0
10-14	1.7	1.6	3.3	1.8	1.7	3.5	1.9	1.8	3.7
15-19	2.2	2.2	4.4	2.5	2.3	4.8	2.4	2.2	4.6
20-24	3.2	3.1	6.3	3.2	3.2	6.4	3.0	3.0	6.1
25-29	3.3	4.1	7.4	3.0	3.6	6.6	3.0	3.8	6.8
30-34	3.1	5.0	8.2	3.0	4.2	7.2	3.3	4.5	7.8
35-39	2.9	4.7	7.6	3.0	4.3	7.3	3.3	4.4	7.6
40-44	2.8	4.5	7.3	3.1	4.3	7.4	3.2	4.3	7.4
45-49	2.9	4.3	7.2	3.3	4.3	7.6	3.2	4.2	7.4
50-54	3.8	5.1	8.9	4.1	4.8	8.9	3.8	4.6	8.4
55-59	4.2	4.6	8.8	4.5	4.3	8.8	4.1	4.3	8.4
60-64	3.5	3.4	6.9	3.3	3.6	6.9	3.3	3.5	6.9
65-69	2.8	2.7	5.4	2.7	2.8	5.5	2.6	2.7	5.4
70-74	1.3	1.4	2.7	1.6	1.5	3.1	1.7	1.5	3.2
75-79	1.3	1.3	2.6	1.4	1.6	3.0	1.5	1.6	3.2
80-84	1.0	1.2	2.2	1.2	1.6	2.8	1.2	1.5	2.6
85+	0.8	1.6	2.4	0.9	1.8	2.8	1.0	1.8	2.7
All ages	45.1	54.9	100.0	46.4	53.6	100.0	46.6	53.4	100.0
Median age			43.1			44.6			43.8

<u>Age group</u>	<u>Kwai Tsing</u>			<u>Tsuen Wan</u>			<u>Tuen Mun</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	1.9	1.8	3.7	2.0	1.8	3.8	1.9	1.7	3.6
5-9	2.0	1.8	3.8	2.0	1.8	3.8	1.9	2.0	3.9
10-14	2.0	1.8	3.7	1.8	1.6	3.4	1.8	1.8	3.7
15-19	2.5	2.4	4.9	2.4	2.3	4.6	2.5	2.4	4.9
20-24	3.0	3.0	6.0	3.1	3.2	6.4	3.0	3.2	6.2
25-29	3.2	3.7	6.9	3.4	4.0	7.4	3.1	3.6	6.7
30-34	3.2	4.6	7.9	3.2	4.7	7.9	3.1	4.3	7.4
35-39	3.2	4.6	7.8	2.8	4.6	7.4	3.2	4.5	7.7
40-44	3.3	4.4	7.7	3.5	4.8	8.3	3.4	4.7	8.1
45-49	3.4	4.1	7.4	3.1	4.5	7.7	3.7	4.6	8.3
50-54	3.9	4.6	8.5	4.1	5.0	9.1	4.2	4.6	8.9
55-59	4.1	4.2	8.3	4.5	4.4	8.9	4.3	4.4	8.8
60-64	3.2	3.5	6.7	3.5	3.3	6.7	3.5	3.7	7.3
65-69	2.6	2.8	5.4	2.5	2.5	5.0	2.7	2.6	5.3
70-74	1.8	1.8	3.6	1.5	1.4	2.9	1.5	1.5	3.0
75-79	1.5	1.4	2.9	1.2	1.4	2.5	1.3	1.4	2.7
80-84	1.0	1.4	2.4	1.0	1.3	2.2	0.8	1.1	1.9
85+	0.8	1.6	2.4	0.7	1.4	2.0	0.6	1.2	1.8
All ages	46.8	53.2	100.0	46.1	53.9	100.0	46.6	53.4	100.0
Median age			43.5			43.2			43.7

2 Population structure

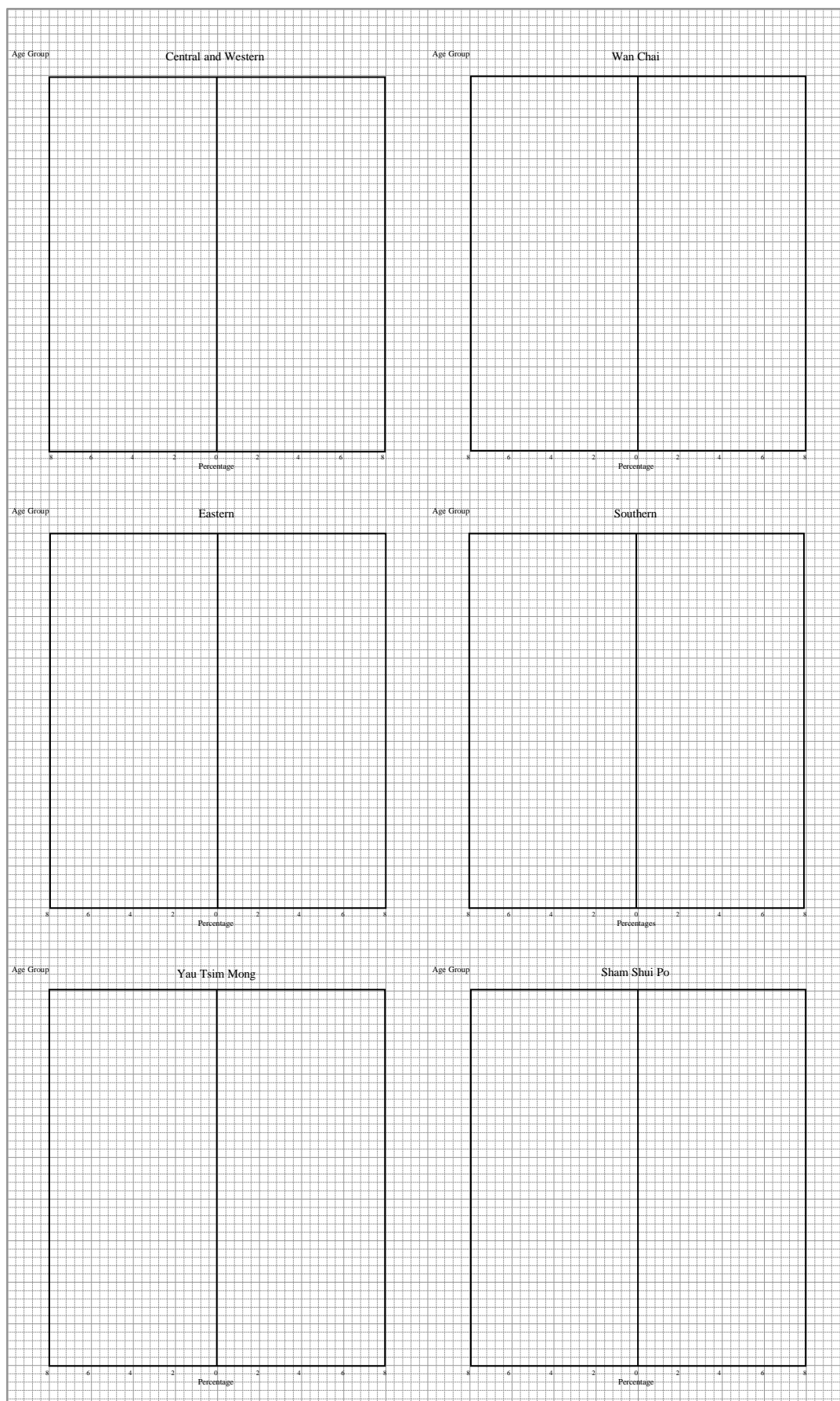
Percentage distribution of population by age and sex, June 2016 (cont'd)

<u>Age group</u>	<u>Yuen Long</u>			<u>North</u>			<u>Tai Po</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	2.1	2.0	4.1	2.2	2.0	4.1	1.8	1.7	3.6
5-9	2.2	2.0	4.3	2.2	2.3	4.5	2.1	2.0	4.1
10-14	1.9	1.8	3.7	2.0	2.1	4.2	1.9	2.0	3.9
15-19	2.6	2.3	4.9	2.5	2.2	4.7	2.4	2.3	4.7
20-24	3.4	3.2	6.5	2.9	2.9	5.8	2.7	2.9	5.7
25-29	3.0	3.9	6.9	3.0	3.6	6.6	3.3	3.6	6.9
30-34	3.3	4.8	8.1	3.2	4.8	8.0	3.1	4.3	7.4
35-39	3.4	4.9	8.2	3.3	4.6	8.0	3.0	4.8	7.8
40-44	3.3	4.6	7.9	3.1	4.5	7.7	3.3	4.9	8.2
45-49	3.2	4.2	7.4	3.3	4.3	7.7	3.5	4.5	8.0
50-54	3.8	4.5	8.3	4.1	4.5	8.6	3.9	4.6	8.5
55-59	4.0	4.0	8.0	4.2	3.9	8.1	4.5	4.7	9.2
60-64	3.3	3.4	6.7	3.3	3.2	6.5	3.4	3.4	6.8
65-69	2.7	2.8	5.4	2.6	2.6	5.2	2.5	2.5	5.0
70-74	1.7	1.4	3.1	1.5	1.4	3.0	1.4	1.5	2.9
75-79	1.4	1.3	2.7	1.3	1.4	2.7	1.5	1.4	2.9
80-84	0.9	1.0	1.9	1.1	1.2	2.3	0.9	1.2	2.1
85+	0.6	1.3	1.9	0.8	1.6	2.4	0.8	1.5	2.3
All ages	46.6	53.4	100.0	46.8	53.2	100.0	46.1	53.9	100.0
Median age	42.1			42.7			43.6		

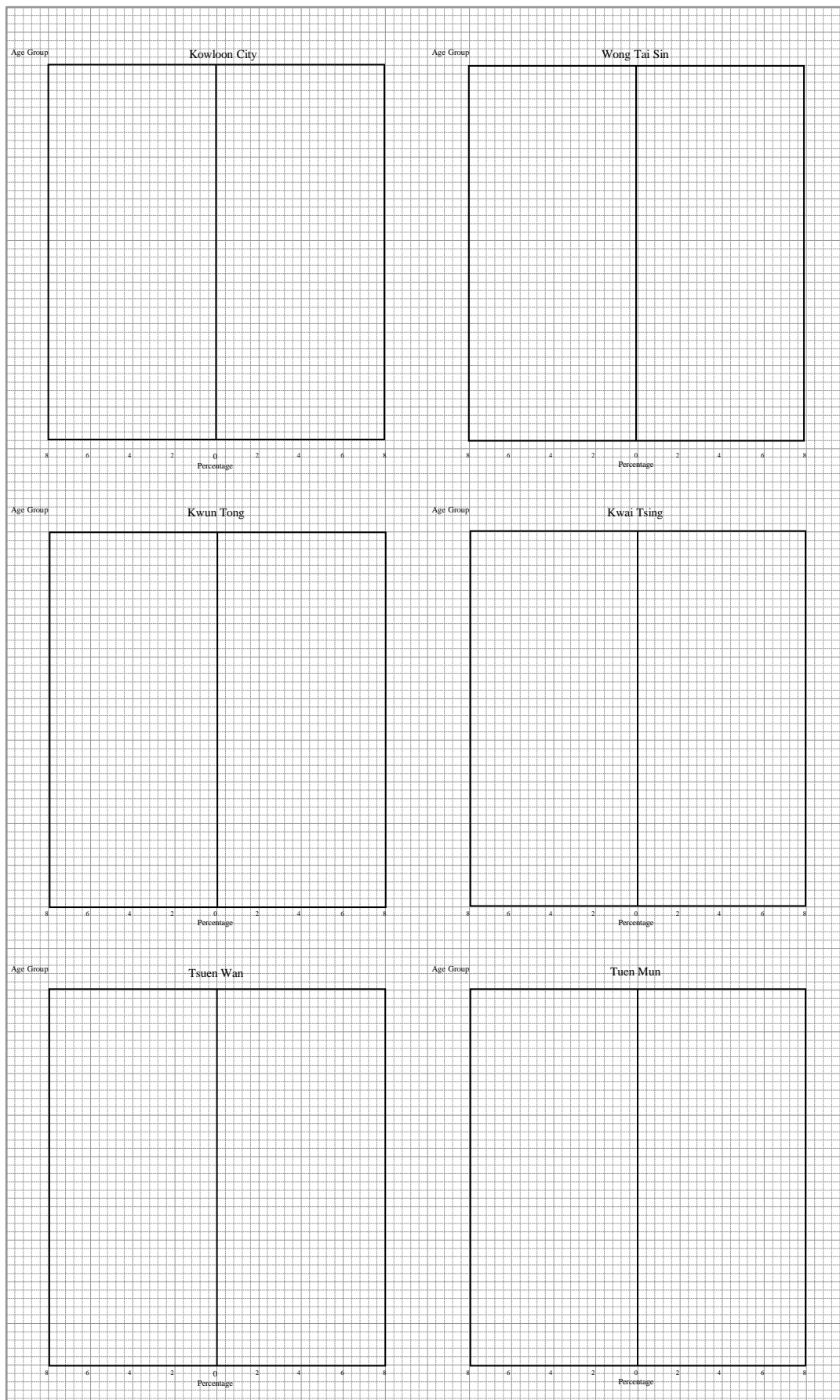
<u>Age group</u>	<u>Sha Tin</u>			<u>Sai Kung</u>			<u>Islands</u>		
	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>	<u>Male</u>	<u>Female</u>	<u>Total</u>
0-4	1.9	1.7	3.6	2.1	2.0	4.1	2.4	2.1	4.4
5-9	2.1	1.9	4.1	2.1	1.9	4.0	2.0	1.9	3.9
10-14	1.9	1.8	3.7	1.7	1.6	3.4	1.6	1.6	3.2
15-19	2.5	2.4	4.9	2.5	2.1	4.6	2.3	2.1	4.5
20-24	3.0	3.1	6.1	3.0	3.1	6.1	2.9	2.8	5.8
25-29	2.9	3.6	6.5	3.1	4.0	7.1	3.4	4.1	7.5
30-34	3.0	4.4	7.3	3.3	5.0	8.4	3.5	5.1	8.6
35-39	2.8	4.5	7.3	3.3	4.8	8.1	3.5	4.9	8.4
40-44	3.1	4.8	7.9	3.2	4.6	7.8	3.3	4.4	7.7
45-49	3.8	5.0	8.7	3.3	4.6	7.8	2.9	4.1	7.1
50-54	4.2	4.8	9.0	3.9	4.8	8.7	3.6	4.4	8.0
55-59	4.0	4.3	8.3	4.1	4.3	8.5	4.2	4.2	8.4
60-64	3.2	3.4	6.6	3.3	3.5	6.8	3.4	3.4	6.8
65-69	2.7	2.7	5.4	2.7	2.9	5.5	2.8	2.7	5.6
70-74	1.4	1.5	2.9	1.5	1.5	3.0	1.7	1.5	3.2
75-79	1.4	1.6	2.9	1.4	1.3	2.6	1.6	1.3	2.8
80-84	1.1	1.3	2.4	0.9	1.0	1.9	0.9	1.3	2.2
85+	0.8	1.5	2.3	0.6	1.0	1.6	0.8	1.0	1.8
All ages	45.7	54.3	100.0	45.9	54.1	100.0	46.9	53.1	100.0
Median age	44.2			42.8			42.4		

Note : Individual percentages may not add up to 100 due to rounding.

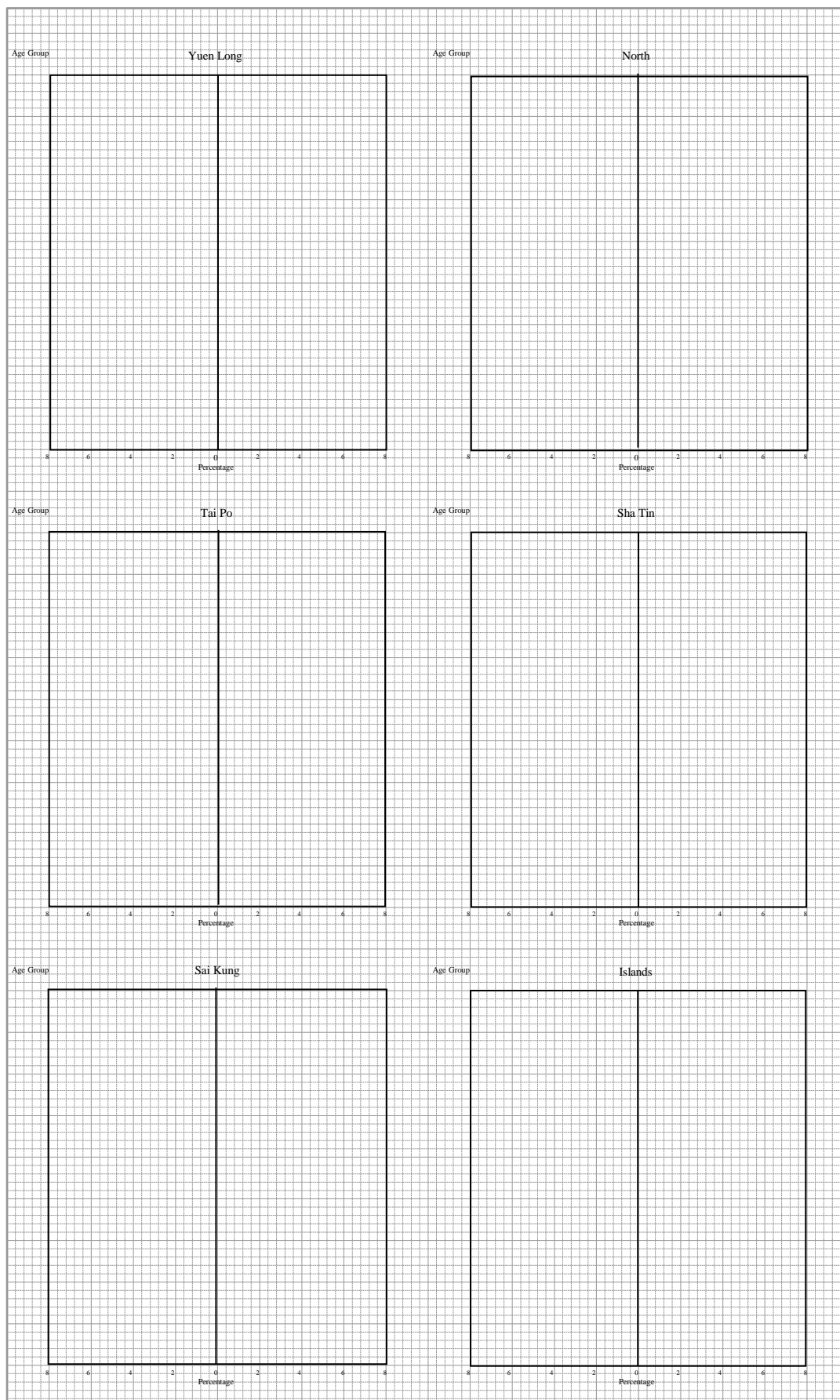
2 Population structure



2 Population structure



2 Population structure



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3 Impact of changes in population and its structure on society



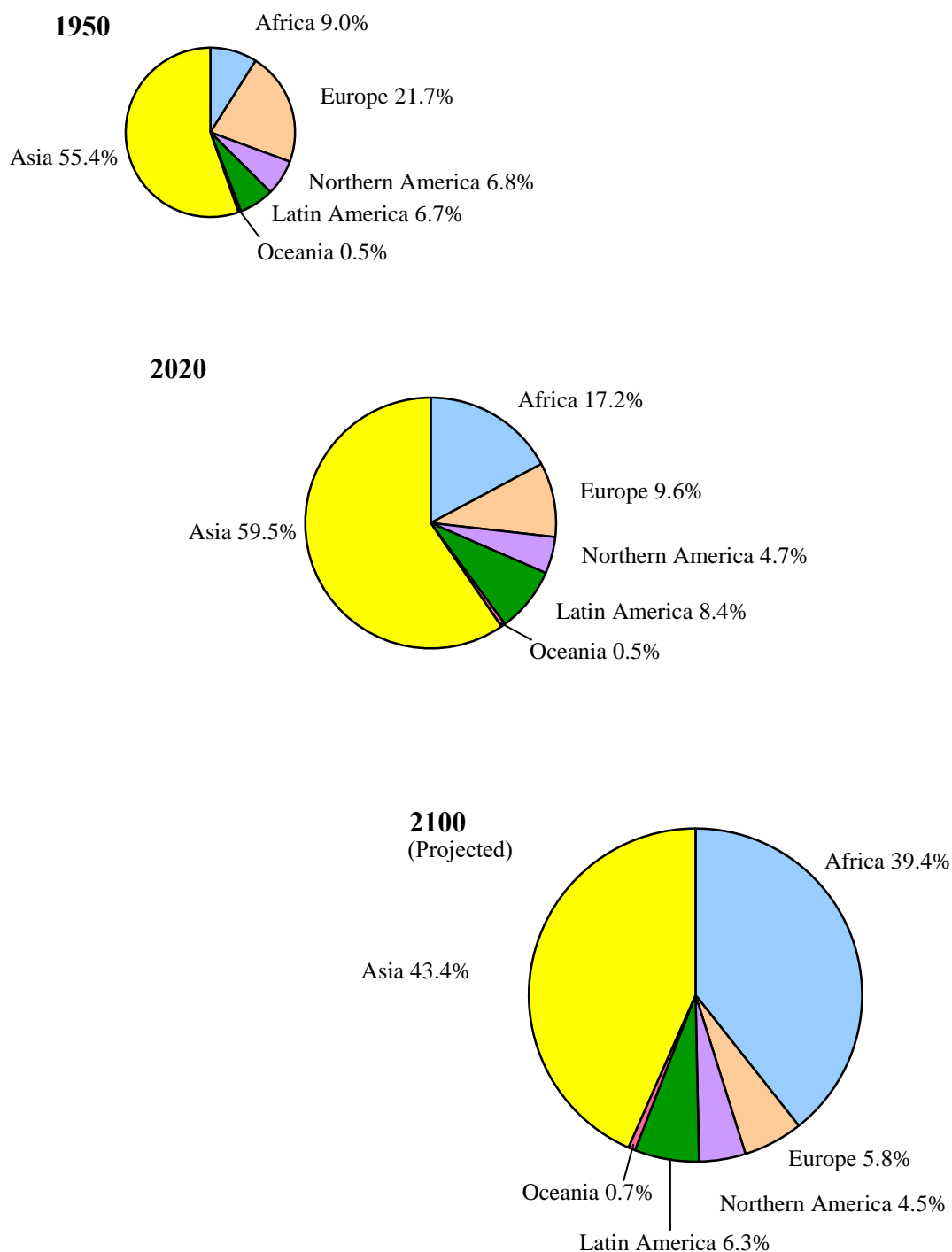
Introduction

This chapter discusses the impact of changes in population and its structure on society. It shows how statistical data can be used to identify the problems caused by population growth. Population control and forward planning of service requirements are the solutions to these problems. To carry out such work, population data of good quality are required.

The current population of the world as at 2021 is estimated to be around 7.9 billion by the United Nations Population Division, being mainly a result of an unprecedented growth of population in the 20th century. This very large population size has caused much concern about the availability of resources to meet the demand of all the people for food, clothing, housing, education, medical services, etc.

The great burden from rapid population growth is likely to persist in the near future. Latest population projections indicate that by 2100, the world population will increase to 10.9 billion. In particular, population problems will be more serious in some poorer areas or countries where populations grow faster than in more developed regions.

Chart 3.1 **Distribution of world population by major area, 1950, 2020 and 2100^{(1), (2)}**



Notes:

- (1) Latin America includes Central America, South America and the Caribbean.
- (2) Areas of the pie charts are proportional to the population sizes in the corresponding years.

Source: *World Population Prospects : The Population Database*, Population Division of the United Nations Department of Economic and Social Affairs

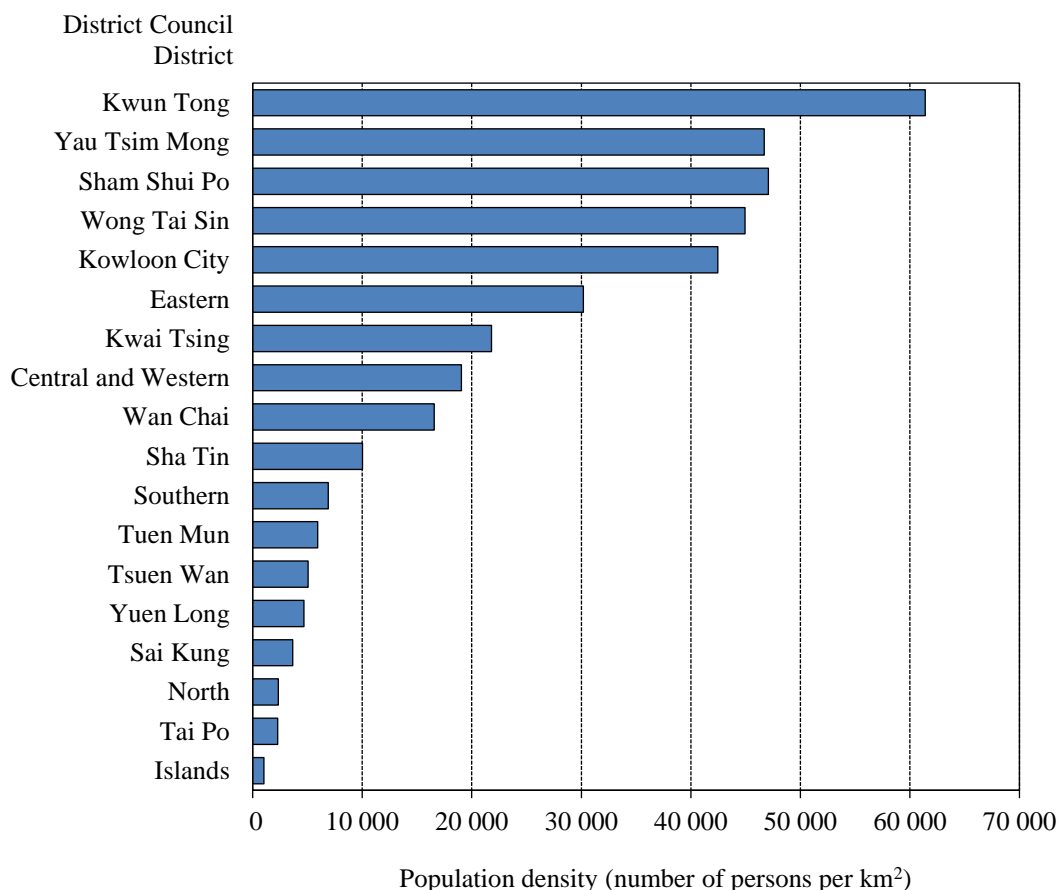
Impact of changes in population and its structure on Hong Kong

In Hong Kong, there are a number of concerns arising from the continuous growth of population and changes in its structure.

Increasing population density

With 7.48 million people (excluding marine population) living in its land area of only 1 110 square kilometres, Hong Kong is one of the most densely populated places in the world. In 2020, the territory as a whole had an average of 6 890 persons per square kilometre, compared to 6 500 persons per square kilometre in 2010. For some areas, the population density was even higher. For instance, Kwun Tong, with 61 410 persons per square kilometre, was the most densely populated district in 2020.

Chart 3.2 Population density by District Council district, 2020



To reduce urban congestion and to meet the new housing needs of the growing population, systematic and coordinated development of new towns began in the early 1970's. Since then, there has been rapid development of new towns in the more remote areas. At present, there are twelve new towns, namely Tuen Mun, Sha Tin, Kwai Chung, Tai Po, Tsuen Wan, Fanling / Sheung Shui, Tsing Yi, Tseung Kwan O, Ma On Shan, Yuen Long, Tin Shui Wai and North Lantau.

The development of new towns has led to a re-distribution of the population, from the older urban areas on Hong Kong Island and in Kowloon to the new towns. According to the results of the 16BC, people living in the new towns accounted for about 47% of the Hong Kong land population in 2016, while the percentage was only 22% in 1976.

Traffic congestion

The large population of Hong Kong generates a huge volume of traffic which, coupled with a lack of space, places a great strain on the internal transport systems.

To obtain an indication of the traffic volume, the number of motor vehicles can be compared with the total length of roads. As at end-2020, there were 373 motor vehicles per kilometre of road, compared with 293 as at end-2010. The increase was mainly contributed by the increase in the number of private cars.

As in places all over the world, people of Hong Kong rely much on public transport services in their daily living.

In 2020, public transport carried 3.3 billion passengers⁽³⁾, as compared with 4.2 billion in 2010. The drop in patronage in 2020 was mainly due to the COVID-19 pandemic and implementation of the related anti-epidemic and social distancing measures.

As in past years, railways continue to be a major type of carrier among the various public transport modes in Hong Kong. They comprise the Mass Transit Railway (MTR) heavy rail systems (which include ten local lines, Intercity Through Train, the Hong Kong Section of the Express Rail Link and the Airport Express Line), the Light Rail and the Hongkong Tramways. In 2020, the daily patronage of railways was 3.6 million passenger journeys, as compared with 4.5 million in 2010. Over the same period, the share of railways in total public transport journeys increased from 38.9% in 2010 to 40.1% in 2020.

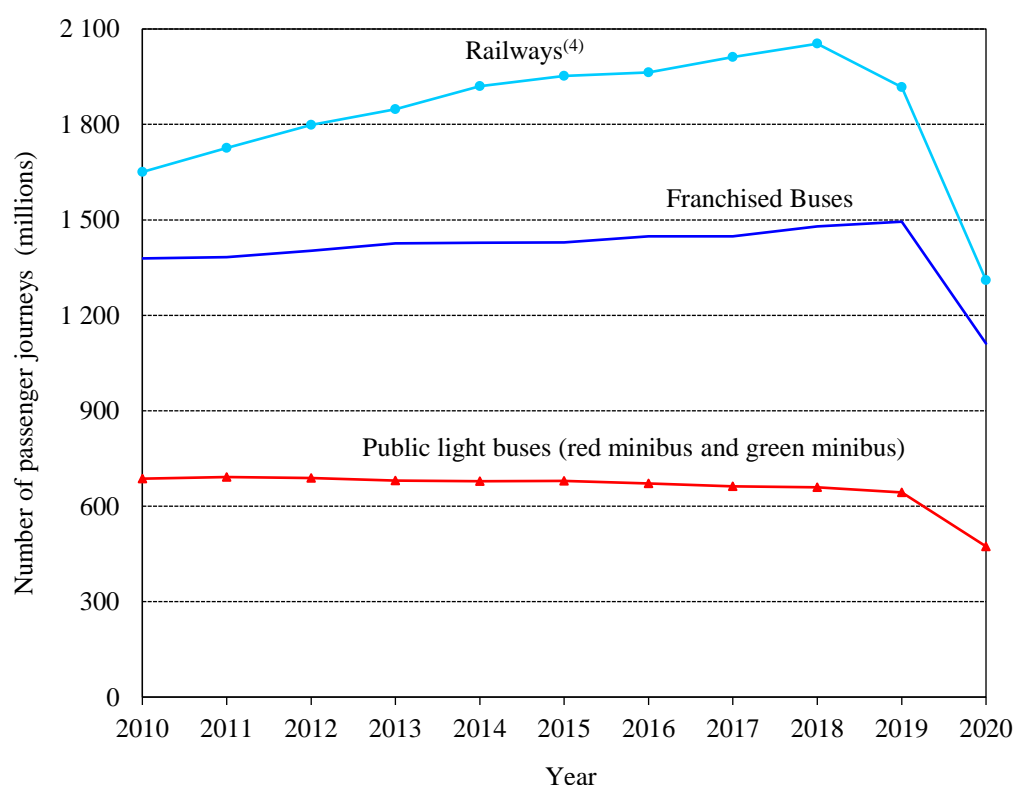
Note :

- (3) The number of passengers cited in transport statistics actually refers to the number of passenger journeys. Since a person may make more than one journey during a period of time, the figure is usually larger than the number of people who have ever made journeys during the period.

Another important component of the public transport system in Hong Kong is franchised buses. In 2020, they carried about 3.0 million passenger journeys or 34.0% of all public transport journeys a day. Ten years ago, the daily patronage was 3.8 million passenger journeys, or 32.5% of the total public transport journeys.

To ensure the smooth and efficient movement of people and goods, careful co-ordination and management of the traffic and transport systems are needed. This involves a programme to improve the road network, expansion of public transport services and measures to achieve more economic use of the limited road capacity.

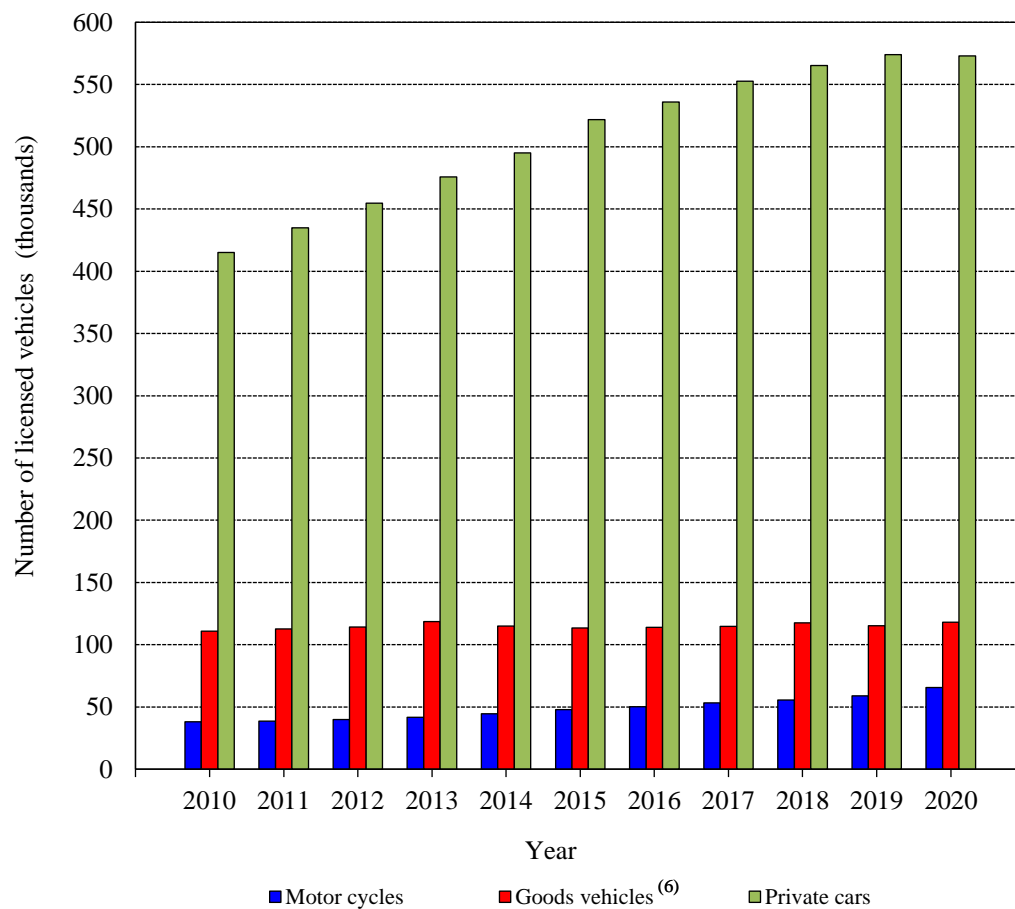
Chart 3.3 Passenger journeys by major mode of public transport, 2010 – 2020



Note :

- (4) Railways comprise the MTR heavy rail systems (which include ten local lines, Intercity Through Train, the Hong Kong Section of the Express Rail Link and the Airport Express Line), the Light Rail and the Hong Kong Tramways.

Chart 3.4 Motor vehicles licensed, 2010 – 2020⁽⁵⁾



Notes :

(5) Figures refer to end of the year.

(6) Goods vehicles include Special Purpose Vehicles.

Increasing demand for housing

As Hong Kong is scarce of land, the Government has to ensure that there is steady and sufficient supply of serviced land for meeting the demand for housing brought about by the continuous growth of the population. To achieve this, the Government needs to develop strategic growth areas (including new and existing land for housing), renew urban areas, redevelop old districts, reclaim more land, perform better town planning and rezone agricultural and industrial land for housing development where appropriate.

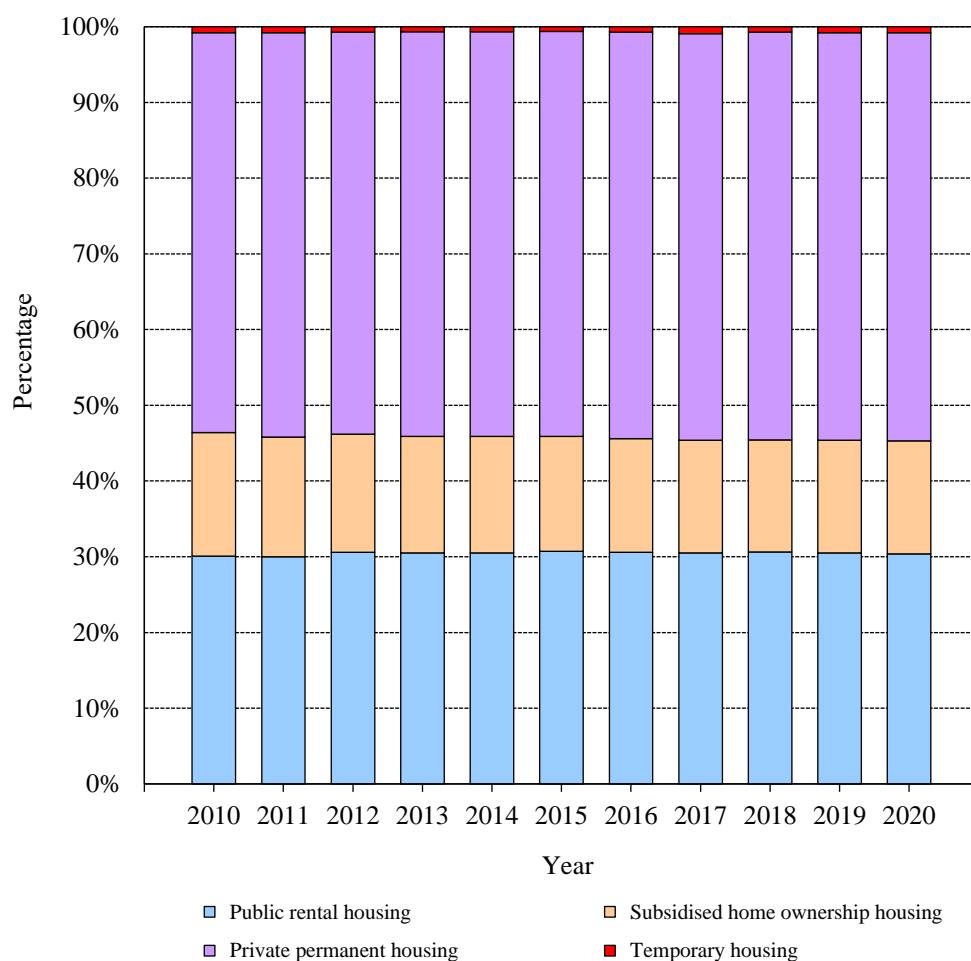
During 2010 to 2020, around 321 000 residential flats were completed to meet the housing needs of people in Hong Kong. As at end of September 2020, the total stock of permanent living quarters in Hong Kong was 2 923 600.

Of the 2.65 million domestic households in 2020, 30.4% resided in public rental housing, 14.9% in subsidised home ownership housing⁽⁷⁾ and 53.9% in private permanent housing⁽⁸⁾. Only less than 1% of domestic households lived in temporary housing.

Notes :

- (7) Subsidised home ownership housing includes flats built under the Home Ownership Scheme, Middle Income Housing Scheme, Private Sector Participation Scheme, Green Form Subsidised Home Ownership Scheme, Buy or Rent Option Scheme and Mortgage Subsidy Scheme, and flats sold under the Tenants Purchase Scheme of the Hong Kong Housing Authority. It also includes flats built under the Flat for Sale Scheme, Sandwich Class Housing Scheme and Subsidised Sale Flats Projects of the Hong Kong Housing Society; and flats in Urban Renewal Authority Subsidised Sale Flats Scheme. Subsidised sale flats that can be traded in open market are excluded.
- (8) Figures include private housing blocks, flats built under the Urban Improvement Scheme of the Hong Kong Housing Society, villas / bungalows / modern village houses, simple stone structures / traditional village houses and quarters in non-residential buildings. Subsidised sale flats that can be traded in open market are also put under this category.

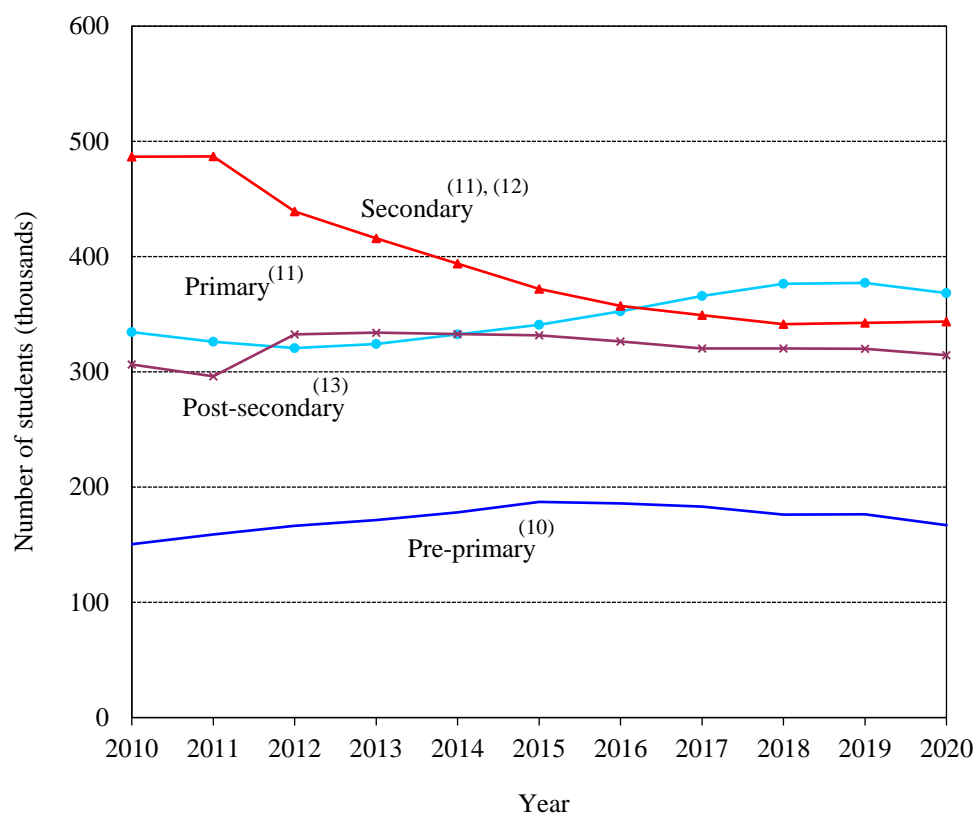
Chart 3.5 **Distribution of domestic households by type of housing, 2010 – 2020**



Increase in post-secondary education opportunities

Owing to the changes in the age structure of the population, the number of students studying in primary education showed a decrease during 2010 to 2012 but has rebounded since 2013. On the other hand, the number of students studying in secondary education has decreased remarkably since 2012 due to the drop in the number of students in the relevant age group. On post-secondary education, through the development of the publicly-funded and self-financing sectors, about 50% of our young people in the relevant age cohort in the 2020/21 academic year have access to degree-level education, and nearly 80% of them now have access to post-secondary education locally, taking into account sub-degree students.

Chart 3.6 Student enrolment⁽⁹⁾ by level of education, 2010 – 2020



Notes :

- (9) Figures include both full-time and part-time students attending long programmes lasting for at least one school / academic year. Figures do not include students attending tutorial, vocational and adult education courses offered by schools below post-secondary education level. Figures for secondary and post-secondary education for 2020 are provisional.
- (10) Figures include nursery, lower and upper classes in kindergartens and kindergarten-cum-child care centres registered under the Education Bureau, and special child care centres registered under the Social Welfare Department.
- (11) Figures include special schools.
- (12) Figures include evening schools, craft level courses and Diploma Yi Jin programme. Prior to the 2012/13 school year, secondary education covers Secondary 1 to Secondary 7. Upon implementation of the New Senior Secondary Academic Structure, there are no subsidised Secondary 7 places under local curriculum starting from the 2012/13 school year.
- (13) Figures include universities and colleges offering post-secondary courses including certificate / diploma, associate degree or equivalent and bachelor degree or above; and also non-local registered or exempted courses leading to non-local higher academic qualifications and operated jointly with non-local institutions.

Increasing elderly dependency ratio

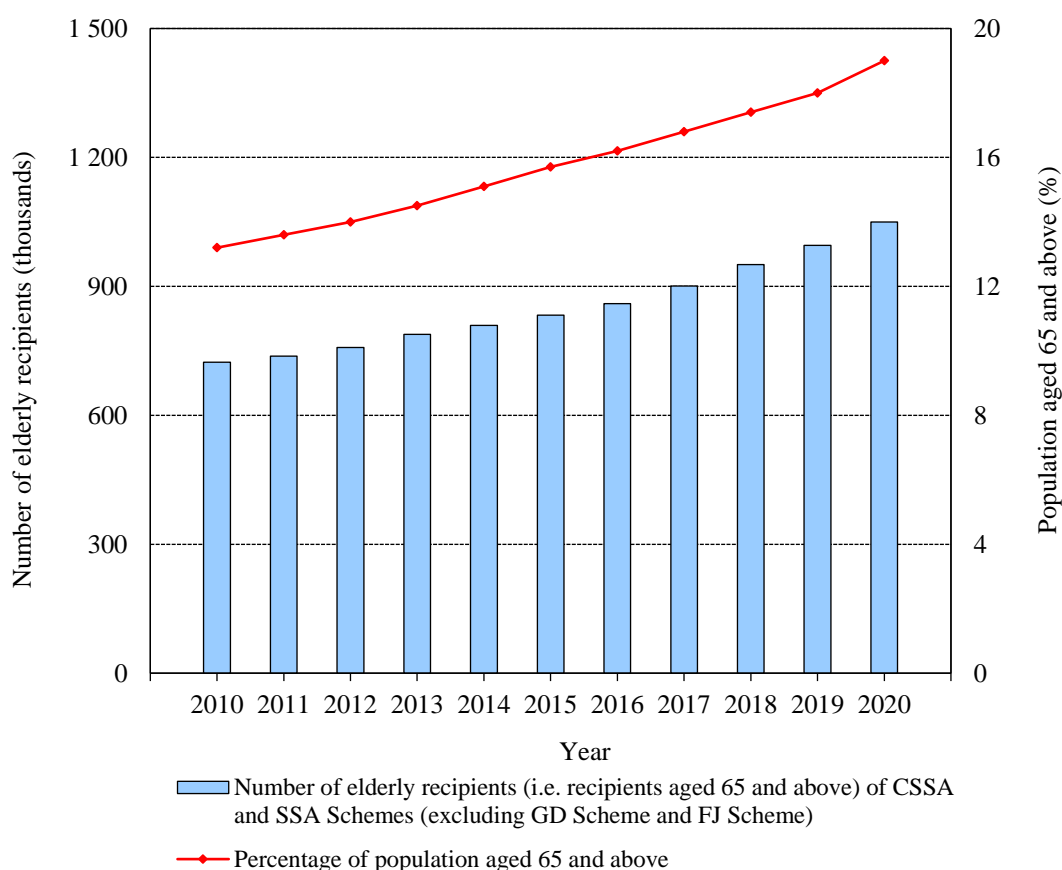
The population of Hong Kong is ageing, as can be seen from the increase in the median age of the population from 41.2 in 2010 to 45.0 in 2020. As a result, the elderly dependency ratio increased from 175 per 1 000 population of working age in 2010 to 262 per 1 000 population of working age in 2020. It is common to consider the elderly as dependent on those aged 15 to 64. The rise in the elderly dependency ratio reflects that there is an increase in the demand for social services, in particular social welfare and medical and health services.

Increasing demand for social welfare services

The percentage of population aged 65 and above has increased gradually, resulting in the increasing demand for social welfare services. The total number of elderly recipients (i.e. recipients aged 65 and above) of the Comprehensive Social Security Assistance (CSSA) and Social Security Allowance (SSA) Schemes (excluding Guangdong Scheme and Fujian Scheme) increased from 723 700 in end-2010 to 1 049 600 in end-2020. While the CSSA Scheme is designed to provide members of the community who cannot support themselves financially with monetary assistance to meet their basic and special needs, the SSA Scheme is to provide a monthly allowance to members of the community to meet their special needs arising from old age or disability.

The Government also provides a wide range of elderly and community services. Community services include the operation of social centres for the elderly, district elderly community centres, neighbourhood elderly centres, day care centres / units for the elderly, enhanced home and community care services, and integrated home care services, etc. which aim to enable the elderly to continue to stay in the community.

Chart 3.7 **Number of elderly recipients of the Comprehensive Social Security Assistance (CSSA) and Social Security Allowance (SSA) Schemes (excluding Guangdong (GD) Scheme and Fujian (FJ) Scheme) and percentage of population aged 65 and above, 2010 – 2020⁽¹⁴⁾**



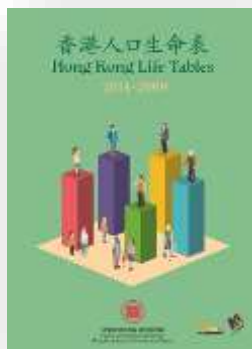
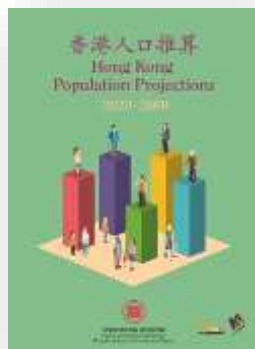
Population projections

For the purpose of forward planning of service needs, the size, structure and distribution of the population in future years have to be projected. A reliable projection requires careful examination of past trends of fertility, mortality and population movement to determine their possible changes in the future. The assumed changes are then added onto the base population, which is derived from a population census or by-census, year after year to obtain the projection results.

Note :

(14) Figures refer to December of the year.

C&SD is responsible for compiling projections of the population of Hong Kong. The main use of the population projections is to provide a common basis for government programme planning in such areas as education, housing, transport, social services and health services. The projection results are also widely applied in academic research and business development and planning in the private sector. The latest set of population projections was released in September 2020, with a 50-year projection period from mid-2020 to mid-2069.



A set of population projections compiled based on the mid-2019 population estimate and a corresponding set of domestic household projections were released in September 2020.

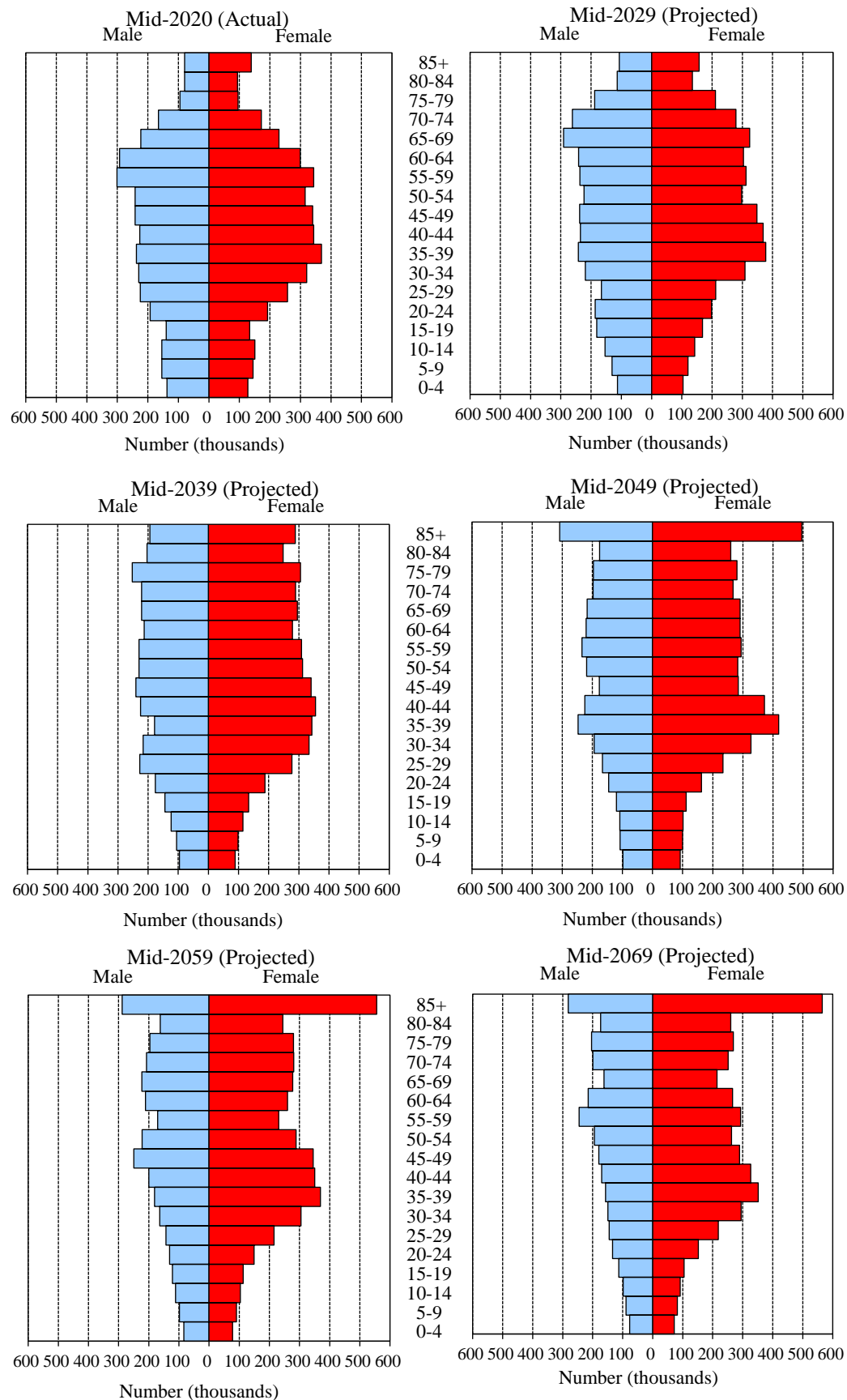
“Component method” for population projections

The “component method”, which is commonly used internationally, is adopted for compiling the population projections. Under this method, the size and age-sex structure of the projected population in each of the projection years are obtained by applying different assumptions made on the fertility, mortality and population movement conditions for the projection year to the population situation in the preceding year. Therefore, in compiling the population projections, the population situation in a base year will be used as the starting point. It is then brought forward under separate projections of fertility, mortality and population movement, year after year until the end of the projection period. While fertility, mortality and population movement assumptions are formulated mainly on the basis of the past trends and recent developments pertaining to the socio-economic conditions in Hong Kong, government policies, if involved, are taken as that the existing policies would continue to apply except for known policy changes.

Major projection results

In the 2019-based projections, the Hong Kong population is projected to increase at an average annual rate of 0.4%, from 7.51 million in mid-2019 to the peak of 8.11 million in mid-2041, and then decline to 7.35 million in mid-2069 (at an average annual rate of decrease of 0.3%). The average annual growth rate over the 10-year period from 2019 to 2029 is projected to be 0.5%. Yet, with significant increase in the number of deaths upon ageing of the population, the average annual rate of decline over the last 10 years of the projection period (i.e. from 2059 to 2069) is projected to be 0.5%.

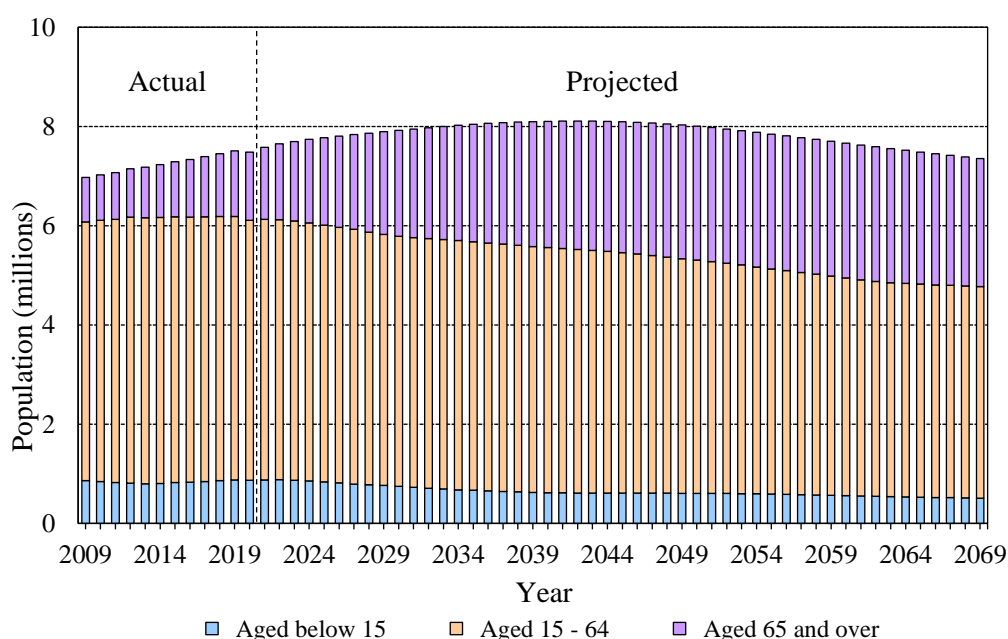
Chart 3.8 Hong Kong population pyramid at selected years



Population on an ageing trend

Population ageing is expected to continue. With post-war baby boomers entering old age, the number of elderly persons aged 65 and over is projected to nearly double in the coming 20 years. Excluding foreign domestic helpers, the number of elderly persons will increase from 1.32 million (18.4% of the total population) in 2019 by 1.20 million to 2.52 million (33.3%) in 2039. Compared with the growth of about 0.61 million in the last 20 years (from 1999 to 2019), the elderly population will increase distinctly at a much faster pace in the future. It is also worth noting that the elderly population will remain at over 2.5 million for at least 30 years. In 2069, the number of elderly persons is projected to reach 2.58 million (38.4%). Meanwhile, due to the persistently low fertility rate, the proportion of the population aged under 15 is projected to decrease gradually from 12.2% in 2019 to 7.6% in 2069.

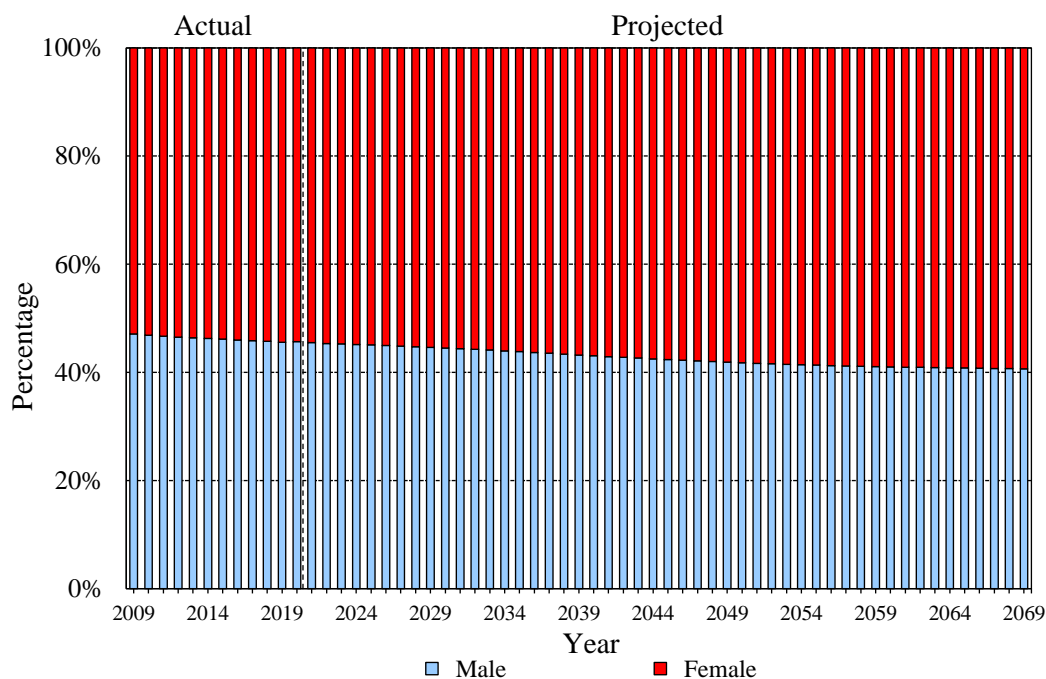
Chart 3.9 Hong Kong population by age group, 2009 – 2069



Decreasing sex ratio

Another noteworthy point is that the proportion of males in the population would keep on decreasing. In 2019, the sex ratio (i.e. the number of males per 1 000 females) of the population was 838. Owing to the continued entry of One-way Permit holders (many being Hong Kong men's wives in the Mainland) and foreign domestic helpers (mostly being younger females) into Hong Kong in the coming years and the fact that females in general live longer than males, the sex ratio is projected to fall noticeably to 685 in 2069. Even with the effects of foreign domestic helpers excluded, the sex ratio would still come down from the level of 910 in 2019 to 801 in 2069.

Chart 3.10 **Proportion of male and female populations, 2009 – 2069**
(including foreign domestic helpers)



Labour force projections

The size and the composition of the labour force within the population are important determinants of economic development. Labour force projections of Hong Kong compiled by C&SD provide information on the future labour supply in Hong Kong and its age and sex distribution. Such information serves as useful reference for policy planning and formulation. The latest set of labour force projections was released in September 2020, covering the projection period from 2020 to 2069.

Methodology

In compiling the labour force projections for the period from 2020 to 2069, reference has been made to the results of the 2019-based population projections and the latest trends of the age-sex specific labour force participation rates. Foreign domestic helpers are not included in the projected labour force participation rates and labour force figures.

The labour force, synonymous with the economically active population, comprises the employed population and the unemployed population. The labour force participation rate refers to the proportion of the labour force in the population aged 15 and over. It is a measure of the propensity of the persons of working age to be in the labour force. In particular, the proportion of persons participating in the labour force in a particular age-sex group is termed as the age-sex specific labour force participation rate for the group.

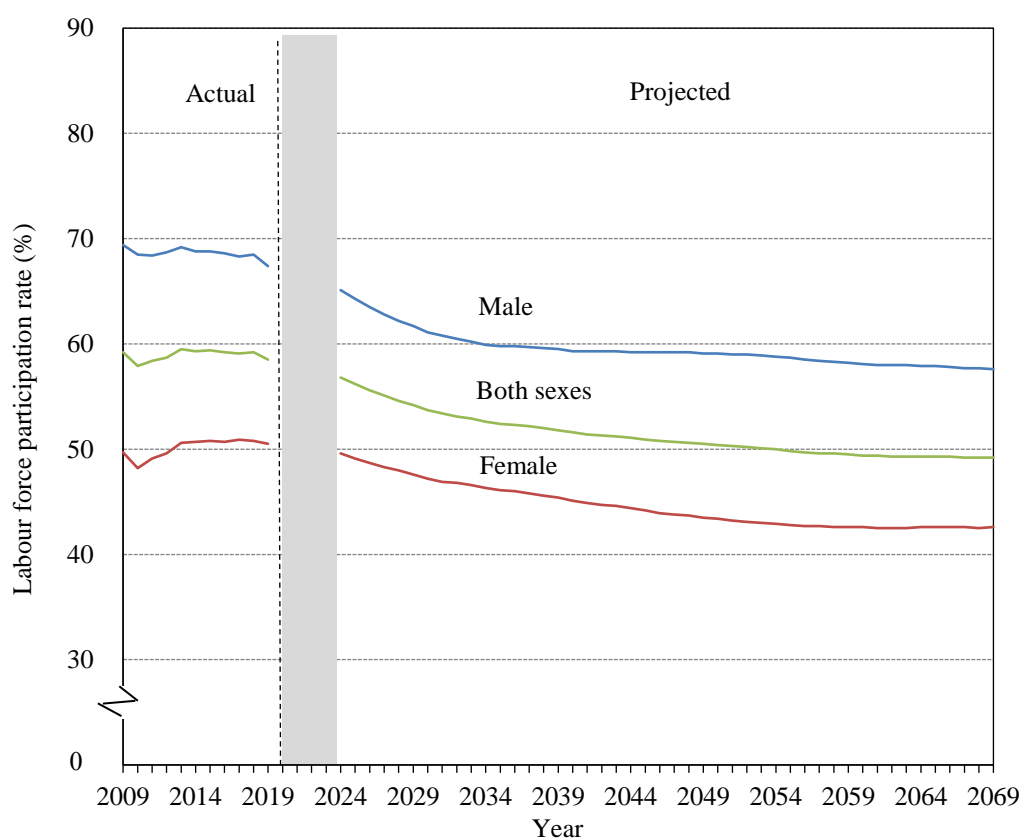
In compiling the projected labour force, a set of projected labour force participation rates for individual projection groups in the population for different years within the projection period is first compiled with reference to the latest trends of the age-sex specific labour force participation rates. The projected labour force participation rate for each projection group is then multiplied to the projected population size of the corresponding group to derive the projected labour force of the group in each of the years over the projection period. Finally, the projected labour force of all groups in the same year are summed up to give the projected total labour force for the year concerned.

Major projection results

Projected labour force participation rates (excluding foreign domestic helpers)

The overall labour force participation rate is projected to decline steadily from 58.5% in 2019 to 49.2% in 2069. Owing to the population ageing effect, the overall labour force participation rate for both males and females are projected to decrease from 67.4% and 50.5% in 2019 to 57.6% and 42.6% in 2069 respectively.

Chart 3.11 Labour force participation rate (excluding foreign domestic helpers) by sex, 2009 – 2069⁽¹⁵⁾



Note :

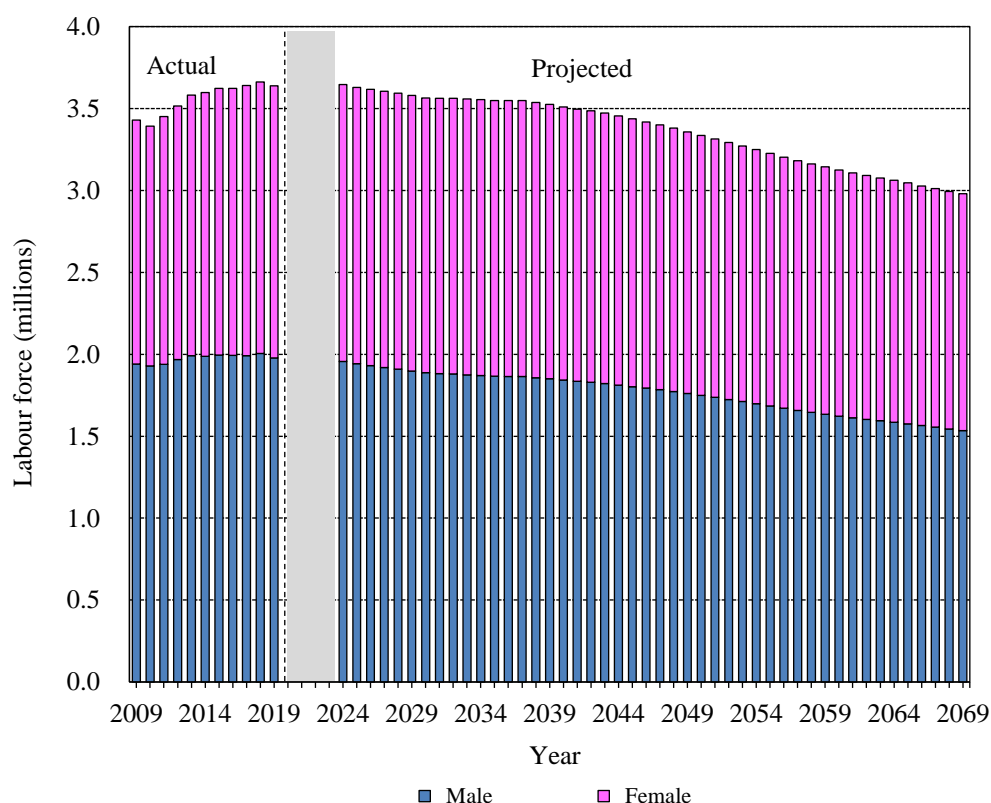
- (15) Owing to the impact of the COVID-19 pandemic, the projection results, which are derived based on long-term underlying trends of the population structure and its propensity to be in the labour force, for the years from 2020 to 2023 are not shown.

Projected labour force (excluding foreign domestic helpers)

The total labour force is projected to decrease from 3.64 million in 2019 to 3.56 million in 2031. It will then hover between 3.55 million and 3.56 million until 2037, before decreasing to 2.98 million in 2069.

The labour force for males is projected to decrease gradually from 1.98 million in 2019 to 1.54 million in 2069. The labour force for females is projected to vary narrowly between 1.66 million and 1.69 million in 2019 to 2042 and then decrease gradually to 1.44 million in 2069.

Chart 3.12 Labour force (excluding foreign domestic helpers), 2009 – 2069⁽¹⁶⁾



Note :

- (16) Owing to the impact of the COVID-19 pandemic, the projection results, which are derived based on long-term underlying trends of the population structure and its propensity to be in the labour force, for the years from 2020 to 2023 are not shown.

Further information

The above contents present only part of the information produced by C&SD on the topics concerned. For further information regarding the topics discussed in this chapter (e.g. latest statistics, statistical reports, concepts and methods), please visit the following sections of the C&SD website :

[Population estimates](#)

[Population censuses and by-censuses](#)

[Population and household projections](#)

[Demographics](#)

[Labour force, employment and unemployment](#)

[Transport](#)

[Information and communications](#)

[Tourism](#)

[Housing and property](#)

[Education](#)

[Social welfare](#)

[Health](#)

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

Exercise

Identifying impact of changes in population and its structure on society

To arouse the public's awareness of various population and social problems, readers may try to identify such problems in the districts they live, in the whole territory of Hong Kong, or in other countries.

For example, readers may consider the problem of traffic congestion in Hong Kong by looking up statistics compiled by C&SD or other government departments (e.g. Transport Department) in order to quantify the magnitude of traffic congestion in broad terms, and to consider how the various problems can be solved. Examples of relevant statistics include number of motor vehicles licensed, length of roads and number of passengers using different kinds of public transport.

4 Other official statistics



Introduction

Official statistics are generally statistics compiled by the Government based on raw data from such sources as administrative records, special returns and surveys. Where surveys are conducted, there are often statistical legislations requiring the target persons or companies to supply the required raw data.

C&SD is the central statistical office of Hong Kong. C&SD together with statistical units established in various government bureaux and departments forms the Government Statistical Service. Broadly speaking, most general-purpose statistics come under the responsibility of C&SD. The statistical units in various government bureaux and departments are responsible for specific-purpose statistics (for dedicated use in their respective work areas) and provide necessary support in the application of statistics.

In this knowledge-based era, more and more people are making use of statistics in their work and daily lives. Official statistics play an important role in a wide range of endeavours, including macro-economic analysis, day-to-day administration and long term planning of the Government, decision-making of individuals and business firms, and enhancing people's understanding of the society and their participation in discussions about social and economic policies.

Some of the more common economic and social statistics are introduced in the following sections.

(A) Economic statistics

Economic statistics comprise, among others, the following areas : trade statistics, national income statistics, balance of payments statistics, labour statistics, price statistics and operating statistics of businesses.

Just as doctors need to use medical equipment when they make diagnoses, economic analysts need to make reference to statistics in forming their views from theoretical considerations. Economic statistics serve as measuring instruments which enable the analysts to judge whether different economic sectors in the economy are in harmony, whether the economy is stagnant or overheated, and whether economic performance will improve or decline. Although different analysts may have different views on economic prospects or on the role of the Government, there is no doubt about the importance of good measuring instruments to them.

4 Other official statistics

Apart from facilitating macro-economic analysis, economic statistics are also very useful in business planning. Businessmen can make use of the statistics in deciding what businesses to invest in, what products to produce, where to locate shops, at what wages they should employ workers, and so on.

Trade statistics

Hong Kong is an externally oriented economy. Its economic performance is highly related to the performance of the external sector. Hong Kong external trade comprises trade in goods (i.e. merchandise trade) and trade in services.

Trade in goods covers movements of merchandise between Hong Kong and her trading partners, by land, air, water and by post. It comprises imports and total exports.

Trade in services includes exports and imports of services. Exports of services are the sales of services to the rest of the world, whereas imports of services are the purchases of services from the rest of the world.

(1) Merchandise trade

Merchandise trade statistics provide important indicators of the performance of the external sector of the economy in respect of merchandise trade. They can be analysed by the two components of external merchandise trade, namely total exports and imports. In addition to aggregate statistics of trade in respect of each of the components, detailed statistics are also available on Hong Kong's trade with different countries / territories and for different commodities.

Besides providing very useful information on the performance of an economy, trade statistics can also be used by business firms in decision-making on such areas as forecasting business prospects, measuring market shares, planning investment and formulating marketing, production and development strategies.

As a free port, Hong Kong has minimal import and export licensing requirements. Most products do not need licences to enter or leave Hong Kong. Unlike many other economies, there is no import tariff in Hong Kong. Yet, persons who import or export goods (except for exempted goods) are required to submit import / export declarations to the Customs and Excise Department within 14 days after the importation / exportation of goods. The import / export declarations are subsequently forwarded to C&SD for further processing and compilation of Hong Kong's external merchandise trade statistics. The import / export declaration is a typical example of special returns for collecting raw data essentially used for trade statistics compilation.

4 Other official statistics

Electronic submission of trade declarations has been made mandatory as from April 2000. In 2020, around 18.7 million import / export declarations were processed by C&SD.



In 2020, some 18.7 million import/export declarations and 6.1 million cargo manifests were processed by C&SD.

The Hong Kong Special Administrative Region is a separate customs territory, as stated in “The Basic Law of the Hong Kong Special Administrative Region of the People’s Republic of China”. Import / export declaration is also required of Hong Kong’s trade with the Mainland, and statistics relating to this are included in Hong Kong’s external merchandise trade statistics.

In 2020, the value of Hong Kong’s total merchandise trade was \$8,197.3 billion, lower than that in 2019 by 2.5%. Of this, \$3,927.5 billion were attributable to total exports and \$4,269.8 billion to imports.

Between 2010 and 2020, the values of total exports and imports of goods increased respectively at an average annual growth rate of 2.6% and 2.4%.

Total exports of goods comprise domestic exports and re-exports. Domestic exports are the natural produce of Hong Kong or the products of a manufacturing process in Hong Kong which has changed permanently and substantially the shape, nature, form or utility of the basic materials used in manufacture. Re-exports are products which have previously been imported into Hong Kong and which are re-exported without having undergone in Hong Kong a manufacturing process which has changed permanently and substantially the shape, nature, form or utility of the basic materials used in the manufacture. The values of exports are recorded on f.o.b. (free on board) basis, i.e. on the basis of the value of the commodities when they leave the customs boundary of Hong Kong.

4 Other official statistics

Imports of goods are goods which have been produced or manufactured in places outside the jurisdiction of Hong Kong and brought into Hong Kong for local use or for subsequent re-export as well as Hong Kong products re-imported. Their values are recorded on c.i.f. (cost, insurance and freight) basis, i.e. on the basis of the value of the imported commodities when they enter into Hong Kong. C.i.f. value of an imported commodity is usually higher than its f.o.b. value, as the former includes also the insurance and transportation fees for delivering the commodity from the exporting territory to the importing territory.



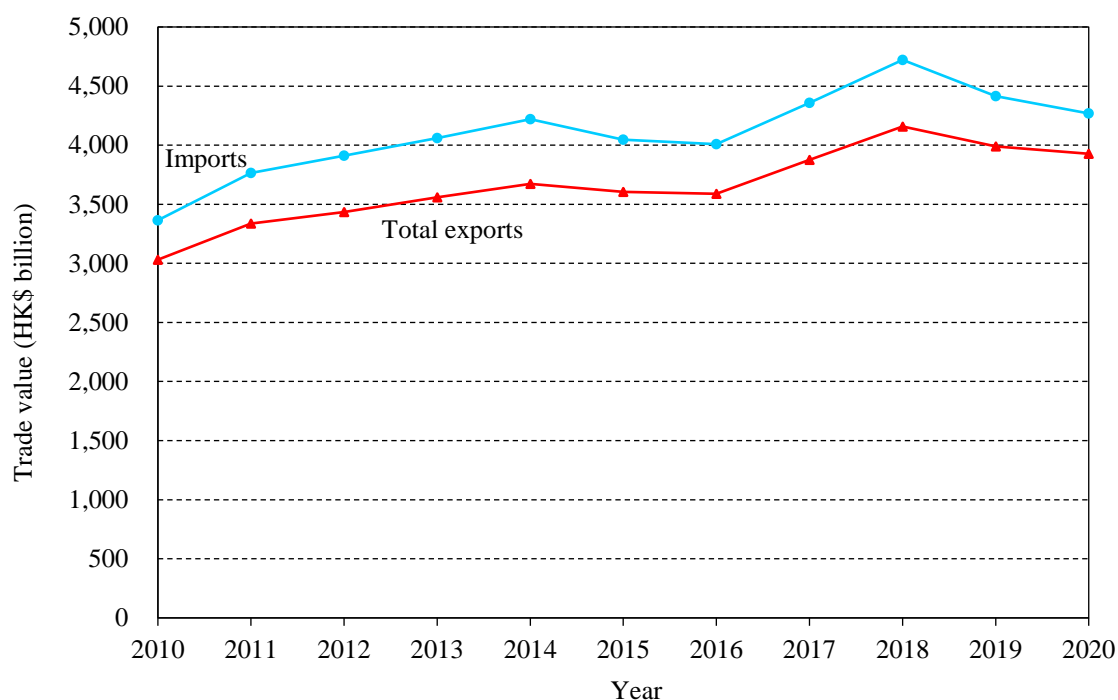
The Mainland and the United States of America were the two largest destinations of Hong Kong's total exports in 2020. They accounted for 59.2% and 6.6% respectively of the total export value.

The major commodities in Hong Kong's total exports include electrical machinery, apparatus and appliances, and electrical parts thereof; telecommunications and sound recording and reproducing apparatus and equipment; office machines and automatic data processing machines; non-metallic mineral manufactures; and professional, scientific and controlling instruments and apparatus.

Most of Hong Kong's imports of goods come from the Mainland, Taiwan, Singapore, Korea and Japan. In 2020, the Mainland accounted for 45.1% of the total import value, compared to 45.5% in 2010.

4 Other official statistics

Chart 4.1 Values of total exports and imports of goods, 2010 – 2020



(2) Trade in services

With the structural change in the Hong Kong economy, the importance of service industries has been on the rise. Being an externally oriented economy, Hong Kong is an important centre not only for trade in goods, but also for trade in services (TIS). TIS in Hong Kong has been maintaining observable growth in recent years.

Hong Kong's TIS statistics can be traced back to the reference year of 1980. Owing to data limitation, the classification of services at that time was only based on major industries in which the Hong Kong businesses were engaged. In response to the growing demand for detailed statistics on TIS, Hong Kong has started releasing detailed TIS statistics by type of services and country / territory on an annual basis since 2002, with the series dated back to the reference year of 1995.

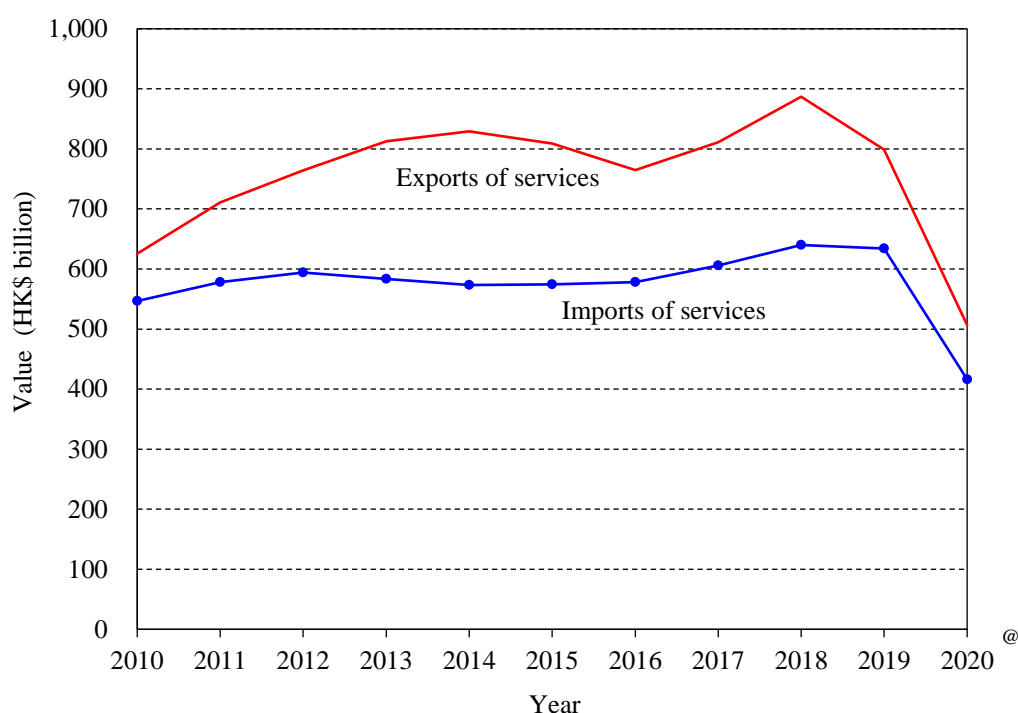
During the period from 2010 to 2019, the value of total exports of services rose significantly, from \$625.7 billion in 2010 to \$798.9 billion in 2019, at an average annual growth of 2.8%. Total value of imports of services also increased, from \$546.9 billion in 2010 to \$634.2 billion in 2019, at an average annual growth of 1.7%. However, both the values of total exports and imports of services recorded declines in 2020 due to the impact of the COVID-19 pandemic. In 2020, the two largest service components in exports of services were transport and financial services (at \$177.7 billion[@] and \$168.1 billion[@] respectively), which also brought about a sizable surplus in the overall TIS after netting out the total imports of services.

4 Other official statistics

Analysing exports of services of Hong Kong by geographical breakdown⁽¹⁾ in 2019, the Mainland (37.7%) and the United States of America (14.9%) were the major destinations, followed by the United Kingdom (8.9%), Japan (4.4%) and Singapore (4.2%).

For imports of services⁽¹⁾ of Hong Kong, the Mainland (37.8%) and the United States of America (11.0%) were also the major sources, followed by Japan (8.2%), the United Kingdom (6.3%) and Singapore (4.4%).

Chart 4.2 Values of exports and imports of services of Hong Kong, 2010 – 2020



Note :

- (1) Financial intermediation services indirectly measured (FISIM) have no geographical breakdowns. Hence, trade in services figures analysed by country / territory do not include figures in respect of FISIM.

National income statistics

Gross Domestic Product (GDP) and Gross National Income (GNI) are core statistics in National Accounts. They are both important economic indicators and are useful for analysing the overall economic situation of an economy, with the former particularly useful for reflecting the level of production, and the latter for aggregate income of residents.

GDP is a measure of the total value of production of all resident producing units of an economy in a specified period (typically a year or a quarter), before deducting the consumption of fixed capital. By providing statistics on the production of various sectors of the economy, GDP is more relevant for analyses related to production activities in the economy, such as employment, productivity, industrial output, investment in equipment and structure.

GDP of Hong Kong is compiled using both the “production approach” and the “expenditure approach”. Under the production approach, GDP is an aggregate measure of the total value of net output of all resident producing units. Net output is measured by value added, which is defined as the value of gross output *less* the value of intermediate consumption (that is the value of goods and services used up in the course of production). Each producing unit works to “add value”. Summation of the value added of all resident producing units gives an aggregate measure of the total output of the economy which is free from double counting.

It is essential to apply the concept of value added in GDP compilation in order to avoid double counting the value of production. Since various producing units are indeed closely linked in the course of production, the goods or services produced by a producing unit may be used as the intermediate consumption of another producing unit. If the gross outputs of individual producing units are added up directly, the values of certain goods and services will be counted more than once and the GDP so derived will exaggerate the true value of production.

From another angle, goods and services produced will eventually be consumed by final users which will be captured in the total expenditure on final demand for goods and services. Thus, the expenditure approach can also be applied for the compilation of GDP.

Under the expenditure approach, GDP is compiled as the total final expenditures on goods and services (including private consumption expenditure⁽²⁾, government consumption expenditure, gross domestic fixed capital formation, changes in inventories and exports of goods and services), less imports of goods and services.

The production and expenditure approaches represent how components within GDP can be viewed from two different perspectives. In theory, there is only one GDP figure. However, since the data sources and estimation methods adopted in the compilation of GDP in different approaches are not the same, some statistical discrepancies may exist between the GDP estimates compiled under the two different approaches.

Conceptually, changes over time in GDP at current prices can be factored into two components, reflecting (1) changes in the prices of goods and services produced or purchased, and (2) changes in their volumes. In order to measure the volume growth of GDP and its components, the effect of price changes has to be eliminated. The year-on-year change in the volume measure of GDP gives a measure of the “real” growth of an economy.

To compile the volume measures of GDP and its components, the annually re-weighted chain linking approach is adopted. For a particular year, the volume estimates of major components of GDP revalued at preceding year prices are first derived by “deflating” the current price values of sub-components by the relevant price indices (or in some cases by revaluing the current period quantities at preceding year prices) at the most disaggregated levels. The volume estimate of GDP is then obtained by aggregating the volume estimates of GDP major components revalued at preceding year prices. With the effect of price changes eliminated, the volume estimate reflects the real growth of GDP. The preceding-year weighted volume measures of GDP and its components are chain linked to a selected reference year in order to obtain a continuous time series of the chain volume measures of GDP and its components.

Note :

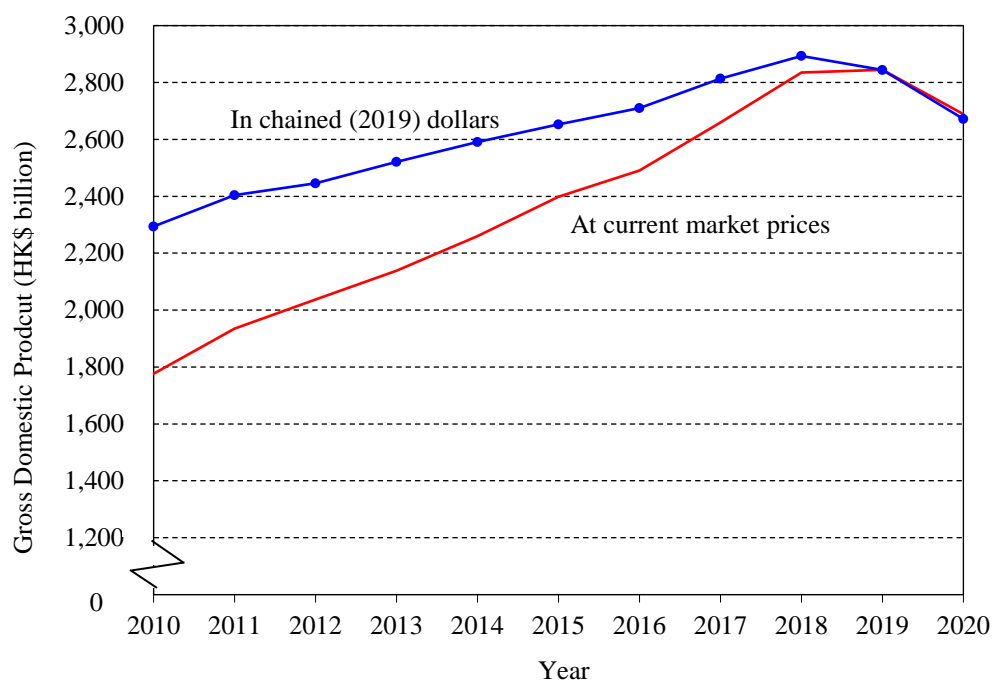
- (2) Private consumption expenditure (PCE) refers to the total value of final consumption expenditure on goods and services by households and private non-profit institutions serving households. It is a comprehensive measure of household overall spending on consumption goods (purchased from various channels including the conventional retail outlets) and services purchased locally or outside Hong Kong.

PCE is distinguished from retail sales statistics in that:

- (i) retail sales statistics, primarily intended to measure the sales receipts of goods sold by local retail establishments for gauging the short-term business performance of the local retail sector, refer to consumer spending on goods purchased from local retail establishments but do not cover those consumer spending on electricity, gas and water and on various services (such as housing, transportation, education, medical and health care, recreation, entertainment);
- (ii) visitors' spending in Hong Kong is included in the retail sales figure but not in PCE; and
- (iii) Hong Kong residents' consumption expenditure abroad is covered in PCE but such spending outside Hong Kong is outside the coverage of retail sales statistics.

4 Other official statistics

Chart 4.3 Gross Domestic Product of Hong Kong, 2010 – 2020



Hong Kong's GDP for 2020 at current market prices amounted to \$2,688.5 billion, about 1.5 times of the corresponding figure of \$1,776.3 billion for 2010. GDP for 2020 in chained (2019) dollars was \$2,671.6 billion, or 1.2 times of the corresponding figure of \$2,294.1 billion for 2010. This represented an average annual growth rate of 1.5% in real terms between 2010 and 2020.

Apart from being a measure of the overall economic performance of an economy, GDP is often used in international comparisons of state of economic well-being. In the light of the variations in the scale of different economies, "per capita GDP" is a more relevant indicator for comparing the economic well-being in different places. Per capita GDP of an economy is obtained by dividing the total GDP in a year by the population of that economy in the same year.

At current market prices, per capita GDP for Hong Kong increased from \$252,887 in 2010 to \$359,343 in 2020. This represented an average annual growth rate of 3.6%. To eliminate the effect of price changes over the ten-year period, the average annual growth rate of per capita GDP in real terms during the period can be referred to, which was 0.9%.

GNI is another useful measure of economic performance. It measures the total income earned by residents of an economy⁽³⁾ from engaging in various economic activities, irrespective of whether the economic activities are carried out within the economic territory of the economy or outside. Therefore, GNI and related statistics are particularly useful for analysing economic situations relating to income of residents, investment, domestic demand and inflation.

GNI is obtained by adding to GDP the primary income earned by residents from outside the economic territory and deducting primary income earned by non-residents from within the economic territory. Primary income includes income from direct investment, portfolio investment, other investment, reserve assets⁽⁴⁾ and compensation of employees. Similar to GDP, GNI can be compiled on the basis of current market prices and in chained dollars.

Real Gross National Income (RGNI) measures the real purchasing power of the total income earned by residents of an economy, taking into account the relative changes in import and export prices. RGNI at preceding year prices is obtained by adding the terms of trade adjustment and real net external primary income flows to GDP in volume terms. The RGNI in chained dollars is calculated using the annually re-weighted chain linking approach, in much the same way as the compilation of the chain volume measures of GDP.

In Hong Kong, the first set of GNI statistics was produced in 1995 in respect of the reference year of 1993.

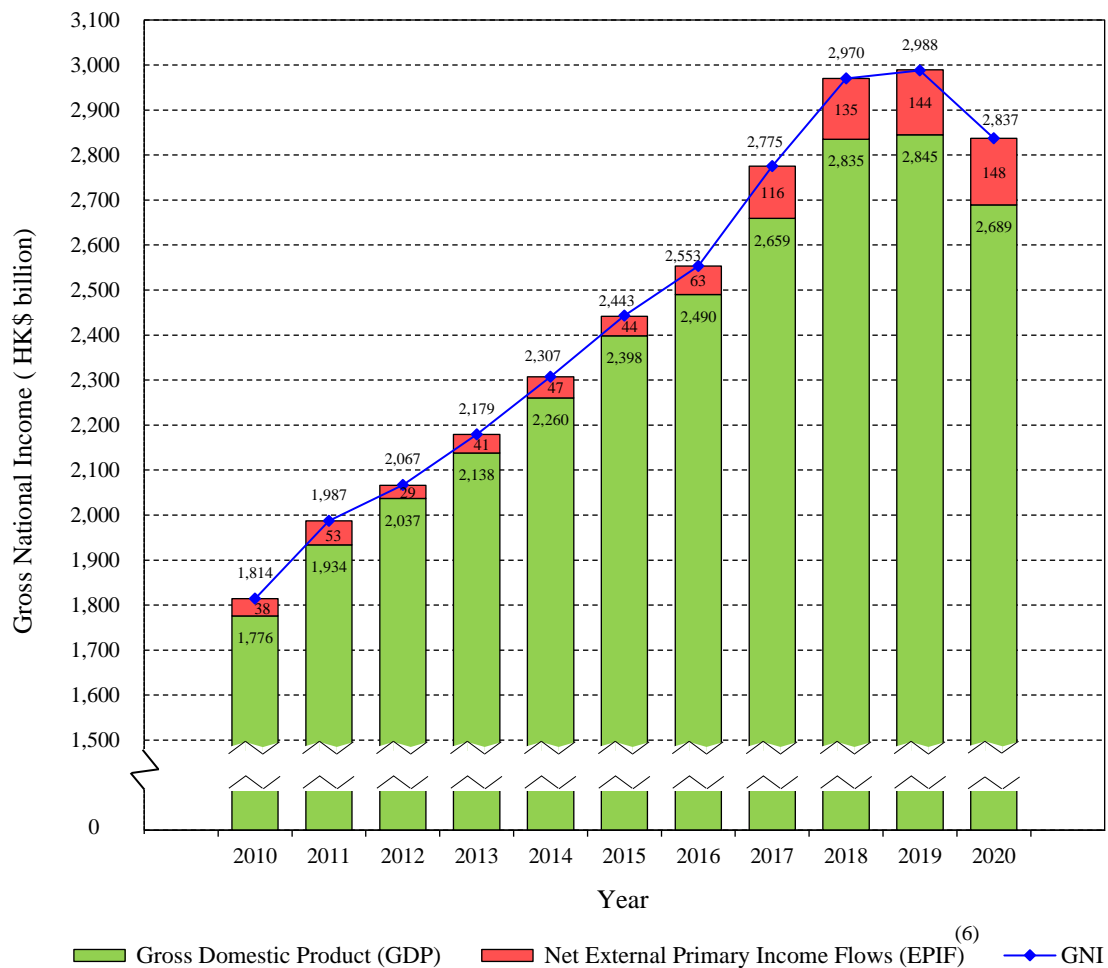
GNI for 2020 at current market prices was \$2,837.0 billion, or about 1.6 times of the corresponding figure for 2010. RGNI for 2020 in chained (2019) dollars was \$2,815.9 billion, or about 1.2 times of the corresponding figure for 2010.

Notes :

- (3) Residents of an economy include individuals and organisations. According to international standards, for individuals, residents refer to those who normally stay in the economic territory of the economy, irrespective of their nationality. If an individual has stayed in the economy for at least 12 months or intends to do so, he / she is considered as normally staying in that economy. For organisations, residents refer to those which ordinarily operate in the economic territory of the economy. The economic territory is the geographic territory under the effective control of the government of that economy. Conceptually, the residence status of individuals and organisations depends on their centre of predominant economic interest.
- (4) Please refer to the section on “Balance of Payments statistics” on page 81 for more details about direct investment, portfolio investment, other investment and reserve assets.

4 Other official statistics

Chart 4.4 Gross National Income of Hong Kong at current market prices, 2010 – 2020⁽⁵⁾



Balance of Payments (BoP) statistics

Just as you would keep track of your income, expenditure, investments, loans, etc., an economy would do the same by conducting “national accounting”. In particular, the economy would keep a BoP account, which records all its transactions with the rest of the world.

Notes :

(5) Individual figures may not add up to the respective total due to rounding.

(6) Net EPIF equals to external primary income inflow minus external primary income outflow.

BoP is a statistical statement that systematically summarises, for a specific time period (typically a year or a quarter), the economic transactions of an economy with the rest of the world (i.e. between residents and non-residents). A BoP account comprises two broad accounts : (a) the current account; and (b) the capital and financial account.

The current account measures the flows of goods, services, primary income and secondary income between residents and non-residents. Transactions recorded in this account reflect the provision and acquisition of resources by an economy to and from other economies.

The primary income account shows the amounts receivable and payable abroad in return for providing / obtaining use of labour, financial resources or natural resources to / from non-residents. Primary income mainly comprises compensation of employees and investment income. Compensation of employees is the return for the contribution of labour inputs to the production process. Investment income is the return for providing financial resources; it consists of dividends, reinvested earnings, interest, etc.

The secondary income account records current transfers between residents and non-residents. Current transfers are transactions in which real or financial resources that are likely to be consumed immediately or shortly are provided without the receipt of equivalent economic values in return. Examples include workers' remittances, donations, official assistance and pensions. Current transfers are unilateral in nature and are offsetting entries in the BoP account for one-sided transactions.

Within the capital and financial account, the capital account measures external transactions in capital transfers, and the acquisition and disposal of non-produced, non-financial assets (such as trademarks and brand names). Examples of capital transfers include forgiveness of debts by creditors and cash transfers involving the acquisition or disposal of fixed assets. The financial account records transactions in financial assets and liabilities between residents and non-residents. It shows how an economy's external transactions are financed. Transactions in the financial account are classified by function (i.e. the purpose of the investment) into direct investment, portfolio investment, financial derivatives, other investment and reserve assets.

Direct investment refers to external investment in which an investor of an economy acquires a lasting interest and a significant degree of influence or an effective voice in the management of an enterprise located in another economy. For statistical purpose, an effective voice is taken as being equivalent to a holding of 10% or more of the voting power in an enterprise.

4 Other official statistics

Portfolio investment refers to investment in non-resident equity securities and debt securities (e.g. bonds and notes, money market instruments), other than that included in direct investment or reserve assets. Compared with direct investors, portfolio investors in equity securities and debt securities of non-resident enterprises have no lasting interest or influence in the management of the enterprises concerned. A holding of less than 10% of the voting power in an enterprise is regarded as portfolio investment.

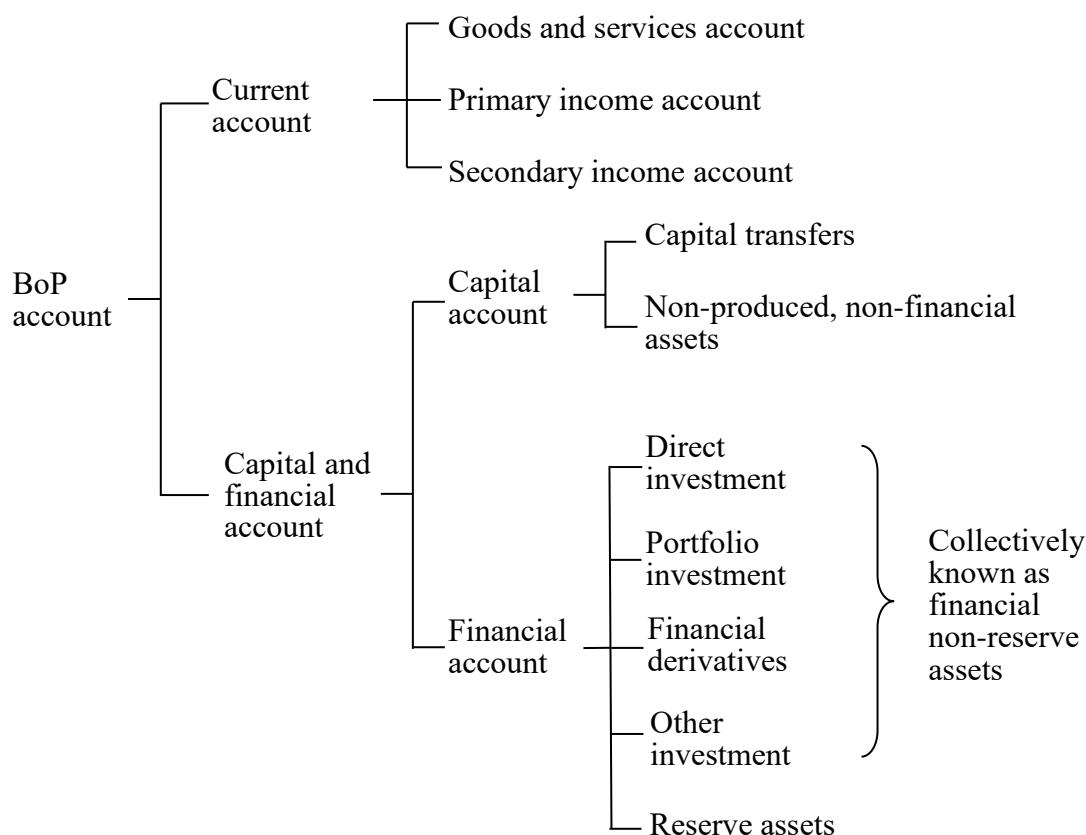
Financial derivatives are financial instruments that are linked to a specific financial instrument, indicator or commodity, and through which specific financial risks can be traded in financial markets in their own right. Financial derivatives include option-type contracts (e.g. warrants and options) and forward-type contracts (e.g. futures, interest rate swaps, currency swaps, forward rate agreements, forward foreign exchange contracts).

Other investment refers to other financial claims on and liabilities to non-residents that are not classified as direct investment, portfolio investment, financial derivatives or reserve assets. Other investment includes non-marketable loans, currency and deposits, trade credits and advances, and other assets / liabilities.

Reserve assets are external assets that are readily available to and controlled by the monetary authority of an economy (for Hong Kong, the Hong Kong Monetary Authority) for meeting BoP financing needs, for intervention in exchange markets to regulate the currency exchange rate of that economy, and for other related purposes (such as maintaining confidence in the currency and the economy, and serving as a basis for foreign borrowing).

4 Other official statistics

The following diagram shows the individual major components of the BoP account :



The overall BoP is the sum of the current account balance, the capital account balance, and the net change in financial non-reserve assets. In principle, this equals (but is in opposite sign) to the net change in reserve assets. A positive value of the overall BoP indicates a BoP surplus, while a negative value indicates a BoP deficit.

BoP statistics of Hong Kong are compiled and disseminated in accordance with the requirements stipulated in the Special Data Dissemination Standard of the International Monetary Fund (IMF). The annual BoP account of Hong Kong has been compiled since the reference year of 1998, while the quarterly BoP account has been compiled since the reference period of the first quarter of 1999.

In 2020, Hong Kong recorded a BoP surplus amounting to \$263.0 billion (as a ratio of 9.8% to GDP), as against a BoP deficit of \$8.9 billion (as a ratio of 0.3% to GDP) in 2019.

Of the major BoP components, the current account surplus widened to \$175.7 billion (as a ratio of 6.5% to GDP) in 2020, from \$166.3 billion (as a ratio of 5.8% to GDP) in 2019. For financial non-reserve assets, there was an overall net inflow of \$22.9 billion (as a ratio of 0.9% to GDP) in 2020, as against an overall net outflow of \$245.6 billion (as a ratio of 8.6% to GDP) in 2019.

4 Other official statistics

Besides the BoP account, the International Investment Position (IIP) statement is also an important component under the framework of BoP statistics.

While the BoP financial account measures transactions in external financial assets and liabilities of an economy occurred during a period, IIP reflects the level of such assets and liabilities at a particular time point. The former involves a flow concept, while the latter refers to a stock concept. Transactions are economic flows during a specific time period. On the other hand, stocks are positions in, or holdings of, assets and liabilities at a particular time point. Transactions in assets and liabilities, among other factors, will affect the stock of these assets and liabilities. In addition to transactions, price changes and exchange rate variations as well as other adjustments (e.g. reclassifications, unilateral cancellation of debts) also have an impact on the value of the stock of an economy's external financial assets and liabilities when expressed in the local currency of the economy.

C&SD started to release annual IIP statistics for Hong Kong in mid-2002. Time series on annual IIP statistics since the end of 2000 and quarterly IIP statistics since the first quarter of 2010 are available.

At the end of 2020, Hong Kong's external financial assets and liabilities amounted to \$48,767.7 billion and \$32,077.3 billion respectively. After netting out the external financial liabilities from the external financial assets, Hong Kong stood as a net creditor, with net external financial assets amounting to \$16,690.4 billion (equivalent to 6.2 times of GDP).

BoP and IIP statistics provide an integrated framework for the analysis of an economy's external economic relationships. They are important for monetary and financial monitoring and policy deliberations in both the domestic and international contexts.

The world economy is becoming increasingly integrated through international trade and investment flows. Globalisation of economic activities is a topic of concern to both the government and private sector of an economy. BoP statistics provide a lot of useful information required for the study of an economy's external orientation.

Besides, previous international financial crises have aroused increased interest in the analysis of IIP statistics, through which an economy's external vulnerability can be assessed. Analyses on the sizes of the external assets and liabilities by type of investment, by financial instrument and by sector allow us to understand which sector in the economy is most vulnerable.

Labour statistics

Labour statistics are very useful economic statistics regarding the labour force and labour market of Hong Kong. They reflect the characteristics of the economically active population and their economic activities. Since working is also an important aspect of one's life, labour statistics are considered as social statistics as well.

The labour force participation rate (LFPR) is obtained by expressing the size of the labour force as a percentage of the population of working age, i.e. population aged 15 and over. This is a measure of the working age population's propensity to be in the labour force. The size of the labour force of Hong Kong in 2020 was 3.89 million and the LFPR was 59.6%.

The unemployment rate, in particular, is one of the most important indicators describing the labour market situation. It refers to the percentage of "unemployed population" in the "labour force". Because of economic downturn, the unemployment rate reached the high level of 7.9% in 2003. The labour market improved drastically towards the end of 2003 and this trend sustained thereafter. Consequently, the unemployment rate dropped significantly to 3.5% in 2008. Impacted by the outbreak of the global financial tsunami in late 2008, the unemployment rate bounced back to 5.3% in 2009. Along with the gradual recovery of the economy from the global recession in 2009, the labour market saw notable improvement, with the unemployment rate gradually dropping from 4.3% in 2010 to 2.8% in 2018. However, owing to the elevated US-Mainland trade tensions and the local social incidents, the unemployment rate increased slightly to 2.9% in 2019. In 2020, owing to the impact of the COVID-19 pandemic, the unemployment rate increased sharply to 5.8%.

As the unemployment rate is subject to effects of seasonal variations (e.g. there are generally more job-seeking graduates entering the labour market in late summer, leading to a higher unemployment rate), short-term fluctuations, say between adjacent months or quarters, in the unemployment rate do not necessarily signal an actual change in the labour market conditions. Hence, when studying the underlying trend of unemployment, it is common to use the seasonally adjusted unemployment rate, which is obtained by using statistical methods that estimate and remove the seasonal variations from the original figures.

The definition used for measuring unemployment follows closely that recommended by the International Labour Organization (ILO). According to the definition, a person aged 15 or over is classified as unemployed if he / she satisfies all of the three following criteria :

- (a) has not had a job and should not have performed any work for pay or profit during the 7 days before enumeration;

4 Other official statistics

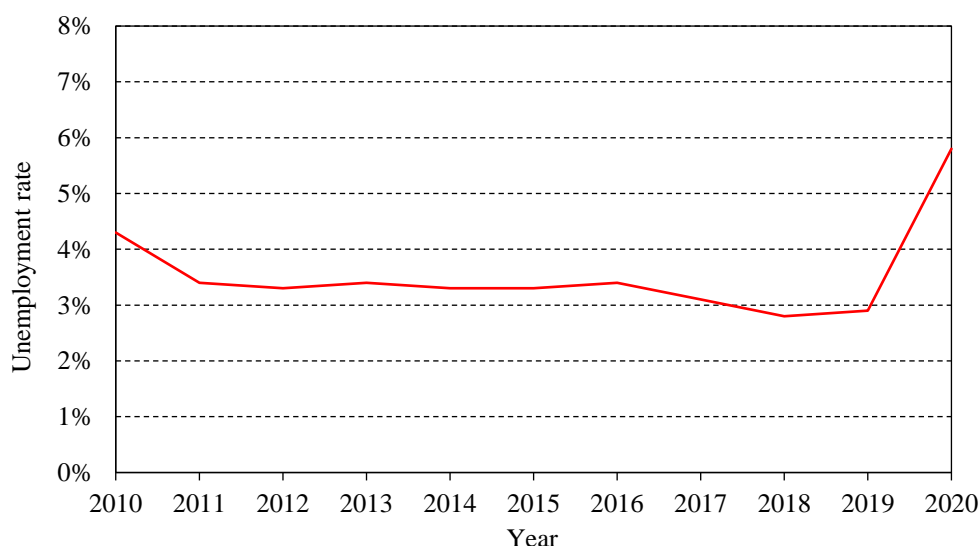
- (b) has been available for work during the 7 days before enumeration; and
- (c) has sought work during the 30 days before enumeration.

However, if a person aged 15 or over fulfils conditions (a) and (b) above only and he / she has not sought work during the 30 days before enumeration because he / she believed that work was not available, he / she is still classified as unemployed, and is regarded as a so-called “discouraged worker”.

It should be emphasised that “whether available for work” is an important condition for defining unemployment. Those persons who are not available for work because of one reason or another (e.g. being fully engaged in household duties) are not classified as unemployed even though they are without work, as they do not fulfil condition (b) of the above definition of unemployment, i.e. not available for work during the 7 days before enumeration.

When looking at the unemployment figures, it should be noted that “unemployment” is a state of affairs, which is not equivalent to the event of “losing a job”. For persons who have been dismissed from their jobs or who have left their jobs for certain reasons, but have managed to take up another job within a short period of time, they may not be counted in the unemployed population by definition, even though they have experienced the event of “losing a job” during the period.

Chart 4.5 Unemployment rate in Hong Kong, 2010 – 2020



Statistics in respect of “underemployed persons” also provide another useful piece of information about the labour force. The underemployed persons are defined as those employed persons who have involuntarily worked less than 35 hours during the 7 days before enumeration and have sought additional work during the 30 days before enumeration, or have not sought but have been available for additional work during the 7 days before enumeration. Those employed persons who worked less than 35 hours per week but have not been available for additional work and have not sought additional work (e.g. full-time teachers in bi-sessional schools) are not classified as underemployed.

Statistics on labour force, employment, unemployment and underemployment are compiled by C&SD based on the data collected from a continuous General Household Survey (GHS) conducted on households (and their members). The sample size of the GHS in a three-month period is about 25 000 households and the survey methodology adopted is in line with international standards and practices.

Apart from the aggregate figures mentioned above, a large amount of statistics analysed by various groupings (e.g. industrial and occupational distributions of the employed population) are also available from the GHS. These statistics are provided to the government bureaux and departments concerned for reference and are also published in the Quarterly Report on General Household Survey, which is available to the public on the C&SD website.

Furthermore, statistics on employment (i.e. number of employees and vacancies in different industries) and wage and payroll statistics are also compiled by C&SD. They are commonly referred to by entrepreneurs and human resources management personnel, since they provide information which is very useful for formulation of personnel management strategies. For example, firms can compare their staffing and vacancy situations with those of the industry taken as a whole or with those of other industries. They can also compare wage levels of their employees with others in the same industry. In addition, C&SD also compiles statistics on the level and distribution of wages of all employees in Hong Kong, as well as their employment and demographic characteristics. These statistics are essential inputs for analyses related to the Statutory Minimum Wage. They are also useful for studies on labour-related topics by the Government and the private sector. The relevant data are collected from surveys conducted on business establishments.

Price statistics

The Consumer Price Index (CPI) is another widely quoted item of official statistics. It is an important economic indicator which summarises changes over time in the price levels of consumer goods and services generally purchased by households. The year-on-year rate of change in the CPI is commonly used to reflect the inflation or deflation affecting households. Specifically, it measures changes in the total cost of a given basket of consumer goods and services representative of the purchases made by households in a specified time period.

The CPI has been widely accepted and used as a reference for salary adjustment purposes so as to maintain the purchasing power of employees in the face of changing prices.

The prices of some consumer goods and services may be subject to seasonal variations causing the CPI to rise or fall. Therefore, when studying changes in the CPI, it is common to refer to year-on-year changes (e.g. comparing the CPI of a month with that of the same month in the preceding year) so as to eliminate the effects of seasonal factors. Another alternative is to use the deseasonalised CPI. The latter is obtained by using statistical methods that estimate and remove the seasonal variations from the original index.

Households in different expenditure ranges have different expenditure patterns. Different series of CPIs are therefore compiled by C&SD to reflect the impact of consumer price changes on households in different expenditure ranges. The CPI(A), CPI(B) and CPI(C) are compiled based on the expenditure patterns of households in the relatively low, medium and relatively high expenditure ranges respectively. The Composite CPI, which is compiled based on the overall expenditure pattern of all these households taken together, reflects the impact of consumer price changes on the household sector as a whole.

Two types of data are required for compiling the CPI, namely price movements of consumer goods and services and their expenditure weights. Given the wide variety of consumer goods and services, it can be imagined that a lot of price data must be collected for the compilation of the CPI. Indeed, C&SD collects over 40 000 price quotations each month from around 3 500 local retail outlets and service providers in Hong Kong for the purpose of compiling the index. Price quotations are also collected from online outlets (both local and non-local) commonly patronised by households in Hong Kong as supplementary data in CPI compilation.



An enumerator is using a mobile tablet to collect retail prices of commodities for compiling the Consumer Price Index.

As for the expenditure weights, they are derived from the results of the Household Expenditure Survey (HES) which is conducted once every 5 years. As households spend more on some items and less on the others, similar price movements in different items may have different impacts on the households and effects on the overall price change. Therefore, a weighting system which represents the relative importance, in terms of expenditure, of individual items in the basket of consumer goods and services bought by households is required for the compilation of the CPI. The weight of each item represents the share of the item in the total expenditure of households.

As driven by the increases in food prices and private housing rents, annual rates of increase in the CPIs climbed up in 2011, and then stabilised during 2012 to 2014. The increasing trend in the CPIs started to moderate from 2015, due to the continued softening in international food and commodity prices as well as the strong US dollar. Annual rates of increase in the CPIs moderated further in 2017 and picked up again since 2018. However, the CPI registered a mild annual rate of increase in 2020 amid the COVID-19 pandemic.

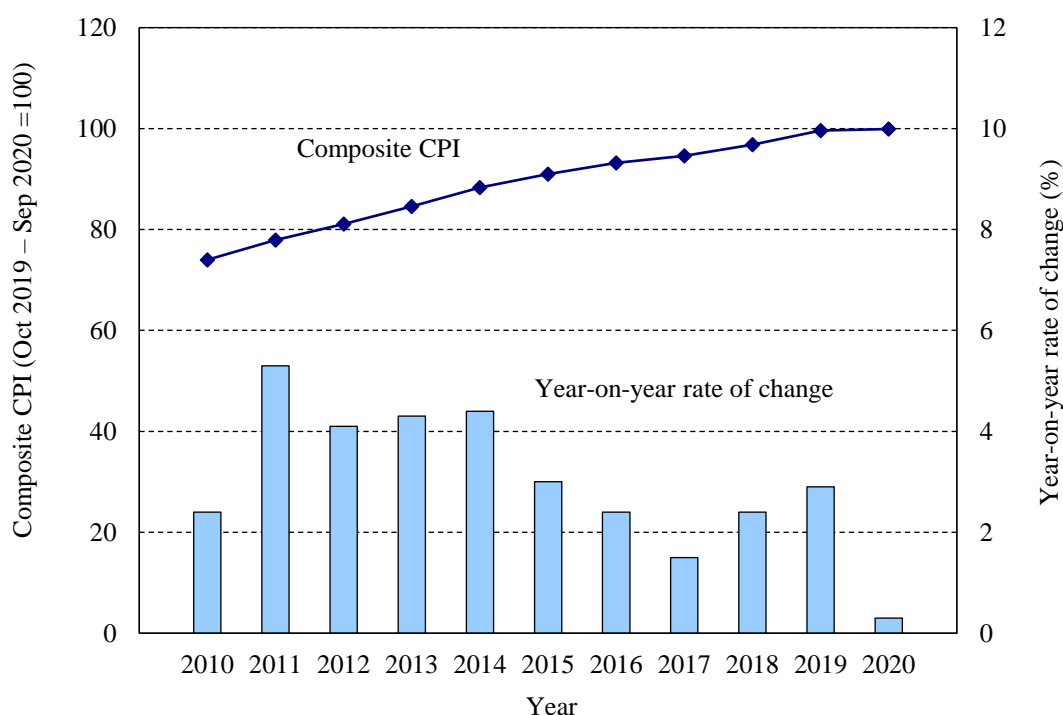
In making reference to the CPI or its change over time, it should be noted that the information thus conveyed reflects the collective experience of all households about inflation / deflation and that it does not always correspond to the experience of individual households. As each household has its own expenditure pattern and prices of different goods and services increase or decrease at varying rates, inflation / deflation does not affect all households to the same extent. If a household spends a lot on goods and services with rapid price increases / decreases, the household will feel greater impact of inflation / deflation.

Besides, people are generally psychologically more aware of isolated cases of drastic price changes, especially those which affect them personally. Thus, one would tend to notice and remember only those large price changes and do not realise that there are other cases of moderate or small price changes. Even individual members of the same household may feel different impacts of price changes. Therefore, while personal experience may be subjective or biased, the CPI provides an objective assessment of price changes affecting households generally.

Another point to note is that the CPI measures changes in the price level of consumer goods and services purchased by households. If we buy more goods or consume services of higher quality than before, then the increase in expenditure is not solely caused by price increase.

4 Other official statistics

Chart 4.6 Composite Consumer Price Index and its year-on-year rate of change, 2010 – 2020^{(7), (8)}



Operating statistics of businesses

Statistics from economic surveys conducted periodically by C&SD provide information about business trend, cost structure and profit situation in various economic sectors. Firms can make use of the statistics to compare their own performance against the general situation within their specific sectors and adjust their business strategies accordingly.

Other economic statistics

Shipping statistics are compiled by C&SD in collaboration with other parties.

Notes :

- (7) The CPIs from October 2019 onwards are compiled based on expenditure weights obtained from the 2019/20 Household Expenditure Survey. The CPIs for earlier periods are compiled based on old weights and have been re-scaled to the new base period for linking with the new index series.
- (8) From October 2020 onwards, the year-on-year rates of change are derived from the 2019/20-based CPIs. The year-on-year rates of change before October 2020 were derived using the index series in the base periods at that time (e.g. the 2014/15-based index series for compiling the rates of change during the period from October 2015 to September 2020), compared with the index a year earlier in the same base period.

4 Other official statistics

(B) Social statistics

Social statistics broadly comprise the following areas : population statistics, poverty statistics, education statistics, transport statistics, housing statistics, medical and health statistics, social welfare statistics and crime statistics.

Population statistics

Population statistics have already been discussed in detail in Chapters 1 to 3. It may be emphasised again here that population statistics, which depict the size, growth and socio-economic characteristics of the Hong Kong population, are among the most useful items of statistical information for government administrators. They are of prime importance in the formulation and administration of government policies in such areas as education, housing, transport, medical and health, and social welfare services. For businesses, population statistics are useful in identifying potential target markets more accurately and in supporting better investment decision-making.

Poverty statistics

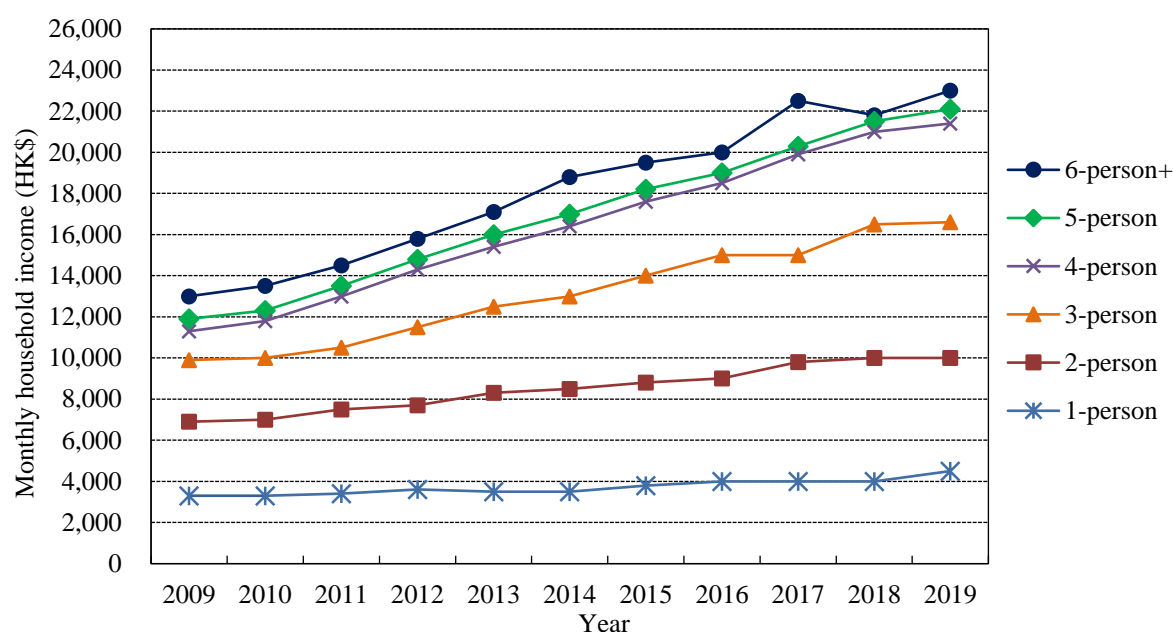
Setting a poverty line is useful for better understanding of Hong Kong's poverty situation and supporting the formulation of poverty alleviation policies.

Generally speaking, there are two mainstream approaches in deriving a poverty line viz. "absolute poverty" and "relative poverty". While the former defines those individuals who cannot meet a level of "minimum subsistence" or "basic needs" as "poor", the latter refers "poor" as those whose living standards are below that of the general public.

4 Other official statistics

In the case of Hong Kong, the concept of “relative poverty” is adopted. Under this approach, household income before policy intervention (purely theoretical assumption)⁽⁹⁾ (i.e. with the impact of taxation and cash transfers removed) is used as the basis for a measurement yardstick and the main poverty line is set at 50% of median household income in respect of each household size. As such, poor households refer to the number of households with monthly household income less than the poverty line while poor population refers to the number of persons in these households. Poverty rate is the ratio of poor population to total population in domestic households. To evaluate the effectiveness of poverty alleviation measures, these poverty indicators based on household income before and after policy intervention (recurrent cash)⁽¹⁰⁾ would be compared.

Chart 4.7 Poverty lines by household size, 2009 – 2019



Notes :

- (9) “Pre-intervention” (purely theoretical assumption) household income refers to the original household income without any policy intervention. It only includes households’ own employment earnings and other non-policy intervention cash income. This is a form of “simulated” household income which does not exist in reality and only represents a certain portion of the total disposable income. Setting a poverty line on such basis aims to reveal the most fundamental situation of a household, and to avoid any distortion of policy measures on the poverty line thresholds.
- (10) “Post-intervention” (recurrent cash) household income is derived by deducting taxes payable and adding back all recurrent cash benefits (such as Comprehensive Social Security Assistance, Old Age Allowance, Old Age Living Allowance, Disability Allowance, Work Incentive Transport Subsidy and Working Family Allowance) from the original household income. The derived household income can more genuinely reflect the amount of monthly disposable cash available in the “pocket” of a household.

4 Other official statistics

As the poverty line is defined in a way relative to median household income by household size, the poverty line for a particular household size group will be raised along with an increase in the median household income in respect of that household size group. The economy fell into recession in the second half of 2019. As labour demand began to slacken, growth in employment earnings of the grassroots also decelerated further in 2019. Against this background, the growth in median household income moderated noticeably. The poverty line thresholds showed a similar trend of decelerating increase in 2019. The poverty lines of 3-person households to 5-person households registered the smallest increases in a decade (ranging from 1.1% to 2.8%⁽¹¹⁾). The poverty line of 2-person households remained virtually unchanged, ending its continuous upward trend for nine years. The annual changes of the poverty line thresholds of 1-person households and 6-person-and-above households were the exceptions, with the former rising markedly by 12.5% to \$4,500 in 2019 and the latter rebounding after a visible fall in the preceding year.

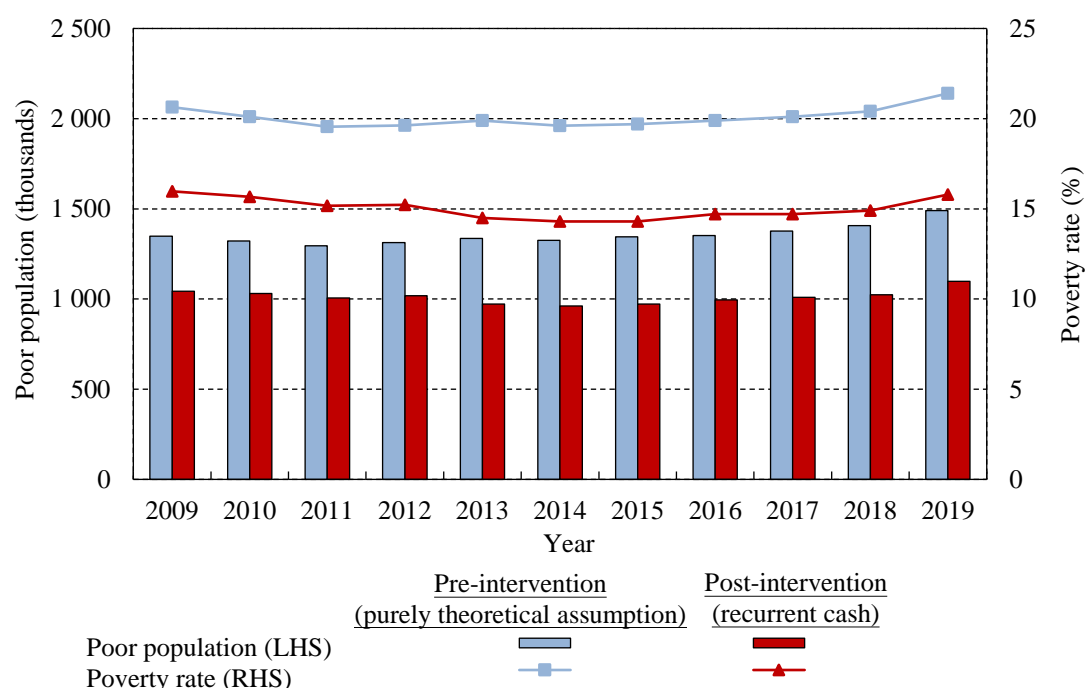
In 2019, the local economy fell into recession and the labour market situation deteriorated during the year. These, coupled with the continuous effect of structural factors of population ageing and dwindling household size, contributed to a notable worsening in the overall poverty situation. After recurrent cash intervention, the overall number of poor households and the poor population in 2019 increased notably to 474 000 (+39 200 or +9.0%) and 1 097 800 (+73 500 or +7.2%) respectively, with the poverty rate up by 0.9 percentage point to 15.8%. Before policy intervention (purely theoretical assumption), increases in some of the poverty indicators would be even more pronounced, with the number of poor households, the poor population and the poverty rate up to 648 500 (+35 700 or +5.8%), 1 490 700 (+84 200 or +6.0%) and 21.4% (+1.0 percentage point) respectively over the period.

Note :

(11) The annual changes in poverty line thresholds are calculated based on unrounded figures.

4 Other official statistics

Chart 4.8 Poor population and poverty rate, 2009 – 2019



Caution should be taken in interpreting the figures relating to the poverty line in the light of the following caveats :

- Assets are not taken into account when deriving the poverty line. Given that household income is used as the single indicator for measuring poverty without considering the amount of assets and liabilities, some “asset-rich, income-poor” people might be classified as poor.
- The “poverty line” is not a “poverty alleviation line”. Without considering household assets, the poverty line cannot be taken as the eligibility criteria of any poverty alleviation initiatives. On the contrary, even if the household incomes of some groups are slightly above the poverty line, they will still be eligible for government subsidies if they meet the means tests for individual support schemes.
- With the poverty line set at a percentage of the median household income (implying that the threshold of the poverty line is not a “fixed income level”), the poor population always exists statistically.

Other social statistics

Education statistics, transport statistics, housing statistics, medical and health statistics, social welfare statistics and crime statistics are basically compiled by the respective government bureaux and departments to meet specific planning and administrative needs. They are also useful to the Government as a whole in formulating broad-range policies. Coordination is necessary to ensure that statistics relating to different areas can be used together in a compatible way for planning activities which cut across various facets of the society.

On education, there are three main areas of statistics, viz. pupils, teachers and school place provision. The Education Bureau compiles a lot of statistics which are very useful for formulating policies and planning facilities.

Regular public transport operating statistics and related statistics on transport are compiled. These provide a basis for understanding the transport and traffic situation of Hong Kong and for transport planning.

Housing statistics cover housing stock and housing production in both the public and private sectors. They also relate to the situation in various housing estates. They are very useful in reflecting the housing conditions of the people of Hong Kong and are important references when planning for housing development is undertaken.

Medical and health statistics provide information about births, diseases, deaths, health-related behaviours and health services. They facilitate a better understanding of health status of people in Hong Kong and are useful to the Government for disease surveillance and control, and formulation of health measures.

Social welfare statistics attempt to establish the number and characteristics of individuals in the community who require assistance, in particular the aged, the unemployed, the disabled, the orphaned or deserted children, the delinquent and people in families with special problems. These statistics are useful in planning, review and monitoring of the provision of social welfare services.

Crime statistics are compiled on the basis of crimes reported to the police, which partially reflect the state of law and order in the society. Some crimes are not reported and statistics on unreported crimes may be collected through the conduct of a survey on crime victimisation periodically.

From a general data user's perspective, social statistics provide an objective and in-depth view of the respective facets of the society, as they can effectively reflect developments and shortfalls in various areas of living conditions and provision of social services.

4 Other official statistics

Ways of obtaining official statistics

C&SD disseminates official statistics through different media, with emphasis on the service principles of friendly access and prompt delivery.

For statistics of common interest, C&SD issues press releases to the media. The schedule for issuing around 130 press releases of regular nature in each calendar year is announced to the media in September of the preceding year. The [schedule](#) is also available to the general public for reference on the C&SD website.

Statistics which should be of general public knowledge are also uploaded on the C&SD website under the “Statistics” section.

C&SD also produces different types of statistical products. Members of the public can download statistical publications and detailed statistical tables of C&SD free of charge from the C&SD website.

To cater for the changing technological environment and service needs, continuous efforts have been made in enhancing the contents and functionality of the C&SD website with a view to further promoting better understanding and application of statistics in the community. The department’s first Annual Open Data Plan was announced on the C&SD website in December 2018. To support the government’s Open Data Policy, statistical tables, datasets and press releases available on the C&SD website have been listed on DATA.GOV.HK for free download and re-use by the public for both commercial and non-commercial purposes. Moreover, statistical datasets in machine readable format (XLS, CSV or XML) are available on the website to provide the statistics currently published in PDF format in statistical reports.

Proper understanding of the concepts and definitions of different kinds of statistics is imperative for their correct interpretation and application. Apart from providing statistical information to the public, C&SD is also prepared to give advice on the interpretation and application of statistics so as to maximise their utilisation to users. In case users require assistance or statistics more detailed than those contained in the press releases and publications of C&SD, they are welcome to approach C&SD for assistance by telephone, facsimile, letter, electronic mail or personal visit. A [list of telephone numbers, facsimile numbers, office addresses and e-mail addresses](#) is given at the C&SD website.

4 Other official statistics

Further information

The above contents present only part of the economic and social statistics produced by C&SD and various government bureaux and departments. For further information regarding the official statistics covering various social and economic aspects of Hong Kong (e.g. latest statistics, statistical reports, concepts and methods), please visit the following sections of the C&SD website :

[Labour force, employment and unemployment](#)

[External trade](#)

[National accounts](#)

[Balance of Payments](#)

[Prices](#)

[Business prospects](#)

[The Four Key Industries and other selected industries](#)

[Energy](#)

[Housing and property](#)

[Public finance, money and market](#)

[Innovation and technology](#)

[Transport](#)

[Information and communications](#)

[Tourism](#)

[Education](#)

[Health](#)

[Social welfare](#)

[Law and order](#)

[Culture, entertainment and recreation](#)

[Environment, climate and geography](#)

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

4 Other official statistics

Exercise

Please give a ✓ in the appropriate box (☐) for the correct answer.

1. The population of Hong Kong in mid-2020 was

- ☐ 5.75 million
- ☐ 6.50 million
- ☐ 7.48 million
- ☐ 7.24 million

2.

<u>Year</u>	<u>Crude birth rate in Hong Kong</u> (Number of births per 1 000 population)
2011	13.5
2020	x

$x =$

- ☐ 7.6
 - ☐ 5.8
 - ☐ 9.3
 - ☐ 9.8
3. If the crude death rate in a given year was 5.0 deaths per 1 000 population and the crude birth rate was 7.2 births per 1 000 population, the rate of natural change per 1 000 population in the period was
- ☐ -2.4
 - ☐ 2.2
 - ☐ -12.0
 - ☐ 12.0
4. Most of the visitors visiting Hong Kong in 2020 came from
- ☐ United States of America
 - ☐ Japan
 - ☐ The Mainland
 - ☐ Europe

4 Other official statistics

5. The population in mid-2015 = a ; and
the population in mid-2020 = b .
The compound average growth rate per annum of the population in this period was
- ☐ $\left(\sqrt[4]{\frac{b}{a}} - 1\right) \times 100\%$
- ☐ $\frac{\left(\frac{b}{a} - 1\right)}{4} \times 100\%$
- ☐ $\left(\sqrt[5]{\frac{b}{a}} - 1\right) \times 100\%$
- ☐ $\frac{\left(\frac{b}{a} - 1\right)}{5} \times 100\%$
6. In 2020, the size of the labour force in Hong Kong was
- ☐ 3.82 million
- ☐ 3.88 million
- ☐ 3.95 million
- ☐ 3.89 million
7. Which category of persons is regarded as economically inactive?
- ☐ Unpaid family workers
- ☐ Employers
- ☐ The unemployed
- ☐ Full-time home-makers
8. Which of the following is not an approach in the compilation of the Gross Domestic Product?
- ☐ Expenditure approach
- ☐ Production approach
- ☐ Industrial approach

Part II

Survey methods and basic statistical concepts

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5 Survey methods



Introduction

Statistics on births, deaths and net movements used in making population projections are compiled from birth and death registration records and immigration clearance records. In addition, information on the latest size and age-sex structure of the population and on various other aspects of persons in the population has to be obtained. This can be achieved by conducting a population census or by-census.

Administrative records, such as the registration records mentioned above, and survey results, such as those obtained through a population census / by-census, are the typical sources of data from which statistics are compiled.

Administrative records provide an economical and accurate data source. However, since they are primarily intended for certain specific purposes, they may not completely meet the statistical requirements, unless special provision has been made to cater for such requirements. Naturally, there are situations where meeting such requirements would mean distorting the original purposes of the administrative records too much. In such circumstances we would have to give up the idea of generating the required statistics as a by-product of the administrative system, and resort to other means of data collection.

Surveys are another important means of data collection whereby the objects of our study are interviewed, observed or given questionnaires to fill in. If we design the survey in such a way that all objects of study will be contacted, one way or another, the survey is specifically referred to as a “census”. If only a sample of the objects is taken for data collection later on, then the survey is more clearly described as a “sample survey”. The language in this aspect is, however, a little loose sometimes. When the word “survey” is used, quite often it is implied that only a sample is taken.

Census versus sample survey

When deciding whether a census or a sample survey should be carried out, a number of factors should be considered. For studies in which the “population” (i.e. the group of persons or other objects we wish to study) is large, a proper sample survey, as compared to a census, is very useful for cutting down the resources required, including money and manpower, and for reducing the overall burden imposed on the persons / objects to be studied. Another benefit of carrying out a sample survey instead of a census is that we can collect, summarise and analyse data more quickly when the information is urgently needed.

5 Survey methods

On the other hand, a complete census can be considered if very accurate information is required on small sub-divisions of the “population” under study, and when comprehensive data on the “population” are needed for forming a benchmark to support further statistical analyses, such as projections.

Population census and by-census

In a population census, basic information is collected from all persons in the population of a country / territory while in a population by-census, only a large sample of persons is covered. Usually a population census is conducted once every ten years. A by-census may be conducted in between two censuses to update the information obtained from the last census.

Because of its long history world-wide, and when there is not likely to be confusion, “population census” is abbreviated as “census” for convenience. Thus, it should be noted that there can actually be census of agriculture, census of industry and so on, apart from population census.

Population censuses and by-censuses taken in Hong Kong

The history of population census in Hong Kong can be traced back to 1841. Earlier censuses were simple, with headcounts taken only. The “1961 Census” was the first population census in which detailed information was collected on a broad spectrum of demographic, social and economic characteristics of the population. Since then, it has become a well-established practice in Hong Kong to conduct population censuses and by-censuses at regular intervals. Censuses were conducted in 1961, 1971, 1981, 1991, 2001, 2011 and 2021. By-censuses were conducted in 1966, 1976, 1986, 1996, 2006 and 2016.

Details of the last population by-census are available in the section “The 2021 Population Census” in Chapter 1.

Objectives of conducting population censuses and by-censuses

In a dynamic city like Hong Kong, many changes in major characteristics of the population occur in a relatively short span of time. Up-to-date and reliable information on the size, composition and geographical distribution of the population is necessary for forward planning by the Government. Moreover, as Hong Kong develops into an international business centre, census and by-census data are widely used in assessing market conditions and making investment plans. Such data will also help researchers in studying important social issues.

5 Survey methods

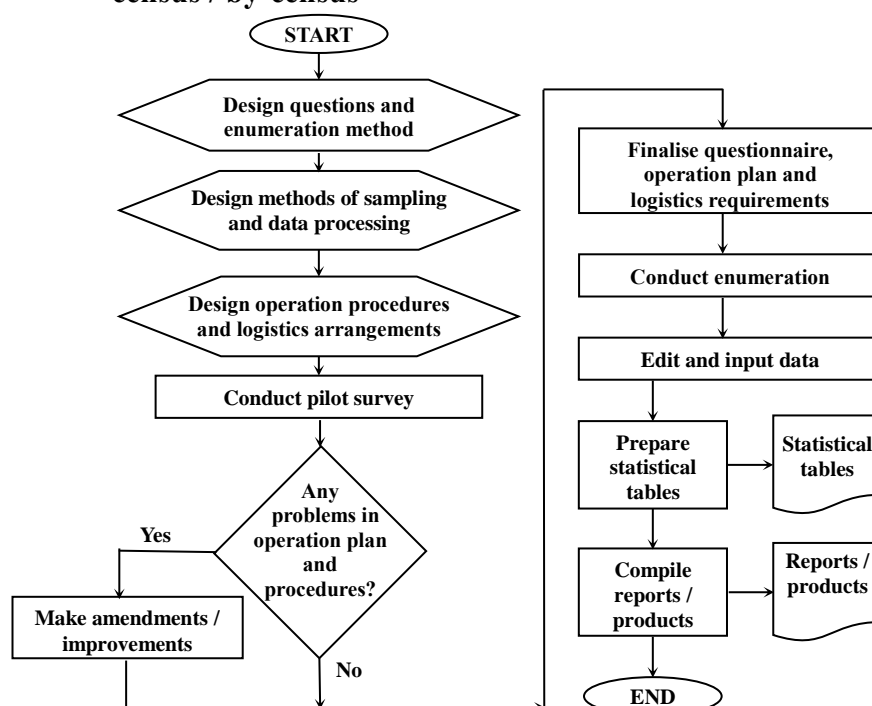
Preparation for conducting a population census or by-census

Conducting a population census or by-census involves a vast amount of preparatory work. These preparatory activities include :

- (1) geographical work, such as preparing maps and lists of places;
- (2) determining the data needs of the Government, business sector and other sectors;
- (3) determining the questions to be included and the statistical tables to be compiled;
- (4) designing the sampling methodology and method of estimation;
- (5) deciding on the method of enumeration, e.g. whether field workers are to conduct household interviews or household members to fill in questionnaires by themselves, as well as detailed plans in applying online questionnaires / telephone interviews; and
- (6) planning the data processing procedures.

To ensure the effectiveness of the population census / by-census operation plan, a pilot survey will be conducted during the preparatory stage of every population census / by-census so as to test the questionnaire and operation procedures as well as to confirm the logistics requirements. Based on the results of the pilot survey, the operation plan is then amended / improved as appropriate for actual implementation. The pilot survey is particularly important for ensuring the smooth conduct of large scale surveys (such as population censuses / by-censuses) which involve the mobilisation of a large number of workers and other resources.

Chart 5.1 Main steps in planning and conducting a population census / by-census



5 Survey methods

Census order

Furthermore, legislation is needed to provide a legal basis for conducting the population census or by-census. Under the [Census and Statistics Ordinance \(Chapter 316\)](#), C&SD is vested with the authority to conduct population census or by-census. The legislation requires all persons to give particulars for themselves and their dwelling places in the data collection process. It also lays down penalties for those who refuse to do so. On the other hand, it contains strict provisions for safeguarding the confidentiality of the information supplied by individual households and persons, which assure that such information will only be used for compiling statistics and will not be released to any parties, including other government departments.

Public support for the population census / by-census

While there are legal provisions in relation to the conduct of population censuses and by-censuses, it is important for the community to realise that the findings of the census / by-census are crucial to the future planning of Hong Kong and that public participation and cooperation are essential in making the operation successful.

In the 21C, a considerable number of students and teachers were recruited as temporary field workers to undertake various tasks. They thus had a chance to participate actively in this important project. Training on interviewing techniques and other necessary skills was provided. Some school premises were used as field centres for the field operation.

Processing of population census / by-census data

After raw data are collected from households and individuals in the population, they must undergo a number of processes before statistical outputs can be produced. The raw data are first edited to correct for inconsistent answers. They are then converted into codes for input into the computer. Finally, various computations are performed by the computer to produce statistical tables in appropriate formats.

Dissemination of population census and by-census results

Results of the more recent rounds of population census and by-census are published in the forms of summary reports and detailed reports. Users can refer to them easily and make use of the results for various purposes. In particular, data users can use the free-of-charge online [Interactive Data Dissemination System](#) to build their own statistical tables. Results of the 16BC are obtainable from the [website of the 2016 Population By-census](#).

5 Survey methods

Other surveys

Apart from population censuses and by-censuses, C&SD and other government bureaux and departments also carry out other surveys to collect various types of social and economic data.

Examples of [surveys carried out by C&SD](#) are :

- General Household Survey
- Monthly Survey of Retail Sales
- Monthly Retail Price Survey
- Household Expenditure Survey
- Quarterly Survey of Employment and Vacancies
- Annual Earnings and Hours Survey
- Annual Survey of Economic Activities

Examples of surveys carried out by other government bureaux and departments are :

- Enrolment Survey (by Education Bureau)
- Traffic Census (by Transport Department)
- Health Manpower Survey (by Department of Health)

Important points to note in conducting surveys

In planning and conducting surveys, there are a number of major points which need to be carefully considered :

(A) Overall planning

- (1) The objectives of the survey should be clearly specified.
- (2) The population covered by the survey should be clearly defined with reference to the survey objectives. “Population”, in the context of a survey, refers to the totality of objects under study. The objects may be human being or otherwise.
- (3) It should be ensured that respondents of the survey are able to provide the information required.
- (4) Adequate resources such as time, money and manpower should be available for the survey.
- (5) In conducting a survey, professional advice is often required and should preferably be sought at an early stage to ensure that the various steps of a survey are properly planned. This is because rectification is normally very difficult after the survey is completed and its results are found to be invalid.

5 Survey methods

(B) Design and selection of sample (in case a sample survey instead of a census is to be conducted)

- (1) Probability sampling methods should be used as far as practicable, instead of non-probability sampling methods. In probability sampling methods, every unit in the population has a known and non-zero probability of being sampled. This allows researchers to draw inferences scientifically from the sample results about the entire population. Examples of probability sampling methods include simple random sampling, stratified random sampling, systematic sampling and cluster sampling.
- (2) Non-probability sampling methods such as haphazard sampling (i.e. picking the sampling units as they come along or as convenient), quota sampling (i.e. selecting sampling units according to some criteria, such as 50% being male and 50% being female, but the selection of units is at the discretion of the interviewers) and self-initiated telephone / online polling (i.e. interested individuals dial a telephone number / visit a website at their own initiative to give views) should be avoided because such methods normally induce biases to the survey results.
- (3) The sample size depends on the characteristics of the population under study, the choice of sampling method and the desired precision level of the estimates. It can be worked out using established statistical methodology. In general, a larger sample size is needed if estimates of higher precision are required.
- (4) Substitution of sampling units or respondents should not be done once they have been selected according to a pre-set sampling method.

(C) Questionnaire design

- (1) The questionnaire used for a survey should contain questions which are relevant, precise, unambiguous, well-sequenced and appropriately phrased. If the questions involve tapping of opinions, care should be taken to avoid questions which may lead respondents towards the direction of a certain answer or questions being loaded in favour of a particular response.
- (2) Requiring respondents to provide an answer while they are unable to do so or genuinely have no opinion will result in invalid answers. Answers like “don’t know” or “no opinion” should be allowed in the questionnaire, as appropriate.
- (3) The questionnaire should not be too long.
- (4) To ensure the effectiveness of the questionnaire, a pilot test of the questionnaire should be conducted on potential respondents.

(D) Collection of raw data

- (1) The mode of data collection, such as the use of personal interviews, telephone interviews, online questionnaires or self-administered questionnaires by mail, should be carefully selected by considering the respondents' willingness to cooperate, the degree of complexity of the subject of enquiry and other relevant factors.
- (2) Various arrangements related to fieldwork should be carefully planned in order to ensure smooth and efficient operation. Fieldwork procedures should be thoroughly tested before implementation.
- (3) The interviewers should be carefully briefed on the concepts and definitions of terms used in the survey and properly trained on the survey procedures before they start working.
- (4) Interviewers should ensure that respondents understand the questions. Probing should be done where necessary. This, however, should not be overdone, lest unnecessary influence will be exerted on respondents.
- (5) Every effort should be made to minimise non-contact or refusal cases of respondents because a low response rate may induce a serious bias in the survey results. Adequate publicity of the survey, proper introduction of the surveying organisation, clear identification of interviewers, and giving advance notice to sampled respondents should help. Arrangements should also be made to follow up on non-contact respondents and to persuade uncooperative respondents to participate.
- (6) The identity and information supplied by individual respondents should be kept confidential. With such assurance, respondents would feel at ease and would be more willing to provide individual or organisational information and opinions. It should be emphasised that survey is a kind of statistical work and not an investigation on individuals.

(E) Processing of raw data and compilation and analysis of statistics

- (1) Raw data should be carefully and thoroughly checked before compilation of statistics.
- (2) Appropriate statistical methodology should be adopted in compiling and analysing the data. In particular, in case a sample design has been used where the probability of selection of every individual respondent is not equal, it is necessary that proper weighting methods are applied to survey results to give unbiased population estimates.
- (3) Due deliberation should be made to decide on an appropriate sub-grouping scheme in analysing survey results at disaggregate levels, taking into account the precision of estimates derived from the sample.

(F) Dissemination of survey results

- (1) It is a usual practice to publish the survey results if the subject of the survey is related to a topic of public interest.
- (2) The survey results should be presented in the form of aggregate statistics so that information supplied by individual respondents would not be disclosed.
- (3) A comprehensive survey report should contain details about different aspects of the survey, in particular details on population coverage, sample design, sample size, sampling error, response rate and likely sources of non-sampling error. Where appropriate, specimen of the questionnaire should be attached.
- (4) When the survey results are released to the media, sufficient details on the survey methodology should be provided in addition to survey findings such that the media may report both. Otherwise, members of the public will have no basis to assess the reliability of the findings.

Assessing quality of survey results

There are many factors that will affect the quality of data obtained from a sample survey. In assessing the data quality of a survey, at least the following issues should be considered :

- (1) Whether the sample of the survey is selected in accordance with a probability sampling method;
- (2) Whether the sample size is sufficiently large;
- (3) Whether the questionnaire is well designed; and
- (4) Whether the response rate of the survey is sufficiently high.

A well-designed and properly selected sample is crucial to the quality of results derived from a survey. Nevertheless, some survey-takers may not appreciate the need for conducting surveys scientifically. “Street-corner surveys” and “self-initiated telephone / online polling” that we frequently come across are examples of non-scientific surveys.

5 Survey methods

In “street-corner surveys”, interviewers pick on passers-by haphazardly. Even though sometimes there are stipulations such as 50% of interviewees being male and 50% being female (such selection procedures are known as “quota sampling”), there is still much discretion for the interviewers to pick the interviewees within such stipulations. Thus, interviewees who seem to be more approachable will have a much greater tendency to be selected generally. Moreover, out of convenience, busy street corners are often chosen for interviewing and thus people who tend to avoid busy spots will have little chance of being selected. Therefore, samples taken through these surveys may not be representative of the target population.

Also, respondents of “self-initiated telephone / online polling” are not selected through an objective method. Because of this, we can expect that people who tend to be more concerned about the subject and have stronger views will be more willing to call / go online while others may not. Obviously, data so obtained cannot be taken for granted to represent the target population.

In a scientific survey, the sample should be selected from a well-defined population by a probability sampling method. Only when probability sampling method is employed, statistical inference based on the data obtained from the sample can be appropriately made.

Apart from using a scientific sampling method, the size of the sample (i.e. the number of selected respondents) of a survey should be sufficiently large. Otherwise, the results of the survey may be subject to substantial error. One should also note that sometimes even though the sample size may be large enough for estimating the characteristics of the “population”, it may not be large enough for estimating the characteristics of certain sub-groups. Consideration for providing estimates pertaining to certain sub-groups should take into account the precision of the corresponding estimates.

In surveys, data are very often collected by way of a questionnaire, though sometimes by observations. Hence, the design of the questionnaire will affect directly the quality of data to be collected. As an example, consider the question : “Many people are against smoking. Do you smoke?” This is obviously a leading question. In fear of counteracting the social norm, a respondent may have a tendency of giving a negative response even though he / she is a habitual smoker. The reliability of data obtained from such a question is dubious.

Last but not least, the response rate achieved in a survey is also an important indicator that helps assess the quality of survey results. Response rate is the percentage of selected respondents who are successfully interviewed. Low response rate will introduce non-response bias to the data because the characteristics of the non-respondents may often be quite different from those of respondents. Therefore, the results of surveys with a low response rate are likely to be biased and misleading.

5 Survey methods

References

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Moser, C.A. and Kalton, G., *Survey Methods in Social Investigation*, Chapter 2, Heinemann Educational Books Ltd., 1979.

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United Nations Statistics Division, [*Principles and Recommendations for Population and Housing Censuses, Revision 3, 2017.*](#)

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

Exercise

Conducting surveys

Readers can design and conduct a survey by drawing reference to the following illustrative example regarding the major procedures in conducting a school survey.

(1) Listing and sampling

There are several possible methods :

- (i) A list of all students in the school is prepared and all students are to be surveyed. This is a “census”.
- (ii) The above list is prepared. By drawing lots, a pre-set number of students is selected. (A more advanced treatment is to use “random” numbers but lot-drawing can achieve the same purpose.) This is called a “simple random sampling method”.
- (iii) Another convenient yet scientific method is to prepare a list of all classes, then randomly select a pre-set number of classes by lot-drawing, and survey all students in the selected classes. This is called a “cluster sampling method”.

Methods (ii) and (iii) above involve “random” selection, which should be distinguished from arbitrary choice of students or classes. The students selected from these methods would form a representative sample for the whole school.

(2) Questionnaire design

The type of information to be collected has to be decided first. Subsequently questions are designed to collect the required information. The information usually includes basic data about the students, such as their age, sex and class. The primary questions may focus on some of their characteristics or about their opinions on certain aspects. A specimen questionnaire is provided herewith for collecting information on students’ habit of surfing the Internet. More items may be added if necessary.

5 Survey methods

(3) Data collection and editing

To collect the information, interviewers may interview respondents (i.e. the selected students) or distribute the questionnaires for self-completion by the respondents themselves. If the interviewing method is used, the interviewers should be trained to conduct interviews properly, ensuring that the questions are understood by respondents and complete answers are supplied. If self-completion method is used, questionnaires normally have to be simple and fully self-explanatory. The completed questionnaires are then edited subsequently. If there are errors, they have to be rectified.

(4) Data processing and analysis

Data in the questionnaires are then processed, with the aid of the computer if necessary. Statistical tables are produced. Graphs may also be prepared for further discussion and analysis. Some simple statistical indicators may also be calculated from the data collected.

Below are some other hints in organising the school survey :

- (i) When setting the questionnaire, try to limit the number of questions to no more than some 15 questions. Keep the questions concise yet precise. Avoid using open-ended questions in a relatively simple survey.
- (ii) Before carrying out the actual school survey, try to test the questionnaire with some potential respondents to see whether it is clear and easy to understand, and whether the respondents are able to provide the information.
- (iii) It is necessary to make sure that every selected student has completed one and only one questionnaire. Omissions and duplications should be rectified.
- (iv) It is necessary to instill in the interviewers a sense of respect for private information. They should be aware of the need to avoid revealing to any unauthorised person the information with regard to individual persons obtained in the interviews. (A small ceremony may be held for interviewers to take an oath on this obligation. This may also boost respondents' confidence in giving true information).
- (v) To process the data, workers can work in groups for data coding, editing, counting, computing, etc. Editing is a process to correct inconsistencies and to eliminate omissions found in answers in the completed questionnaires.

5 Survey methods

- (vi) There are many ways to present the findings. For example, obtain simple frequency count of each variable and present the frequency distributions in the form of bar graphs, line graphs or pie charts.
- (vii) To find out relationship among different variables, it may be interesting to cross-tabulate some of them as follows :
 - number of students by type of housing by monthly household income;
 - number of students by type of housing by type of equipment used to surf the Internet;
 - number of students by type of housing by number of hours spent on surfing the Internet; and
 - number of students by age by purpose for surfing the Internet.

Points to note

The “population” in the school survey (whether a census of the students or a sample survey of them) comprises all students of the school in question. The findings are applicable to students of the school (if the survey is conducted properly). One should be careful not to generalise the findings to, say, students of the district where the school is situated or even to all students of Hong Kong. If we do wish to find out facts about all students of Hong Kong, the design of the survey will have to be more complex and the scale of the operation will be much bigger.

Survey questionnaire

Serial No. : _____

Please put a “✓” in the appropriate answers.

(1) Age : _____ (in complete years)

(2) Sex : 1 ☐ Male 2 ☐ Female

(3) Number of household members (including yourself) : _____

(4) Type of housing

- 1 ☐ Public rental housing
- 2 ☐ Subsidised home ownership housing
- 3 ☐ Private housing

(5) Monthly household income

- 1 ☐ Less than \$10,000
- 2 ☐ \$10,000 - \$19,999
- 3 ☐ \$20,000 - \$29,999
- 4 ☐ \$30,000 - \$39,999
- 5 ☐ \$40,000 - \$49,999
- 6 ☐ \$50,000 or more

(6) What is your major purpose(s) for surfing the Internet?

(You may choose more than one option.)

- 1 ☐ Communication with others (e.g. sending/receiving messages/e-mails)
- 2 ☐ Online entertainment (e.g. playing Internet games, watching videos/movies)
- 3 ☐ Online shopping
- 4 ☐ Surfing social media
- 5 ☐ Searching for information
- 6 ☐ Others (please specify: _____)

(7) How much time did you totally spend in surfing the Internet last week?

- 1 ☐ Less than 10 hours
- 2 ☐ 10 to less than 20 hours
- 3 ☐ 20 to less than 30 hours
- 4 ☐ 30 to less than 40 hours
- 5 ☐ 40 hours or more

5 Survey methods

(8) How often did you use the Internet to search for information for your study last week?

- 1 ☐ Less than 5 times
- 2 ☐ 5 to less than 10 times
- 3 ☐ 10 to less than 15 times
- 4 ☐ 15 times or more

(9) What kind(s) of equipment do you usually use to surf the Internet?

(You may choose more than one option.)

- 1 ☐ Smartphone
- 2 ☐ Notepad / tablet
- 3 ☐ Notebook / desktop computer
- 4 ☐ Others (please specify: _____)

(10) Which of the following web browsers do you prefer to use for surfing the Internet?

(You may choose more than one option.)

- 1 ☐ Internet Explorer / Microsoft Edge
- 2 ☐ Google Chrome
- 3 ☐ Firefox
- 4 ☐ Safari
- 5 ☐ Others (please specify: _____)

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6 Uses and misuses of statistics



Introduction

“Statistics” has two meanings: first, as information in quantitative form relating to an aggregate group, i.e. the numbers themselves; second, as the subject in science dealing with such information, i.e. the principles and methods which have been developed for handling data. Information pertaining to an individual element – be it a person, firm or other subject of interest – is, on its own, normally not referred to as “statistics”. In the context of statistical work, such information is called raw data, which become statistics only after going through some compilation or processing steps such as summation or calculation of average. Hence, the two aspects of statistics, as information and methodology, have interlocking relationships.

Statistics, as a subject in science, plays an increasingly important role on various fronts. It is widely used in business, education, science, engineering, and economic and social research. It also serves as a useful tool to facilitate better understanding of the society and discussion of socio-economic issues in a scientific manner.

Although statistics are useful, it is important to use them properly. Statistical data have to be of reasonably good quality before they are put into use and this relies on proper methods of data collection and compilation. When interpreting and analysing statistics, appropriate techniques should be applied, or else wrong conclusions may be arrived at.

Uses of statistics

(1) Description of situations

People are often looking for relevant information in a form which can help them understand the situations at work or in their daily lives. For example, a headmaster observes that students of the S1 class seem to be taller than the students of the S1 class five years ago (this is a piece of qualitative information as it represents the perception of a phenomenon).

To ascertain this, information on the height of each student in the S1 class and similar information of students in the S1 class five years ago are studied. However, there are hundreds of students and going over the records alone may only give an impression of the students’ height in general, leading to merely a broad confirmation of the headmaster’s impression.

6 Uses and misuses of statistics

The most common way to tackle this kind of situation is to calculate the “mean” height for each of the two groups. The summarisation of individual students’ data to an aggregate form, i.e. “statistics”, is a more precise, quantitative description of the situation.

(2) Comparison

Comparison is to assess whether two or more groups of items have different properties, e.g. comparison between districts, countries, or different points of time.

In the above example of students’ height, the headmaster can compare the average height of each of the two groups of students and then identify which group of students are on the whole actually taller, and by how much.

(3) Detection of relationship

Examples include detection of relationship between smoking and having lung cancer, and the relationship between income and expenditure.

(4) Evaluation

An example is the evaluation of the effectiveness of certain action programmes, such as the “Water Conservation Campaign”.

(5) Prediction

An example is the prediction about the future based on existing trends and knowledge of relevant developments, such as sales forecast and population projections.

(6) Support for policy formulation

An example is to make reference to data on current and future road traffic obtained in a study to decide whether a highway should be constructed.

(7) Operational and process control

An example is to use statistics for application in the quality control process of manufactured goods.

6 Uses and misuses of statistics

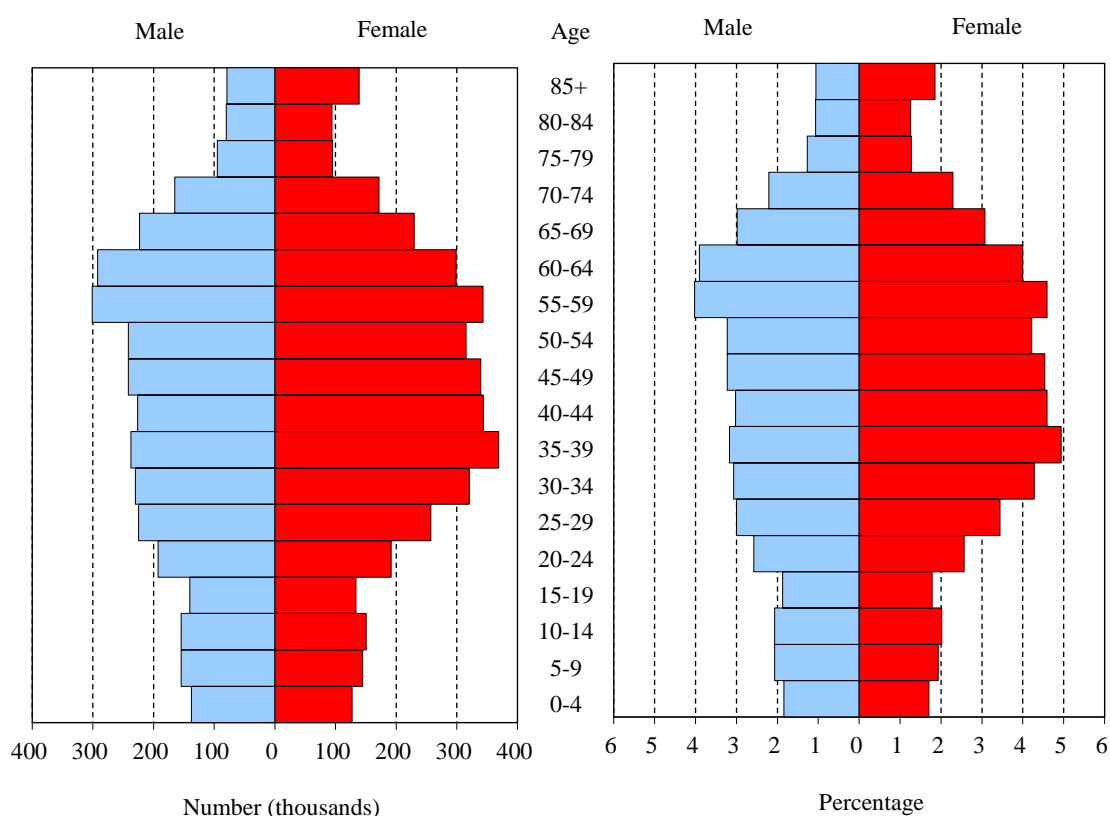
Social statistics

Social statistics are concerned with such subjects as the social environment, demographic characteristics of people, their activities and their opinions and attitudes.

Some important social statistics are :

- (1) Demographic characteristics
- population size
 - population composition
 - births
 - deaths
 - net movements
 - marriages

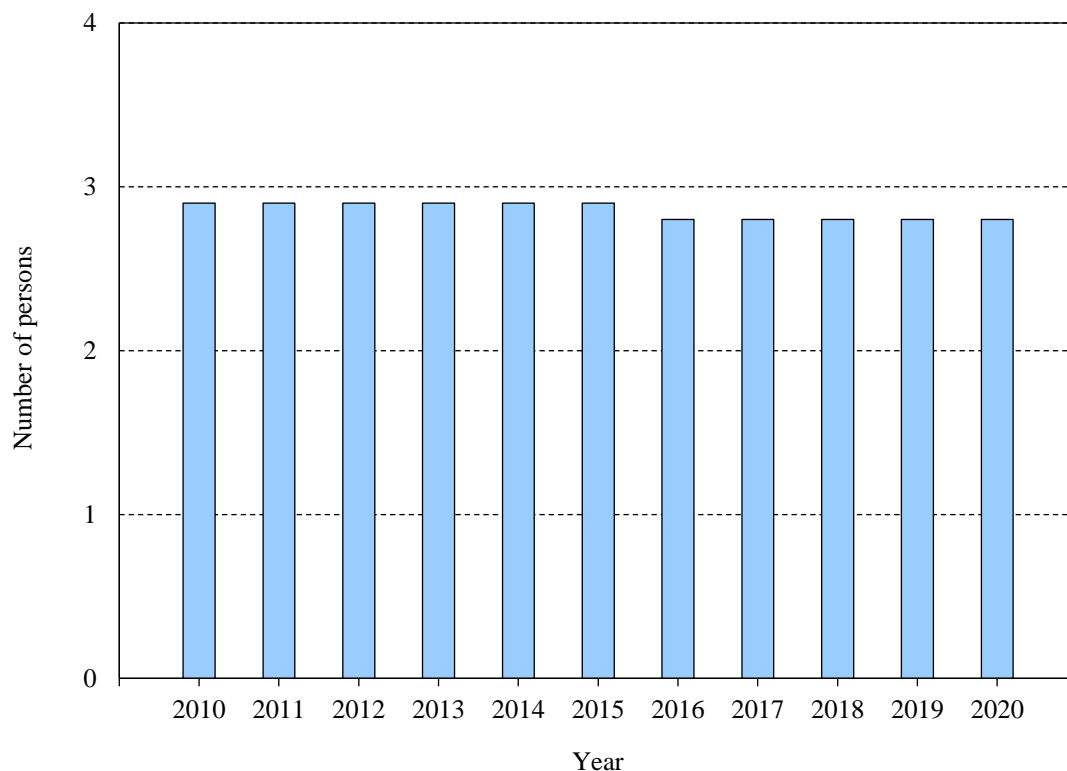
Chart 6.1 Population of Hong Kong by age and sex, mid-2020



6 Uses and misuses of statistics

- (2) Domestic households⁽¹⁾
- household size
 - household composition
 - household income

Chart 6.2 **Average domestic household size, 2010 – 2020**



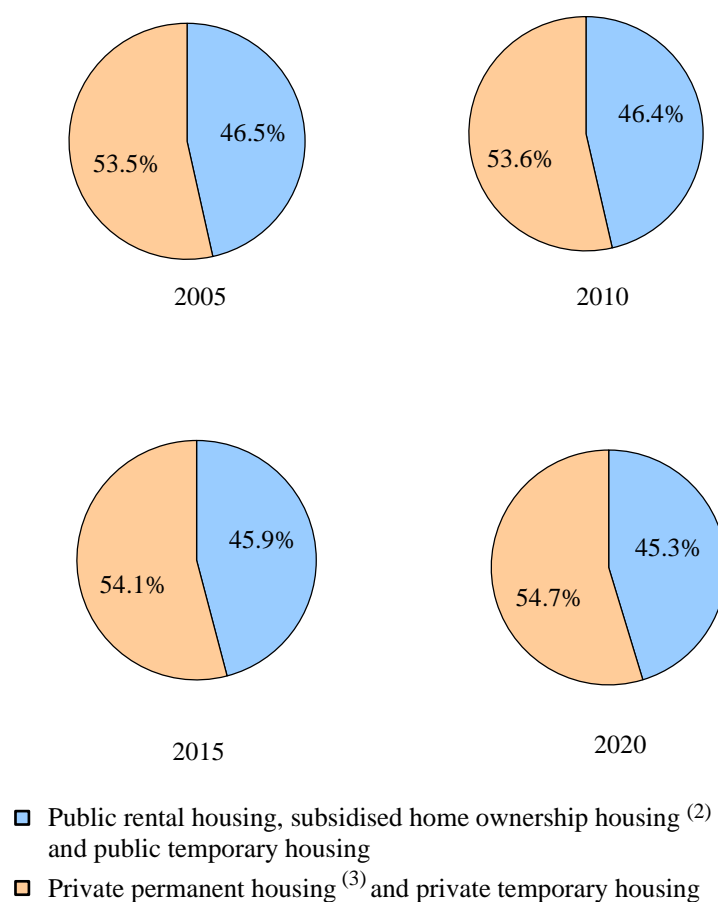
Note :

- (1) A domestic household consists of a group of persons who live together and make common provision for essentials for living (e.g. sharing food and utensils). These persons need not be related. If a person makes provision for essentials for living without sharing with other persons, he / she is also regarded as a household. In this case, the household is a “one-person household”. Households comprising only non-Hong Kong residents or Mobile Residents are not classified as domestic households.

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- (3) Housing
- stock of permanent quarters
 - housing facilities
 - housing type
 - degree of sharing
 - tenure of accommodation
 - rent

Chart 6.3 **Percentage distribution of domestic households by type of housing, 2005 – 2020**



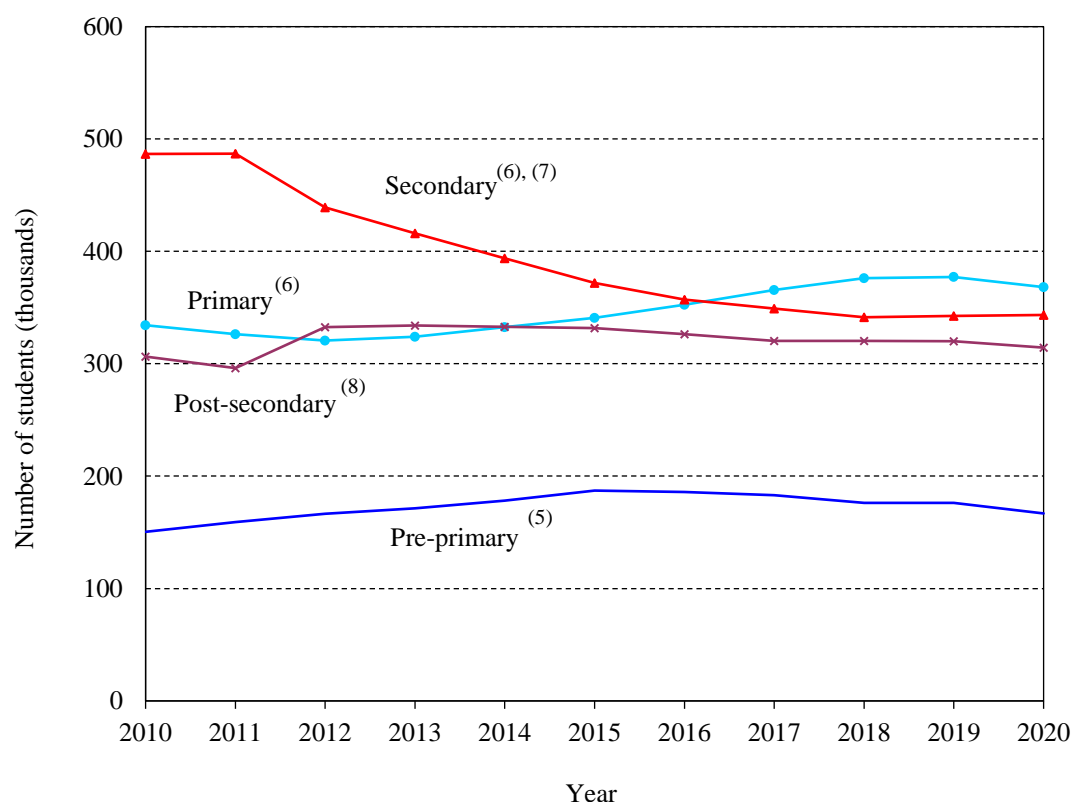
Notes :

- (2) Subsidised home ownership housing includes flats built under the Home Ownership Scheme, Middle Income Housing Scheme, Private Sector Participation Scheme, Green Form Subsidised Home Ownership Scheme, Buy or Rent Option Scheme and Mortgage Subsidy Scheme, and flats sold under the Tenants Purchase Scheme of the Hong Kong Housing Authority. It also includes flats built under the Flat for Sale Scheme, Sandwich Class Housing Scheme and Subsidised Sale Flats Projects of the Hong Kong Housing Society; and flats in Urban Renewal Authority Subsidised Sale Flats Scheme. Subsidised sale flats that can be traded in open market are excluded.
- (3) Figures include private housing blocks, flats built under the Urban Improvement Scheme of the Hong Kong Housing Society, villas / bungalows / modern village houses, simple stone structures / traditional village houses and quarters in non-residential buildings. Subsidised sale flats that can be traded in open market are also put under this category.

6 Uses and misuses of statistics

- (4) Education - educational attainment of population
 - schools
 - teachers
 - student enrolment

Chart 6.4 Student enrolment⁽⁴⁾ by level of education, 2010 – 2020



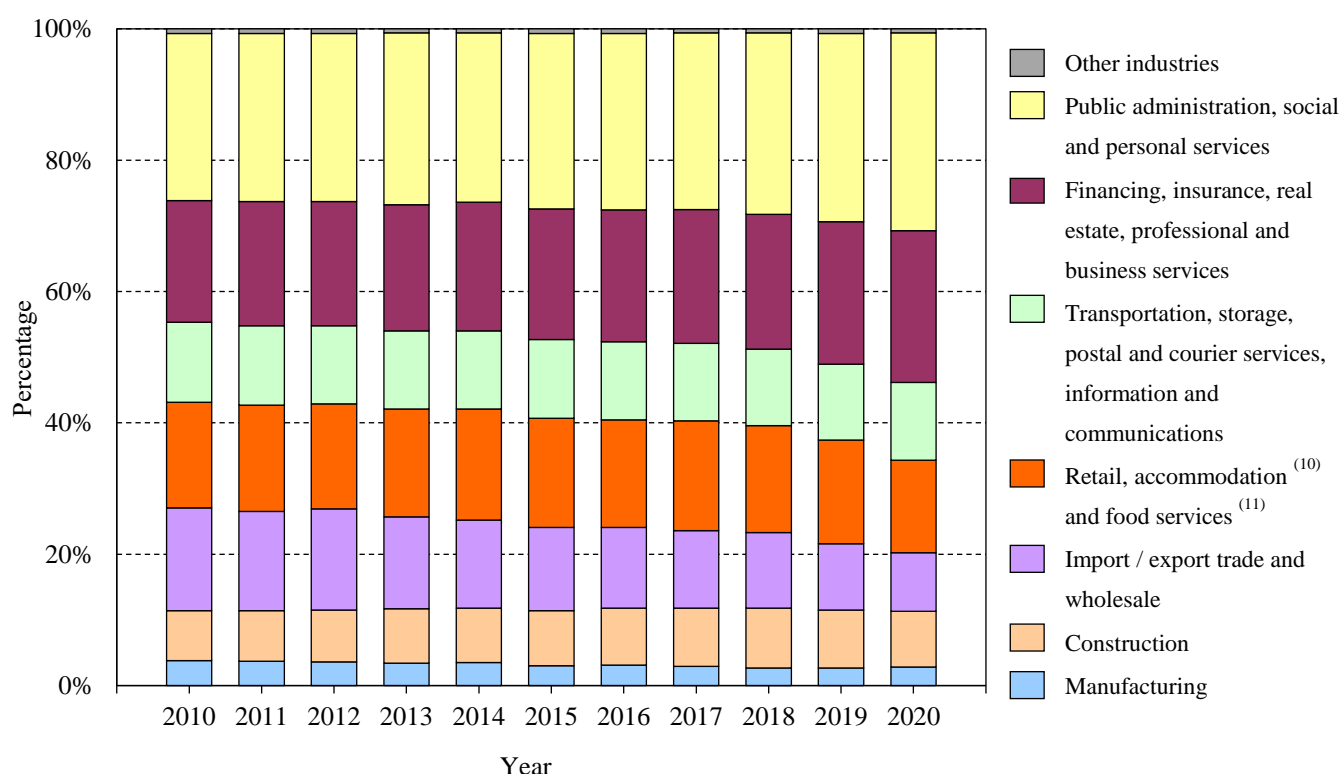
Notes :

- (4) Figures include both full-time and part-time students attending long programmes lasting for at least one school / academic year. Figures do not include students attending tutorial, vocational and adult education courses offered by schools below post-secondary education level. Figures for secondary and post-secondary education for 2020 are provisional.
- (5) Figures include nursery, lower and upper classes in kindergartens and kindergarten-cum-child care centres registered under the Education Bureau, and special child care centres registered under the Social Welfare Department.
- (6) Figures include special schools.
- (7) Figures include evening schools, craft level courses and Diploma Yi Jin programme. Prior to the 2012/13 school year, secondary education covers Secondary 1 to Secondary 7. Upon implementation of the New Senior Secondary Academic Structure, there are no subsidised Secondary 7 places under local curriculum starting from the 2012/13 school year.
- (8) Figures include universities and colleges offering post-secondary courses including certificate / diploma, associate degree or equivalent and bachelor degree or above; and also non-local registered or exempted courses leading to non-local higher academic qualifications and operated jointly with non-local institutions.

6 Uses and misuses of statistics

- (5) Employment
- labour supply
 - unemployment and underemployment
 - distribution of employed persons by industry
 - distribution of employed persons by occupation
 - hours worked
 - earnings from employment

Chart 6.5 Distribution of employed population by industry⁽⁹⁾, 2010 – 2020



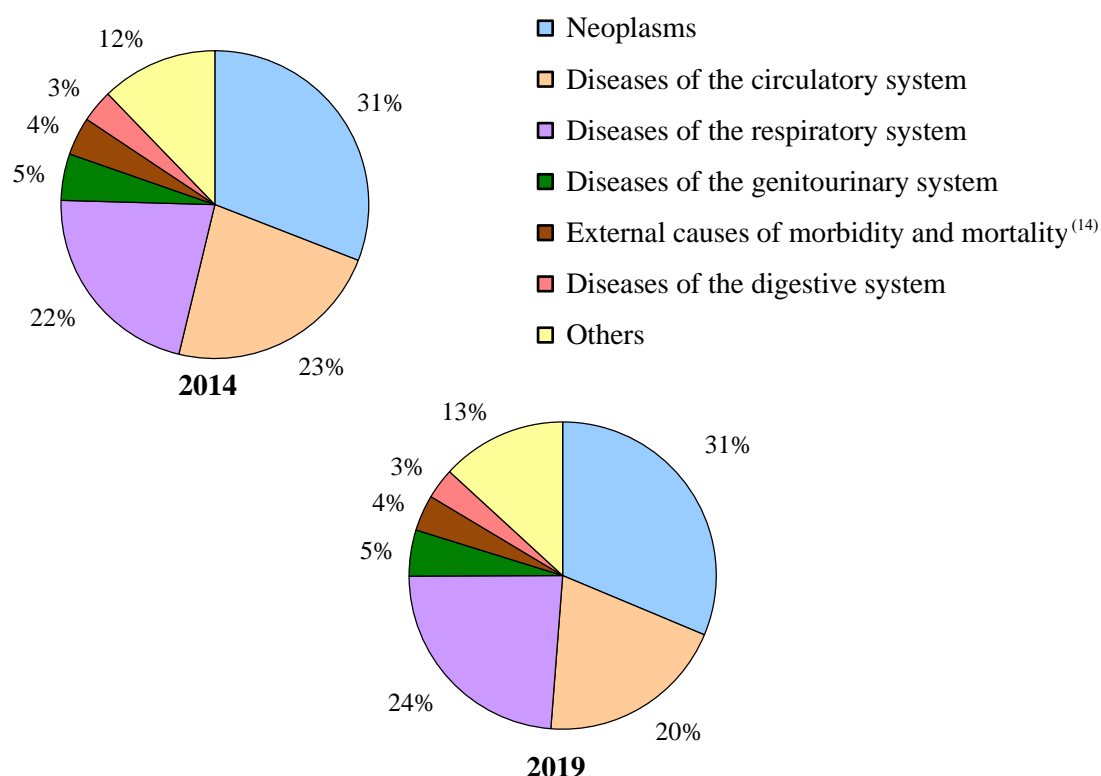
Notes :

- (9) Figures are compiled based on Hong Kong Standard Industrial Classification Version 2.0.
- (10) Accommodation services cover hotels, guesthouses, boarding houses and other establishments providing short term accommodation.
- (11) The retail, accommodation and food services industries as a whole is generally referred to as the consumption- and tourism-related segment.

6 Uses and misuses of statistics

- (6) Medical and health
- healthcare facilities and services
 - health manpower
 - patients
 - diseases
 - causes of death

Chart 6.6 Registered deaths by cause, 2014 and 2019^{(12), (13)}



Notes :

- (12) Classification of diseases and causes of death is based on the International Statistical Classification Diseases of and Related Health Problems (ICD) 10th Revision.
- (13) Individual percentages may not add up to 100 due to rounding.
- (14) According to the ICD 10th Revision, when the morbid condition is classifiable under Chapter XIX as “injury, poisoning and certain other consequences of external causes”, the codes under Chapter XX for “external causes of morbidity and mortality” should be used as the primary cause of death.

6 Uses and misuses of statistics

- (7) Social welfare
 - beneficiaries and benefits
 - services for the elderly
 - family and child welfare services
 - services for young people
 - rehabilitation and medical social services
 - institutional services

- (8) Law and order
 - crimes
 - victims
 - judicial services
 - prisoners / inmates and correctional services

- (9) Culture, entertainment and recreation
 - cultural, entertainment and sports presentations
 - recreational facilities

6 Uses and misuses of statistics

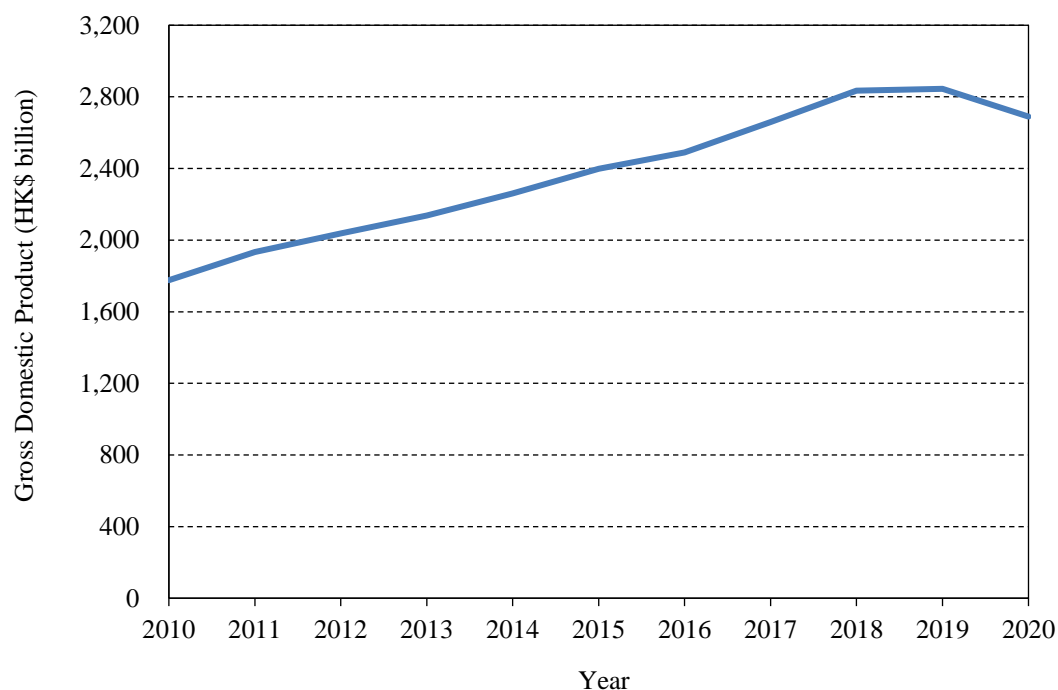
Economic statistics

Economic statistics are statistics related to the structure and performance of an economy and the operating characteristics of different industries. Some statistics can be treated as either economic or social statistics under different analytical frameworks, such as wages and employment.

Some important economic statistics are :

- (1) National Income and Balance of Payments statistics
 - Private consumption expenditure
 - Gross Domestic Product
 - Investment income
 - Gross National Income
 - Balance of Payments account
 - International Investment Position
 - External Debt

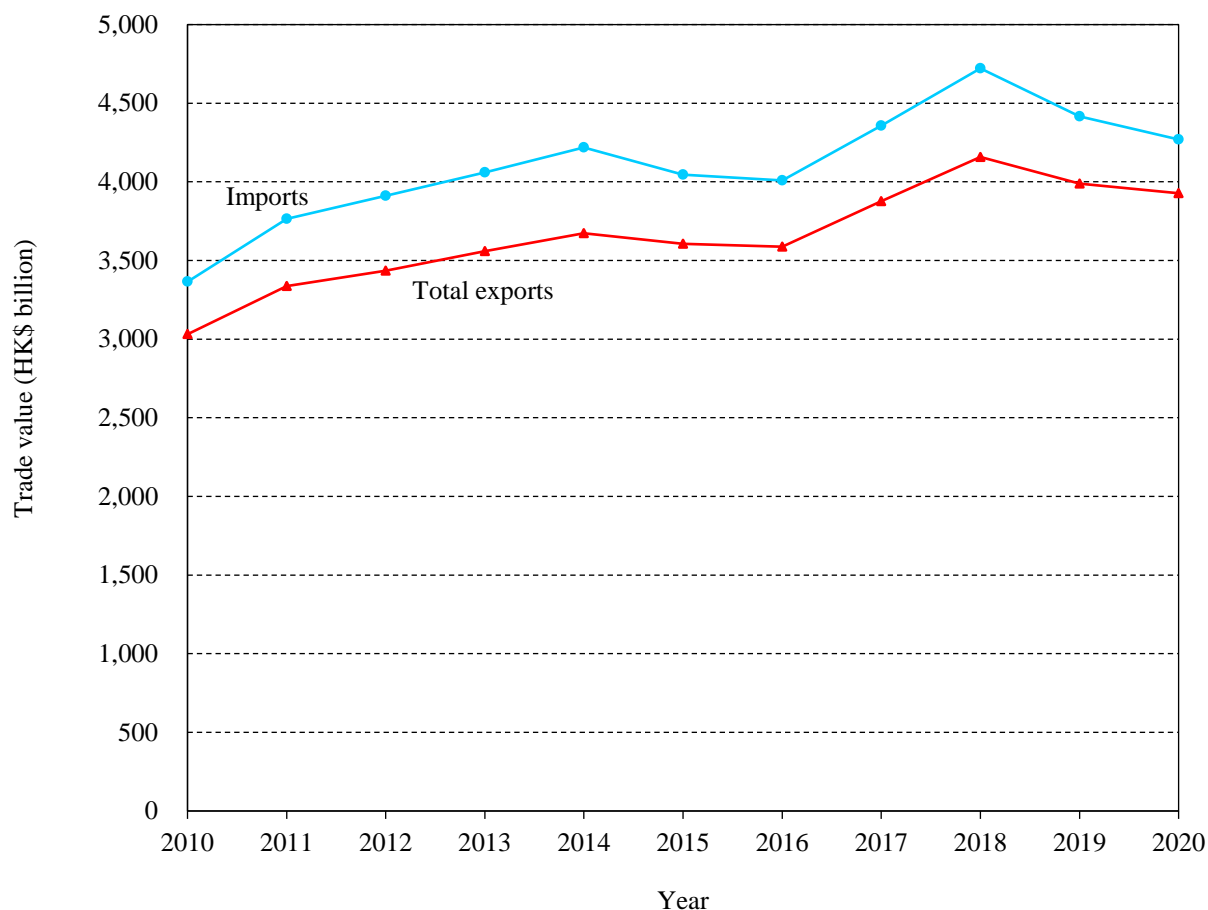
**Chart 6.7 Gross Domestic Product of Hong Kong
(at current market prices), 2010 – 2020**



6 Uses and misuses of statistics

- (2) External trade
- imports and exports of goods
 - trade involving outward processing in the Mainland
 - trade in services
 - offshore trade in goods

Chart 6.8 Values of total exports⁽¹⁵⁾ and imports⁽¹⁶⁾ of goods, 2010 – 2020



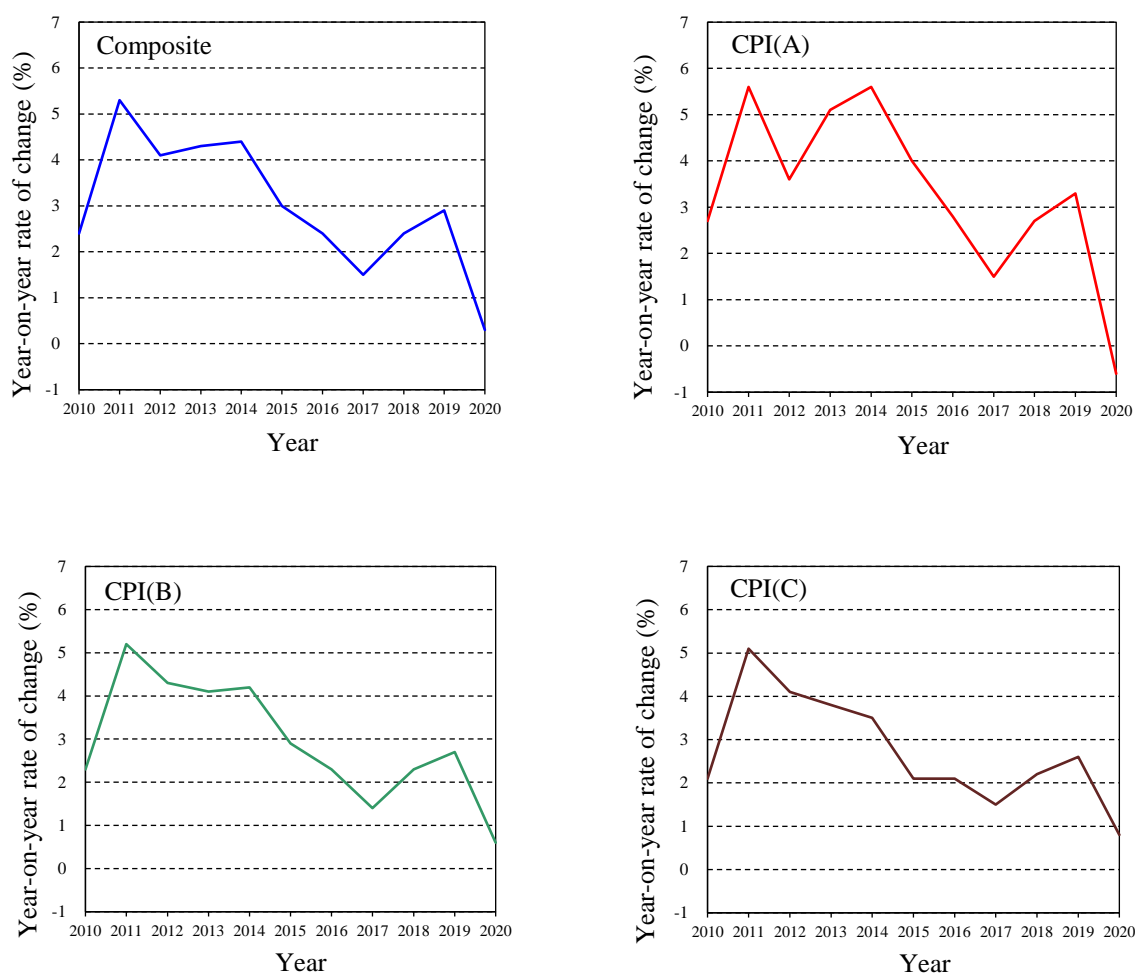
Notes :

- (15) “Total exports” comprise domestic exports and re-exports. Domestic exports are the natural produce of Hong Kong or the products of a manufacturing process in Hong Kong which has changed permanently and substantially the shape, nature, form or utility of the basic materials used in manufacture. Re-exports are products which have previously been imported into Hong Kong and which are re-exported without having undergone in Hong Kong a manufacturing process which has changed permanently and substantially the shape, nature, form or utility of the basic materials used in the manufacture.
- (16) “Imports” are goods which have been produced or manufactured in places outside the jurisdiction of Hong Kong and brought into Hong Kong for local use or for subsequent re-export, as well as Hong Kong products re-imported.

6 Uses and misuses of statistics

- (3) Labour
 - number of persons engaged by industry
 - wages and earnings
- (4) Prices
 - Consumer Price Indices (CPIs)
 - import and export prices
 - wholesale and retail prices

Chart 6.9 Year-on-year rates of change in the Consumer Price Indices⁽¹⁷⁾, 2010 – 2020 (October 2019 – September 2020 = 100)⁽¹⁸⁾



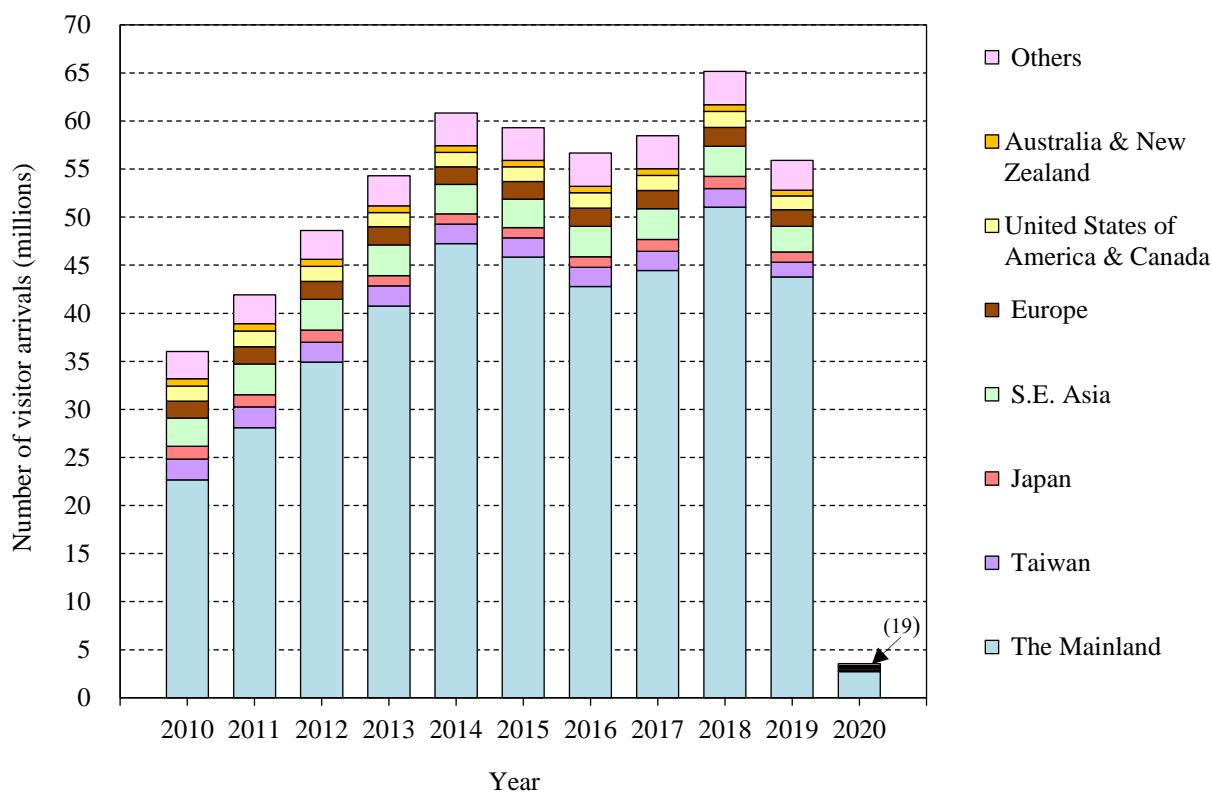
Notes :

- (17) CPIs measure change in the total cost of a given basket of goods and services representative of the purchases made by households in a particular expenditure group in a specified time period. Please see the section on price statistics on pages 89 – 91 for details.
- (18) From October 2020 onwards, the year-on-year rates of change are derived from the 2019/20-based CPIs. The year-on-year rates of change before October 2020 were derived using the index series in the base periods at that time (e.g. the 2014/15-based index series for rates of change for October 2015 to September 2020), compared with the index a year earlier in the same base period.

6 Uses and misuses of statistics

- (5) Operating characteristics and business performance of different economic sectors
- manufacturing
 - electricity and gas supply
 - sewerage, waste management and remediation activities
 - building, construction and real estate
 - import / export, wholesale and retail trades
 - accommodation and food services
 - transportation, storage and courier services
 - information and communications, financing and insurance, professional and business services
- (6) Tourism - visitor arrivals and their spending in Hong Kong

Chart 6.10 Visitor arrivals by country / territory of residence, 2010 – 2020



- (7) Finance
- deposits and loans
 - foreign exchange
 - stock exchange turnover and index of share prices
 - public accounts
 - asset management

Note :

(19) Including Taiwan, Japan, S.E. Asia, Europe, United States of America & Canada, Australia & New Zealand, and Others.

6 Uses and misuses of statistics

Misuses of statistics

Nowadays, the society has become increasingly more scientific-minded. Arguments without the support of relevant figures can hardly convince people. This shows how important statistics are. However, if the data are not properly used, one will make a blunder in trying to be smart. Not only will the arguments be refuted and queried, decision-makers may also be misled to make the wrong decisions, which may cause serious consequences.

To fully understand the proper ways of using statistics, one has to acquire the knowledge through in-depth learning and accumulation of experience. The following are some common mistakes that should be avoided.

Unknown reference periods of statistics

When making statements about comparisons of statistics over time, it is important to specify the reference periods in question. A statement like “the number of students has grown 30%” is not meaningful. It is necessary to specify that the growth has taken place over a certain interval of time, be it 1 year, 5 years or 10 years, etc.

When describing the changes of a series of statistics over time, it is important to specify the base period of comparison.

Example:

What is wrong with the following statements?

1. “CPI in July was 2.8% higher.”
2. “GDP last quarter declined by 0.5%.”

The base period of comparison should be stated clearly:

1. “The **year-on-year growth rate** of CPI in July was 2.8%.” or “CPI in July this year was 2.8% higher than that in July **last year**.”
2. “The **year-on-year growth rate** of GDP in the last quarter was 3.5%, which was lower by half a percentage point when compared with the 4.0% year-on-year growth rate in the quarter earlier.”

6 Uses and misuses of statistics

Improper use of base of comparison

A restaurant claims in its advertisement that its prices will be cut by 100%. It is, of course, clear that prices cannot be cut by 100%, lest the servings would now be given away free of charge! In fact, what the restaurant does is that food formerly sold at \$60 per order will be sold at \$30 after the price deduction. The restaurant has calculated the 100% from $(\$60 - \$30)/\$30 \times 100\%$ by using the reduced price as the base of comparison. This is incorrect. The proper way of calculation is to use the original price as the base. Hence the reduction is only 50%, i.e. $(\$60 - \$30)/\$60 \times 100\%$.

Improper averaging of percentages and ratios

When individual percentages and ratios are calculated on different bases, they should not be added together directly to get the overall average.

Example :

Population figures⁽²⁰⁾ from 2016 Population By-census

<u>Area</u>	<u>Male</u>	<u>Female</u>	<u>Sex ratio</u> (No. of males per 1 000 females)
Hong Kong Island	561 106	692 311	810
Kowloon	1 033 979	1 207 368	856
New Territories	1 779 617	2 061 003	863
Overall	3 374 702	3 960 682	852

It is incorrect to derive the overall sex ratio for Hong Kong by adding the individual ratios for different areas and then dividing by 3. This would give a wrong value of 843 [i.e. $(810+856+863)/3$]. The true value of 852 should be calculated from the total number of males and females [i.e. $(3\,374\,702/3\,960\,682) \times 1\,000$] instead.

Note :

(20) Excluding the marine population.

6 Uses and misuses of statistics

Misinterpretation of changes

Example (1)

John's monthly salary is \$12,000. When we say that his monthly salary is going to be increased by two times next month, what will be his new salary?

The answer is \$36,000, i.e. $(\$12,000 + \$12,000 \times 2)$. However, if his salary is going to be increased to two times instead, then the revised salary will be $\$24,000 = \$12,000 \times 2$.

Example (2)

The sales volume of a company dropped from \$1,000,000 in 2019 to \$500,000 in 2020. Can we say "The sales volume dropped by two times"?

The answer is no. Sales volume cannot drop by two times (200%). It already becomes zero if it drops by one time (100%)! The correct description should be "The sales volume dropped by half or dropped by 50% [i.e. $(\$1,000,000 - \$500,000) / \$1,000,000 \times 100\% = 50\%$]".

Example (3)

One of the two members of a household was sick. Though it is not wrong to say "50% of the members were sick", a statement like this is not meaningful when the base figure is too small.

Take a look at another example. The customer services department of a company could not reply to a complaint according to the scheduled time. It is not meaningful to say that the customer service of the company was bad based solely on the single incident mentioned above, especially if the total number of complaints received by the company in that particular year was only one.

Mis-presentation of data

The same set of statistical data may be presented in different ways to convey quite different impressions to readers. Hence, illusions would easily occur and readers would then be misled if data are not presented properly. Some common examples of mis-presentation of data are discussed below.

6 Uses and misuses of statistics

Illusion in interpreting absolute magnitude of figures

Simply comparing the absolute magnitude of figures but ignoring other relevant factors may create illusion.

Example:

What is wrong with the following analysis?

“According to Table 1, City A had the least number of hospital beds among the three cities.”

Table 1

<u>City</u>	<u>No. of hospital beds</u>
City A	34 000
City B	45 000
City C	83 000

By simply comparing the number of hospital beds as shown in the table, one may think that the provision of hospital beds is most inadequate in City A among the three. However, to avoid illusion created by the numbers, we should use the “rate” (i.e. the ratio of number of beds to population) to compare the availability of hospital beds in different cities (see Table 2).

Table 2

<u>City</u>	<u>No. of hospital beds per 1 000 population</u>
City A	5.0
City B	1.8
City C	1.0

6 Uses and misuses of statistics

Illusion in interpreting small-based figures

Special care should be taken when interpreting figures in comparison of small base to avoid arriving at the wrong conclusion.

Example:

Which government department best fulfills the requests of information enquirers?

Top five government departments that fulfill the requests of information enquirers		
Rank	Department	Percentage of cases that the enquirers' requests were fully entertained
(1)	Department A	100%
(2)	Department B	55.0%
(3)	Department C	52.5%
(4)	Department D	45.8%
(5)	Department E	42.4%

How would you conclude if more information is given?

Top five government departments that fulfill the requests of information enquirers				
Rank	Department	Total no. of cases	No. of cases that the enquirers' requests were fully entertained	Percentage of cases that the enquirers' requests were fully entertained
(1)	Department A	1	1	100%
(2)	Department B	20	11	55.0%
(3)	Department C	40	21	52.5%
(4)	Department D	48	22	45.8%
(5)	Department E	33	14	42.4%

6 Uses and misuses of statistics

Charts using an improper vertical scale

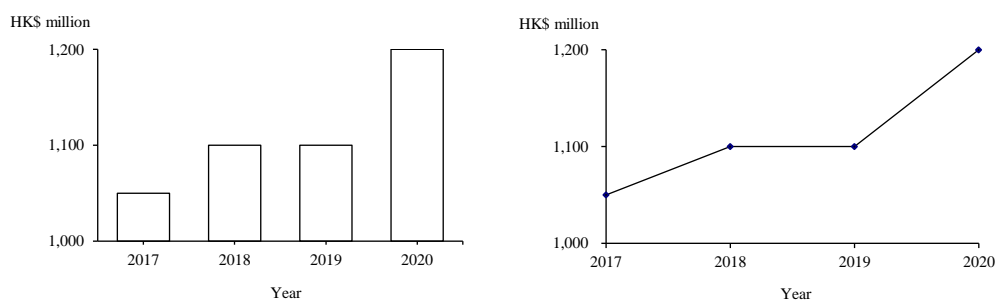
It is essential that charts with an arithmetic scale should begin at the zero base line in order to show the true picture. However, when the data to be presented graphically are of very large values but with small variations, some people would tend to adopt a larger scale and plot the chart from a larger initial point for easy observation and comparison purposes. Watch out for this, as the true relationship between the data for different time points is bound to be exaggerated and a distorted impression will be conveyed. Differences between the data would appear greater, and the slopes indicating the trends seem to be steeper (Chart 6.11(A)).

In order to convey a true picture of the relationship while still highlighting the variations, a broken scale chart is often used (Chart 6.11(B)). It enables the data variations to be observed easily but still reminds readers to watch out for the possible distorted impression that may be conveyed by the chart.

Chart 6.11

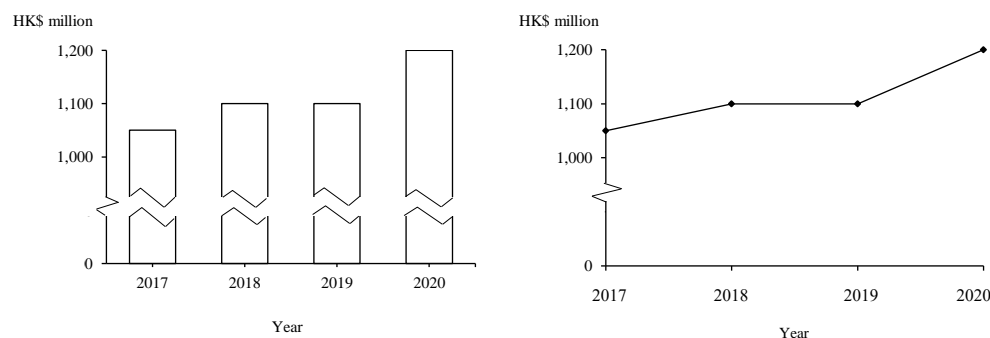
(A) Charts not using the broken scale

Sales turnover of Company ABC, 2017 – 2020



(B) Charts using the broken scale

Sales turnover of Company ABC, 2017 – 2020



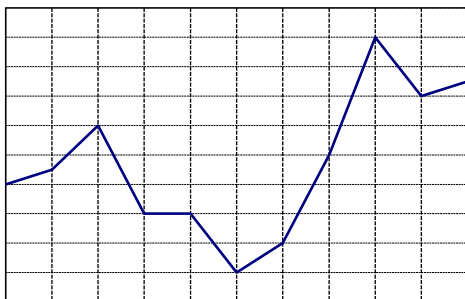
6 Uses and misuses of statistics

Illusions caused by expanding / contracting the grid

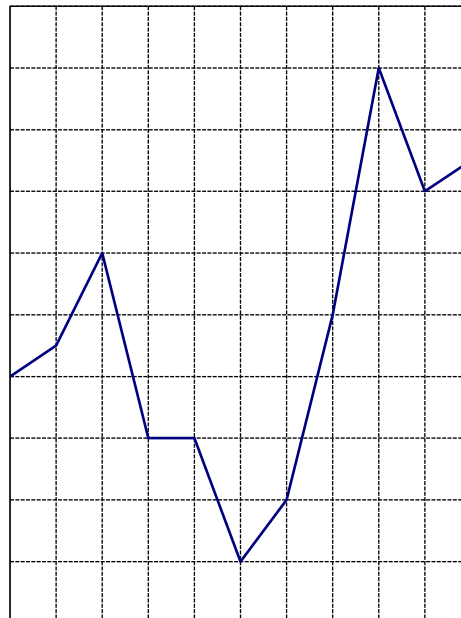
Seemingly, expanding the vertical axis or contracting the horizontal axis of a chart may exaggerate the changes in the trends as depicted in the chart. On the other hand, changes in the trends will appear to be less vigorous than the actual situation if the horizontal axis is expanded or the vertical scale is contracted to a large extent.

Chart 6.12 **Changing the visual image : Contracting or expanding vertical (amount) scale or horizontal (time) scale tends to change the visual picture**

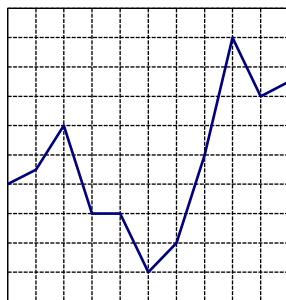
(i) Original scale arrangement



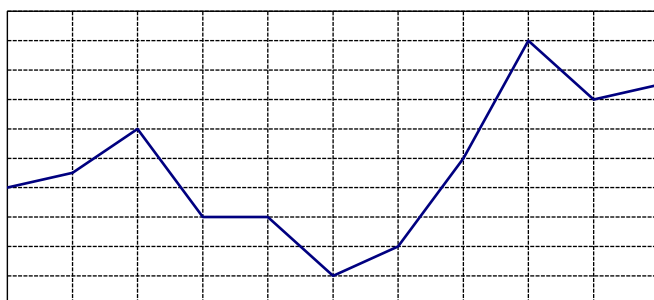
(ii) Expanding vertical scale



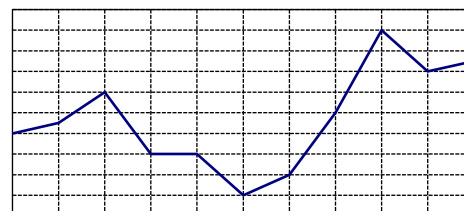
(iii) Contracting horizontal scale



(iv) Expanding horizontal scale



(v) Contracting vertical scale



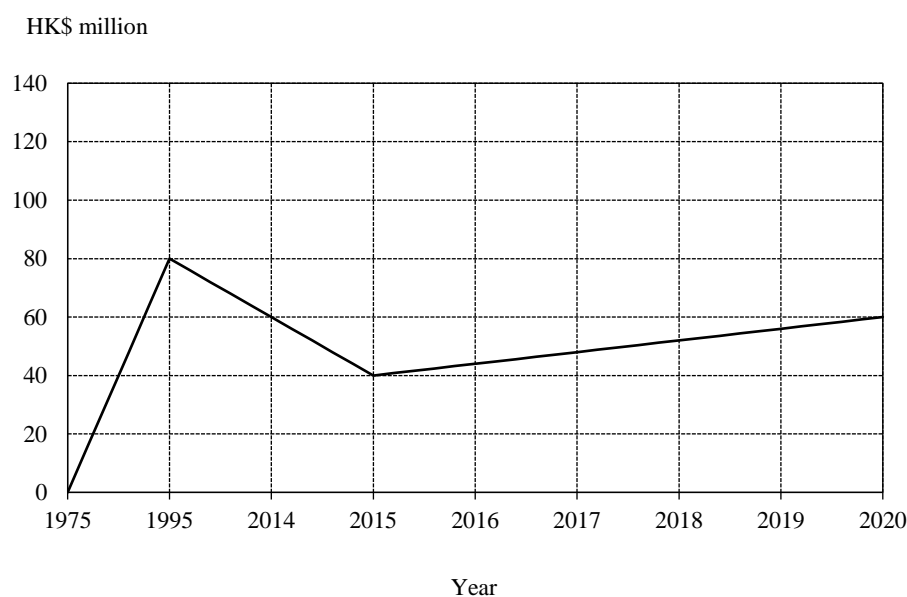
6 Uses and misuses of statistics

Illusions caused by skipping the grid

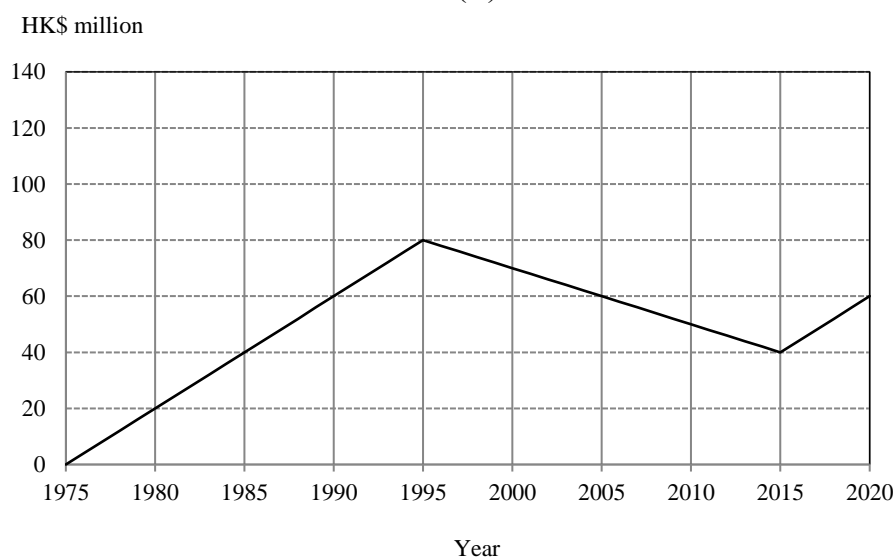
A familiar layout in reports and advertisements is seen in Chart 6.13(A). In order to dramatise the story, a little trick is done with the horizontal (time) scale, so that the period represented by each grid is different. It is not noticeable at a casual glance. Chart 6.13(B) shows what the actual trend looks like when the correct grid spacing is used for the respective years.

Chart 6.13

(A)



(B)



6 Uses and misuses of statistics

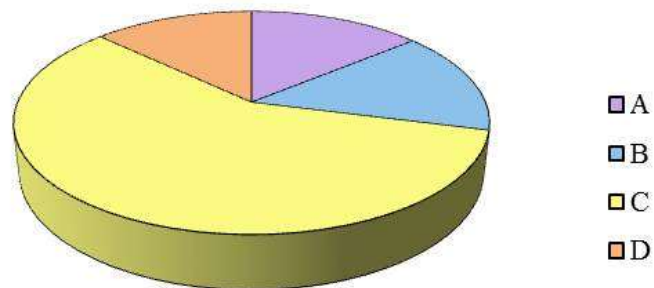
Illusions caused by 3-D charts

Chart 6.14

3-D charts may confuse the readers about the relative size of the portions.

(A)

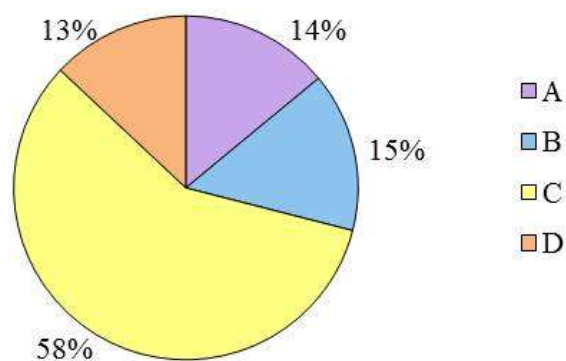
Sales of Company X by Salesperson



2-D charts are clearer and should be used instead.

(B)

Sales of Company X by Salesperson



6 Uses and misuses of statistics

References

Croxton, Frederick E., *Applied General Statistics*, Chapter 1, Prentice-Hall, 1975.

Ilersic, A.R. and Pluck, R.A., *Statistics*, Chapter XVII, XVIII and XIX, HFL Ltd., 1979.

Moroney, M.J., *Facts from Figures*, Penguin Books Ltd., 1965 (3rd edition).

Reichmann, W.J., *Use and Abuse of Statistics*, Penguin Books Ltd., 1964.

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

6 Uses and misuses of statistics

Exercise

Misuse of base figure for comparison

1. Bank Y charges very high interest rates.

A man borrowed \$100,000 from Bank Y for 15 days. He received only \$80,000 in cash. The remaining \$20,000 was deducted as interest for the 15-day period.

Bank Y claimed that the interest rate was 20%
(i.e. $\$20,000 / \$100,000 \times 100\%$) per 15 days. Is this correct?

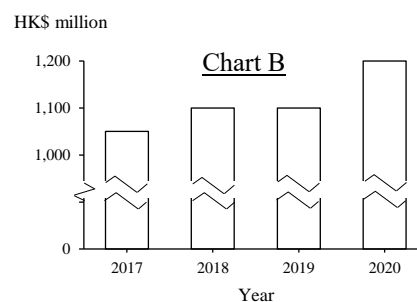
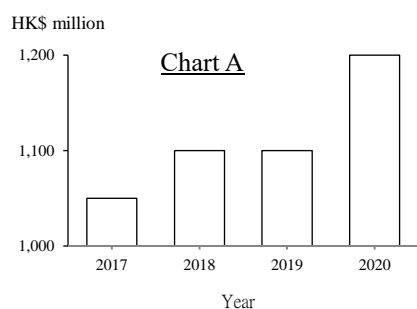
2. The price of an article A was \$100 in 2019 and \$50 in 2020. This means that the price of A in the period has decreased by

- ☐ 50%
- ☐ 100%
- ☐ 150%
- ☐ 200%

Mis-presentation of data

3. Which one of the following charts is visually distorted and should not be used?

- ☐ Chart A
- ☐ Chart B



Misuses of statistics in daily endeavours

4. Readers can collect materials from newspaper cuttings, articles in magazines and commercials on television which may appear to involve misuses of statistics. Readers may then examine various aspects of such examples and analyse whether these are misuses of statistics. Subsequently, readers may make suggestions on how the errors can be rectified, or how the presentation can be improved.

7 Rate, ratio, proportion and percentage



Introduction

Very often, a figure is not meaningful unless it is compared with another figure. For instance, there may be 100 cinemas in a certain city. This may seem to be a large figure. However, when compared with the city's population (say, 10 million), this represents 1 cinema to every 100 000 persons. On the other hand, suppose there are only 10 cinemas in another city. The number may look small, but if the population of the city is only 100 000, each cinema actually serves only 10 000 persons.

Let us look at another example. Suppose there is an increase of 1 000 participants in a certain medical scheme. This may appear to be a remarkable increase. However, if the scheme originally consists of 100 000 participants, the increase is only 1%. On the contrary, an increase of 100 participants in a scheme originally with 500 participants represents a substantial increase of 20%.

“Relative numbers”, which are derived by comparing two related figures⁽¹⁾, are generally more useful than “absolute figures” for data analyses. Rate, ratio, proportion and percentage are examples of some commonly used relative numbers.

Rate

“Rate” is obtained by expressing the measurement of something per unit of something else. The quantities compared are not necessarily of the same kind and hence rate often bears a unit. An example of rate is car speed, say 50 km per hour. Another example is population density, which is calculated by dividing the size of population in a district by the area of the district. The rate of 1 cinema per 100 000 persons mentioned above is also another example describing the degree of availability of movie entertainment facilities.

In the compilation of “rates”, the choice of correct bases is very important, otherwise the results would be misleading. For accurate comparison of “rates”, a base closely related to the target figures to be measured should be used. For example, to calculate the voting rate of a city, the total number of citizens having the right to vote as the base is considered more appropriate than using the total number of citizens in the city as the base.

Note :

- (1) Comparisons are meaningful only when the base figures are not too small. Thus, it would not be meaningful to make a statement that 25% of the members of a household are sick when 1 out of its 4 members falls ill.

With different rates compiled from smaller groups of a population, we often want to get an overall picture for the whole population concerned. However, one should be cautious that individual rates with different bases should not be added together for getting the overall rate.

Ratio

“Ratio” is another way of expressing the relationship between figures. It is normally derived by comparing quantities of the same kind and therefore unlike rate, it does not bear a unit. Sometimes, the relationship is expressed as a ratio to one. For example, the ratio between boys and girls in a class is 3 : 1. However, if it suits our purpose better, we can express the relationship as a ratio to any other number (i.e. other than 1). For the previous example, the ratio between boys and girls can also be written as 30 : 10.

Proportion and percentage

“Proportion” and “percentage” are special types of ratio. “Proportion” relates a “part” to the “whole”; while “percentage” is the case where the relationship between figures is presented as a ratio to one hundred.

Some frequently used relative numbers

Crude death rate

The crude death rate for a given calendar year is obtained by dividing the number of known deaths occurring in a community during that calendar year by the mid-year population of that community, and expressing the result in terms of deaths per 1 000 population.

In 2020, the number of known deaths in Hong Kong was 49 800[#] and the mid-year population was 7 481 800. The crude death rate for 2020 was therefore 6.7[#] per 1 000 population.

Age-sex specific death rate

Mortality varies significantly with age and sex. To study in greater depth the pattern of mortality of people in different age groups and sex, the age-sex specific death rates (or age-sex specific mortality rates) may be referred to. This rate is expressed as the number of known deaths per 1 000 population in the same age group and same sex. For example:

$$\begin{array}{l} \text{Age-sex specific} \\ \text{death rate for males} \\ \text{in the age group 60-64} \end{array} = \frac{\text{Number of known deaths of} \\ \text{males in the age group 60-64}}{\text{Number of males} \\ \text{in the age group 60-64}} \times 1\,000$$

Crude birth rate

Similar to crude death rate, crude birth rate is calculated by dividing the number of known live births during a calendar year by the mid-year population for that year, and expressing the result in terms of births per 1 000 population.

In 2020, the number of known live births in Hong Kong was 43 000 and the mid-year population was 7 481 800. The crude birth rate for 2020 was therefore 5.8 per 1 000 population.

Unemployment rate

The unemployment rate is obtained by dividing the total number of unemployed persons by the labour force in the community. The labour force or economically active population refers to the land-based non-institutional population aged 15 and over who satisfy the criteria for inclusion in the employed population or unemployed population. The unemployment rate of Hong Kong was 5.8% in 2020.

Industrial accident rate in the manufacturing sector

The industrial accident rate in the manufacturing sector is expressed as the number of reported casualties per 1 000 manufacturing workers. The structure of this relative number, with the number of manufacturing workers as the base, highlights the fact that the base figure should relate to the subject matter in question as much as possible. (In this case, manufacturing workers are those “at risk” of industrial accidents and the number of such workers is used as the base.) In 2020, the industrial accident rate in the manufacturing sector in Hong Kong was 12.5 per 1 000 manufacturing workers.

Crime rate

Crime rate is usually expressed as the number of cases of reported crime per 100 000 population. In 2020, the crime rate for Hong Kong was 845 per 100 000 population.

Age specific prosecution rates

To study in greater depth the tendency of committing crimes by people in different age groups, the age specific prosecution rates may be referred to. This rate is usually expressed as the number of persons prosecuted per 100 000 population in the same age group. For example:

$$\begin{array}{l} \text{Age specific} \\ \text{prosecution rate for} \\ \text{the age group 16-20} \end{array} = \frac{\begin{array}{l} \text{Number of persons} \\ \text{in the age group 16-20} \\ \text{who are prosecuted} \end{array}}{\begin{array}{l} \text{Number of persons} \\ \text{in the age group 16-20} \end{array}} \times 100\,000$$

Sex ratio

The relationship of the number of males to the number of females in a population is given by the sex ratio, which presents the number of males per 1 000 females.

As in mid-2020, there were 3 416 300 males and 4 065 500 females in Hong Kong. Thus, the sex ratio was 840 males per 1 000 females.

Proportion of domestic households residing in subsidised home ownership housing

To relate the number of domestic households residing in subsidised home ownership housing⁽²⁾ to the total number of domestic households in Hong Kong, we can obtain the proportion of domestic households residing in subsidised home ownership housing.

The proportion of domestic households residing in subsidised home ownership housing was 14.9% in 2020.

Note :

- (2) Subsidised home ownership housing includes flats built under the Home Ownership Scheme, Middle Income Housing Scheme, Private Sector Participation Scheme, Green Form Subsidised Home Ownership Scheme, Buy or Rent Option Scheme and Mortgage Subsidy Scheme, and flats sold under the Tenants Purchase Scheme of the Hong Kong Housing Authority. It also includes flats built under the Flat for Sale Scheme, Sandwich Class Housing Scheme and Subsidised Sale Flats Projects of the Hong Kong Housing Society; and flats in Urban Renewal Authority Subsidised Sale Flats Scheme. Subsidised sale flats that can be traded in open market are excluded.

Percentage of population by age group

The percentage of population by age group is obtained by dividing the total number of people in a particular age group by the total population size and then multiplying by 100.

As in mid-2020, 11.6% of people in the Hong Kong population were aged under 15, 70.0% aged 15-64 and 18.3% aged 65 and over.

Proper use of relative numbers

Care must be taken when handling or interpreting relative numbers; otherwise we may arrive at incorrect conclusions or mislead other people. The following are two examples to illustrate this.

Example 1 Land-based non-institutional population by District Council district, 2010 and 2020⁽³⁾

<u>District Council district</u>	<u>Land-based non-institutional population</u>			
	<u>2010</u>		<u>2020</u>	
	<u>No.</u>	<u>% of total</u>	<u>No.</u>	<u>% of total</u>
Central and Western	257 000	3.7	236 000	3.2
Wan Chai ⁽⁴⁾	158 100	2.3	173 300	2.3
Eastern ⁽⁴⁾	585 400	8.4	537 900	7.3
Southern	270 600	3.9	260 800	3.5
Yau Tsim Mong	302 800	4.4	323 000	4.4
Sham Shui Po	364 200	5.3	433 500	5.9
Kowloon City	364 200	5.3	419 200	5.7
Wong Tai Sin	414 700	6.0	414 200	5.6
Kwun Tong	606 200	8.7	686 700	9.3
Kwai Tsing	504 500	7.3	500 900	6.8
Tsuen Wan	290 300	4.2	310 000	4.2
Tuen Mun	485 600	7.0	495 000	6.7
Yuen Long	552 500	8.0	640 600	8.7
North	303 800	4.4	314 500	4.3
Tai Po	289 900	4.2	307 900	4.2
Sha Tin	616 600	8.9	684 800	9.3
Sai Kung	421 400	6.1	472 800	6.4
Islands	148 600	2.1	184 700	2.5
Total	6 936 200	100.0	7 395 900	100.0

Notes :

- (3) There may be a slight discrepancy between the sum of individual items and the total due to rounding.
- (4) The boundaries of the Wan Chai district and Eastern district having been adopted since 2016 are different from those adopted in 2015 and earlier years. Therefore, figures of the Wan Chai and Eastern districts for 2016 and thereafter are not strictly comparable with those for 2015 and earlier years in this table.

Comparing the percentage figures for 2010 and 2020, one may notice that the figures for Central and Western, Eastern, Southern, Wong Tai Sin, Kwai Tsing, Tuen Mun and North districts have decreased. For instance, the drops for Eastern and North districts were 1.1 “percentage points⁽⁵⁾” and 0.1 “percentage point” respectively.

One may arrive at a wrong conclusion that these districts have become less populated. In fact, a decrease in the share does not necessarily imply there is a decrease in the actual number. Take the North district as an example. Despite a decrease of 0.1 percentage point in share, the number of land-based non-institutional population of the North district actually increased by 10 700 persons, or 3.5% (i.e. $(314\,500 - 303\,800) / 303\,800 \times 100\%$).

This situation can be attributed mainly to the increase in the total number of land-based non-institutional population over the period. The percentage shares of population in certain districts decreased relatively.

Merely mentioning the drop in the proportion of population, though correct, may not create a right impression for the less statistically-minded people. Referring to both the numbers and the proportions of population will enable the presentation of a more complete and accurate picture.

Note :

- (5) “Percentage point” refers to the absolute sum or difference between two rates or percentages, which is obtained by direct addition or subtraction of the figures concerned. As a matter of fact, an increase of x percentage points and an increase of $x\%$ are not the same. Suppose the passing rates of two different rounds of examination for a class of students were 80% and 84% respectively, the passing rate increased by 4 percentage points ($84\% - 80\% = 4$ percentage points). Alternatively we can also say that the passing rate recorded an increase of 5% (i.e. $(84 - 80)/80 \times 100\%$). However, the second way of presentation is generally not recommended.

7 Rate, ratio, proportion and percentage

Example 2 Registered deaths from external causes of morbidity and mortality in Hong Kong by age group, 2019

<u>Age group</u>	<u>No. of registered deaths</u>		<u>Population at mid-2019</u>	<u>No. of registered deaths per 100 000 persons in the age group</u>
0-14	11	(0.6%)	874 900	1.3
15-49	558	(30.2%)	3 507 900	15.9
50-64	441	(23.9%)	1 802 600	24.5
65 and over	817	(44.2%)	1 322 000	61.8
Total	1 848 ⁽⁶⁾	(100.0%)	7 507 400	

Someone may make such a statement based on the above table: “The majority of people who died of external causes of morbidity and mortality in 2019 was those aged 65 and over (44.2%), followed by those aged 15-49 (30.2%) and 50-64 (23.9%).” This may create a false impression that the death situation in the year for people aged 15-49 was more serious than that for people aged 50-64. Looking at the table more closely, it is observed that the death rate of those aged 15-49 was 15.9 per 100 000 persons. The death rate increased to 24.5 per 100 000 persons for those aged 50-64 and further to 61.8 per 100 000 persons for those aged 65 and over. The death rate for the age group 65 and over was in fact the highest.

It should be noted that the “statement” itself is not wrong. However, the proper way of presenting the situation is to mention the other relevant facts as well so that a more complete picture of the whole situation is provided to enable a clearer understanding of the actual situation.

Reference

Croxtan, Frederick E., *Applied General Statistics*, Chapter 7, Prentice-Hall, 1975.

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

Note :

(6) Including registered deaths of unknown age.

7 Rate, ratio, proportion and percentage

Exercise

Calculating “rate”

Consider the following hypothetical example for studying the passing rate of an open examination :

Broad area / District Council district		Population in 2020	No. of students sitting for the examination in 2020	No. of students passing the examination in 2020
Hong Kong Island	Central and Western	236 000	60 293	44 014
	Wan Chai	173 300	41 110	28 366
	Eastern	537 900	144 528	93 943
	Southern	260 800	63 142	44 831
Kowloon	Yau Tsim Mong	323 000	57 773	36 397
	Wong Tai Sin	414 200	85 917	51 550

New Territories	Sha Tin	684 800	138 281	76 055
	Tai Po	307 900	156 552	60 494

Total		7 395 900	1 403 211	841 927

- Comment on the statement :
“The overall passing rate of the examination in 2020 was 11.4%,
i.e. $(841\,927 / 7\,395\,900) \times 100\%$.”
- Calculate the passing rates for the 4 District Council districts on Hong Kong Island and the overall passing rate for Hong Kong Island.
- Suppose the number of students passing the examination in the Wan Chai district in 2015 was 23 479. Can it be concluded that since there was an increase in the number of students passing the examination (28 366) in 2020, the academic results of students in the Wan Chai district had improved during the period from 2015 to 2020?

8 Measures of central tendency



Introduction

Given a set of data, it is often required to describe them in terms of a single value around which the data are distributed. This value is a measure of “central tendency”, indicating the central position of the given set of data.

There are different choices for the measurement of central tendency. The most common ones are arithmetic mean (or briefly “the mean”), median and mode. These measures of central tendency are applied in different situations depending on the nature of data and the intended purpose.

Mean

The arithmetic mean of a set of data is defined as the sum of the values of the given set of data divided by the number of data points.

$$\bar{X} = \frac{X_1 + X_2 + \dots + X_N}{N}$$

where \bar{X} is the mean;
 N is the total number of data points; and
 X_i is the value of the i^{th} data point, for $i = 1, 2, \dots, N$

Examples :

- (1) The mean height of the students in a class is 1.52 m.
- (2) The mean daily maximum air temperature for the year 2020 was 27.2°C. (The method is to find out the maximum air temperature recorded for each of the 366 days in the year 2020 and then calculate the arithmetic mean of the 366 data points.)

8 Measures of central tendency

Median

The median of a set of data is the middle value of the given set of data when they are arranged in order, either ascending or descending, of magnitude. In case there are two middle values (i.e. when the data set has an even number of data points), then the median is the arithmetic mean of these two middle values.

Examples :

- (1) The median of the set of numbers $\{4, 6, 7, 9, 10\}$ is 7.
- (2) The median of the set of numbers $\{1, 3, 4, 4, 7, 9, 10, 11, 13, 14\}$ is $(7+9)/2$, i.e. 8.
- (3) The median monthly household income of domestic households in Hong Kong in 2020 was \$27,000. In other words, 50% of the domestic households in Hong Kong had a household income more than \$27,000 per month in 2020 while the other 50% had less than \$27,000 per month.
- (4) The median age of men who married for the first time in Hong Kong in 2020 was 31.9.

Mode

The mode of a set of data is the value which occurs with the largest frequency, i.e. the most common value in the given set of data. The mode may not exist, and even if it does exist, it may not be unique.

Examples :

- (1) The set of numbers $\{1, 3, 3, 5, 7, 8, 8, 8, 9, 10, 10, 11, 12\}$ has a mode of 8.
- (2) The set of numbers $\{2, 3, 4, 6, 8, 9\}$ does not have any mode.
- (3) The set of numbers $\{1, 3, 4, 4, 4, 6, 7, 7, 9, 9, 9, 10, 12\}$ has two modes, 4 and 9.
- (4) The modal household size in Hong Kong was 2 in 2020.

8 Measures of central tendency

Grouped data

When presenting a large set of data, it is often useful to classify the data into different classes and to find out the number of data points belonging to each class (i.e. the class frequency). Data organised in this way are called grouped data whereas a tabular arrangement of the data by class showing the corresponding class frequency is called a frequency distribution or frequency table.

Example :

The weights (in kg) of individual students in a class are as follows :

61, 62, 63, 63, 63, 64, 64, 64, 64, 65, 65, 65, 66, 66, 66,
66, 66, 67, 67, 67, 67, 68, 68, 68, 69, 69, 69, 69, 70, 70

To help give a clear overall picture of the weights of the students, the above 30 data points can be re-organised into several classes and a frequency distribution can be constructed.

Step 1 Determine the largest and smallest values in the data set and find the range (i.e. the difference between the largest and smallest values).

Smallest value = 61

Largest value = 70

Range = 9 (i.e. $70 - 61$)

Step 2 Divide the range into a convenient number of classes having the same size (i.e. same class interval⁽¹⁾). The number of classes usually ranges from 5 to 20, depending on the values of the data.

Given that there are only 30 data points in the data set, it is not appropriate to divide the range into a large number of classes (otherwise there will be too few observations in each class). In this example, it is sensible to divide the data set into 5 classes. The class intervals to be used are thus :

61-62;

63-64;

65-66;

67-68; and

69-70

Note :

(1) The smaller value of each class interval shown above is called the lower class limit and the larger value the upper class limit. The mid-point of the class interval is known as the class mark.

8 Measures of central tendency

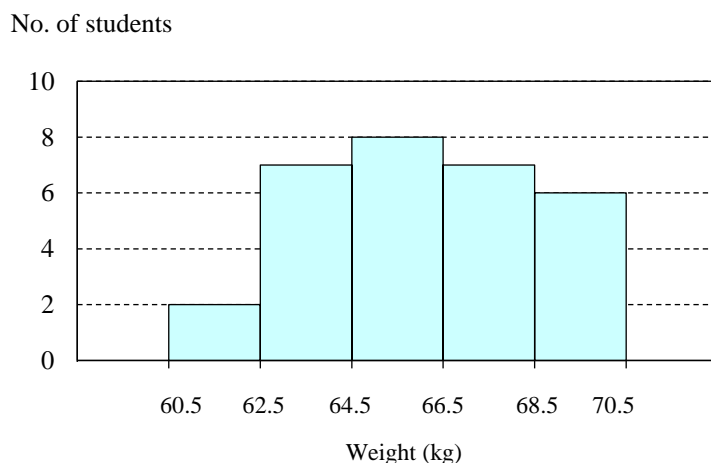
Step 3 Find the class frequency for each class and then construct the frequency distribution.

Weight ⁽²⁾ (kg)	Number of students
61-62	2
63-64	7
65-66	8
67-68	7
69-70	6
Total	30

Histogram

A histogram is a bar chart, with no space between the bars. It is commonly used for presenting frequency distributions of grouped data with continuous class boundaries, with class boundaries shown as points on the horizontal axis and the frequencies as units on the vertical axis. The frequency in a class is proportional to the area of a bar with the base as the class interval. (Please see Chart 8.1 below which is a histogram for the grouped data of the example mentioned above.)

Chart 8.1 Histogram of the number of students



The population pyramid may be visualised as being formed from two horizontally placed histograms, one being the age distribution of males and the other being the age distribution of females.

Note :

- (2) If the weights are rounded to the nearest kg, the class interval, say, 61 kg-62 kg, theoretically includes all measurements from 60.5000...kg to 62.4999...kg. These two class limits, indicated briefly by the exact numbers 60.5 kg and 62.5 kg, are called true class limits or class boundaries.

8 Measures of central tendency

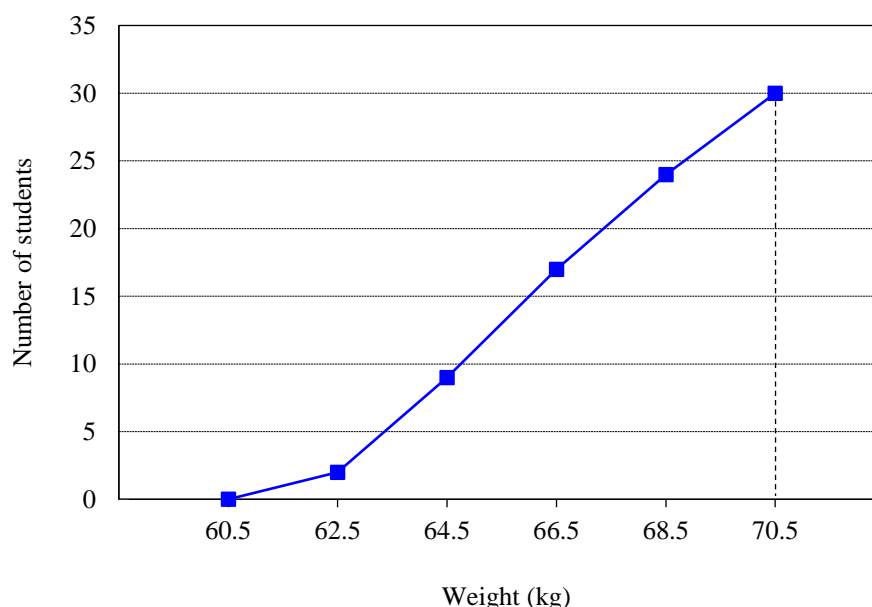
Cumulative frequency polygon

For some purposes, it is desirable to consider the total frequency of all values greater than the lower class boundary of each class (i.e. the “more than” basis for counting total frequency) or the total frequency of all values less than or equal to the upper class boundary of each class (i.e. the “less than” basis for counting total frequency). In such circumstances, it is necessary to construct the cumulative distribution (in tabular form) or the cumulative frequency polygon (in graphical form).

To construct a cumulative frequency polygon, frequencies accumulated for each class are plotted at the lower class limits when the “more than” basis is used. When the “less than” basis is used, cumulated frequencies are plotted at the upper class limits.

Regardless of the basis used, the Y-axis should be drawn long enough to accommodate the total frequency. The points, each representing the cumulative frequency of a particular class, are then joined by a series of straight lines and the S-curve so obtained may be extended to touch the X-axis by dropping a perpendicular line from its highest point. The polygon so formed is a cumulative frequency polygon. (Please see Chart 8.2 below which is a cumulative frequency polygon for the grouped data of the example mentioned above.)

Chart 8.2 Cumulative frequency polygon of the number of students



The cumulative frequency polygon is particularly useful for interpolation. However, it is important to note that the use of straight lines to connect the series of known points is only an approximation to the frequency distribution of the items within any given interval. Nevertheless, this approximation is considered to be sufficiently accurate under most circumstances.

8 Measures of central tendency

Mean of grouped data

The formula to be used to calculate the mean of a set of grouped data is as follows:

$$\bar{X} = \frac{f_1 X_1 + f_2 X_2 + \dots + f_k X_k}{f_1 + f_2 + \dots + f_k}$$

where \bar{X} is the mean;
 X_i is the class mark (i.e. mid-point of the class interval) of the i^{th} class,
for $i = 1, 2, \dots, k$; and
 f_i is the frequency of the i^{th} class, for $i = 1, 2, \dots, k$

The mean thus obtained depends on the way the data are grouped and is only an approximation. However, it reduces the burden of numerical calculation.

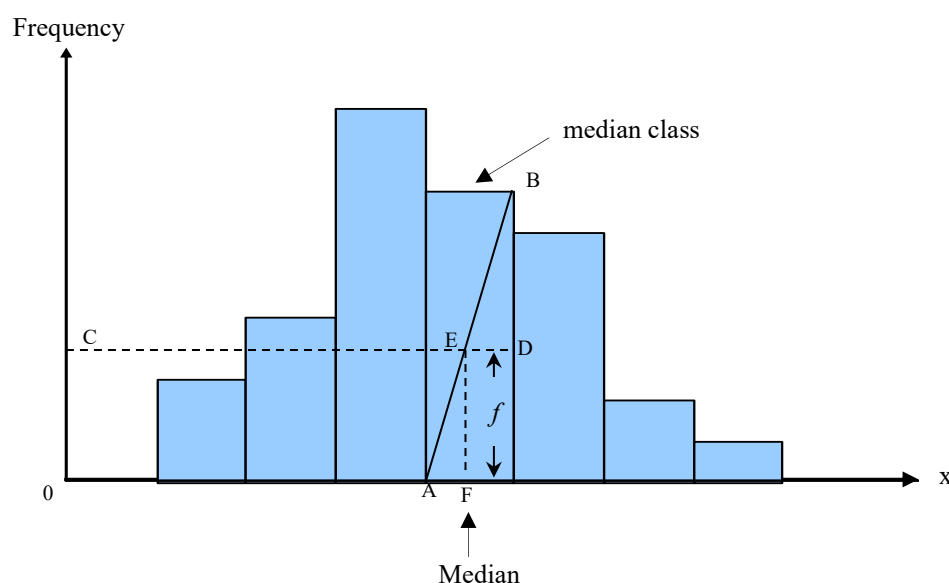
8 Measures of central tendency

Finding the median of grouped data from histogram

Making use of the histogram, an approximation of the median of a set of grouped data can be found.

- Step 1 Construct the histogram for the data set (please see Chart 8.3 below).
- Step 2 Identify the median class, i.e. the class which contains the “middle value”.
- Step 3 Calculate the sum of frequencies of classes lower than the median class, $(\sum f)_l$.
- Step 4 Find f , using the expression $f = N/2 - (\sum f)_l$
where N is the total frequency; and
 $(\sum f)_l$ is the sum of frequencies of classes lower than the median class
- Step 5 Construct a diagonal in the median class. The line should be drawn from the lower left corner to the upper right corner (AB).
- Step 6 At the height corresponding to “ f ” found in step 4, draw a horizontal line (CD) to cut the median class. The line will intersect with the diagonal (E).
- Step 7 Drop a perpendicular line from this point of intersection (E) to the X-axis. The point thus located on the X-axis (F) will give the value of the median.

Chart 8.3



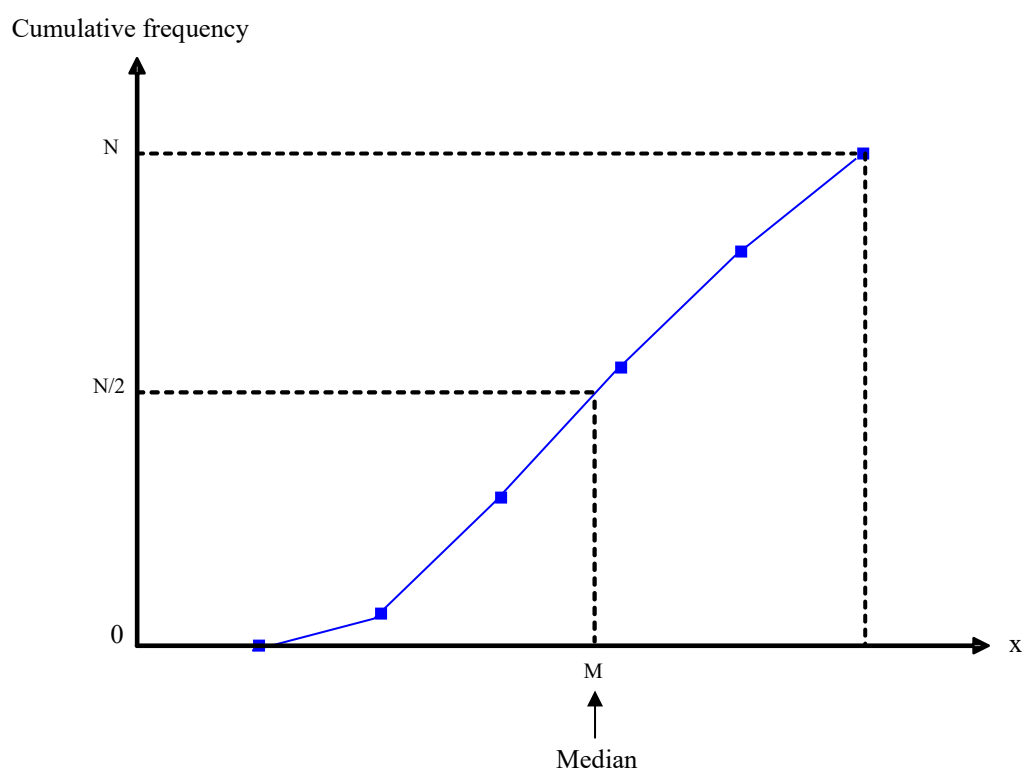
8 Measures of central tendency

Finding the median of grouped data from cumulative frequency polygon

Another graphical method of finding the median is to draw a cumulative frequency polygon.

- Step 1 Construct the cumulative frequency polygon for the data set (please see Chart 8.4 below).
- Step 2 At the cumulative frequency height $N/2$ (N is the number of data points), draw a horizontal line until it touches the cumulative frequency polygon.
- Step 3 Draw a perpendicular line from this point of intersection to the X-axis. The point thus located on the X-axis (M) will give the value of the median.

Chart 8.4



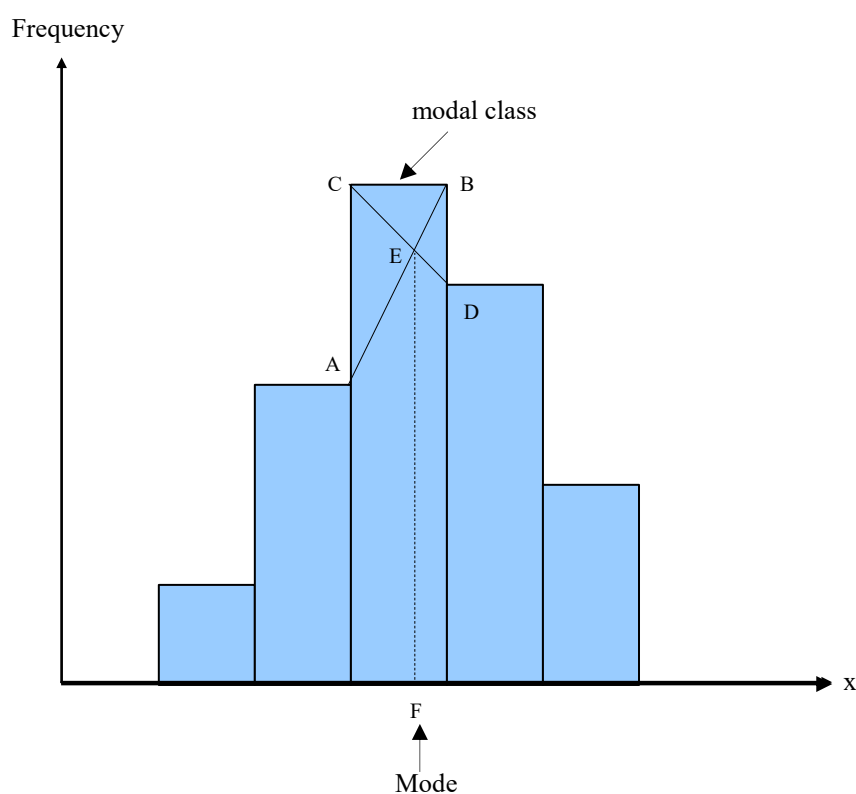
8 Measures of central tendency

Finding the mode of grouped data from histogram

A rough estimate of the mode can also be found with the use of the histogram.

- Step 1 Construct a histogram for the data set (please see Chart 8.5 below).
- Step 2 Identify the modal class, i.e. the class with the largest frequency.
- Step 3 Draw 2 diagonals as shown in Chart 8.5 (AB and CD).
- Step 4 Drop a vertical line from the point of intersection of these 2 diagonals (E) to the X-axis. The point thus located on the X-axis (F) will give the value of the mode.

Chart 8.5



8 Measures of central tendency

Use of mean and median

The mean is the most widely used among all the measures of central tendency, because it has a lot of desirable properties in statistical theories.

For an approximately symmetric set of data such as $\{13, 14, 15, 17, 18.5\}$, the mean 15.5 gives the central location effectively.

The mean, however, is affected by the value of every item in the set of data, and the presence of a few extremely large (or extremely small) items may result in a mean which could be misleading. For example, for the data set $\{1\ 000, 2\ 000, 3\ 000, 3\ 500, 4\ 500, 5\ 000, 30\ 000\}$, the mean is 7 000 which is not a good measure of the central tendency. However, the median, 3 500, is more satisfactory because the existence of a few extreme values generally would not cause the median to fluctuate much.

In daily life, the mean monthly household income is easily affected by extreme values. Hence, the median is more suitable than the mean in measuring the central tendency of household income. In 2020, the median monthly household income of domestic households in Hong Kong was \$27,000.

Supplementary notes - weighted mean

Sometimes, we associate the data (X_1, X_2, \dots, X_k) with certain weighting factors or weights (W_1, W_2, \dots, W_k) , depending on the significance or importance attached to the individual data points. In this case,

$$\bar{X} = \frac{W_1 X_1 + W_2 X_2 + \dots + W_k X_k}{W_1 + W_2 + \dots + W_k}$$

The mean of a set of grouped data is in fact a mean of the class marks weighted by the class frequencies.

Normally, the use of the weighted mean leads to a different conclusion from that using the unweighted mean. In fact, the concept of weighted mean is commonly used in daily life.

8 Measures of central tendency

Example :

The following is a summary of the grade points of the final examination and the mid-term test scored by two students A and B, with the final examination grades weighted 3 times as much as the mid-term test grades :

	Grade points		Weights
	A	B	
Final examination	82	90	3
Mid-term test	78	66	1

If the weights are disregarded,

the mean score of A $= \frac{82 + 78}{2} = \underline{80}$, and

the mean score of B $= \frac{90 + 66}{2} = \underline{78}$.

We would say that A did better than B.

On the other hand, if the weights are taken into consideration,

the weighted mean score of A $= \frac{82 \times 3 + 78 \times 1}{3 + 1} = \underline{81}$,

and

the weighted mean score of B $= \frac{90 \times 3 + 66 \times 1}{3 + 1} = \underline{84}$.

We would then say that B did better than A.

8 Measures of central tendency

References

Croxtan, Frederick E., *Applied General Statistics*, Chapter 9, Prentice-Hall, 1975.

Spiegel, Murray R., *Theory and Problems of Statistics*, Chapter 3, Schaum Publishing Co., 1961.

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

8 Measures of central tendency

Exercise

Calculating mean, median and mode

1. Consider a set of figures :

$\{ 1, 9, 3, 7, 8, 12, 9 \}$

- (i) What is the sum of these seven values?
- (ii) What is the mean?
- (iii) What is the median?
- (iv) What is the mode?
- (v) Is the median equal to the mean of the same seven values?
- (vi) Are the mean and median the same when the set of figures is $\{ 1, 3, 7, 11, 13 \}$?
- (vii) When the mean and median of a set of data are the same, what does this suggest?

2. The mean of $\{ 10, 20, 30, 40, 50 \}$ is

- ☐ 30
- ☐ 35
- ☐ 40
- ☐ 45

3. The mode of $\{ 3, 10, 14, 23, 29, 30, 31 \}$ is

- ☐ 20
- ☐ 23
- ☐ 31
- ☐ Mode does not exist in this set of figures

8 Measures of central tendency

4. When half of the elements of a population are smaller than a value X and half are greater than it, X is the
- ☐ Mean
 - ☐ Median
 - ☐ Mode
5. Among mean, median and mode, which one is the most easily affected by extreme values?
- ☐ Mean
 - ☐ Median
 - ☐ Mode

9 Measures of dispersion



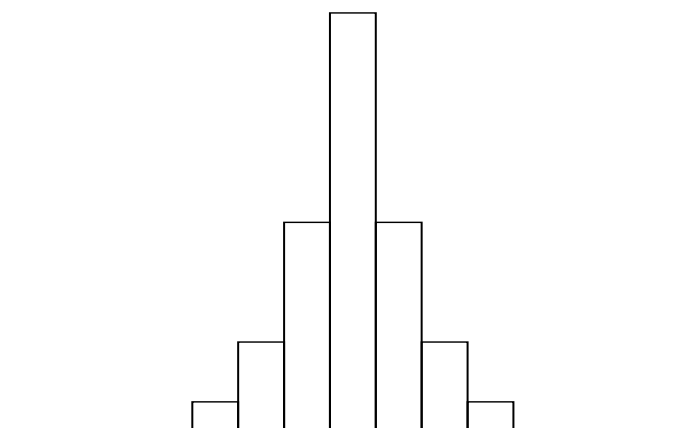
Introduction

Information on the central tendency of a set of data alone is not sufficient to describe its distribution. For instance, two groups of data may have the same mean, yet having different degrees of spread among the data points. To have a better knowledge of a set of data, it is necessary to measure the extent to which individual values vary within the set, or equivalently, the extent to which individual values vary around the mean.

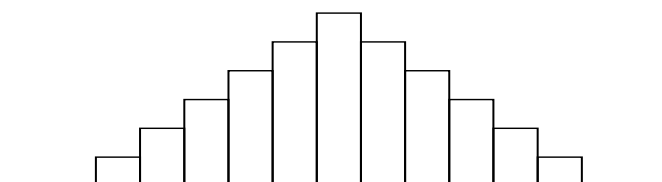
The degree to which numerical data tend to spread around the mean value is called the dispersion of the data. Various measures of dispersion are available. The more common ones are range, mean deviation, variance and standard deviation.

Chart 9.1 **Various degrees of variation**

Small variation



Large variation



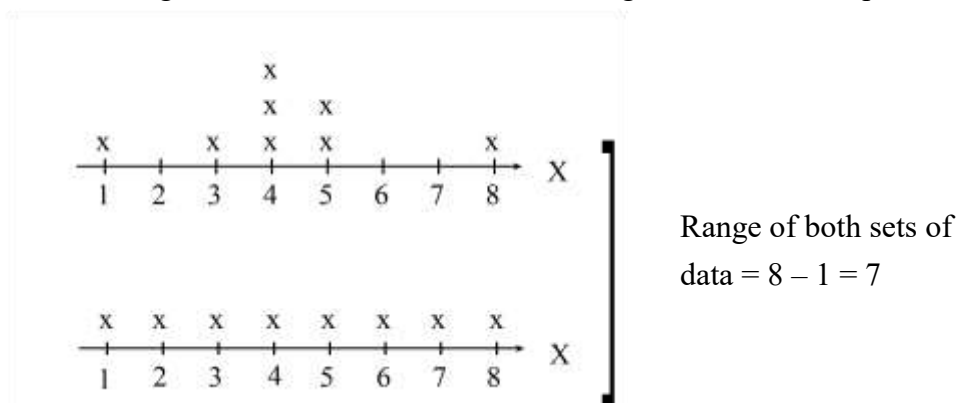
9 Measures of dispersion

Range

The range of a set of numbers is the difference between the maximum and the minimum values. This measure is greatly affected by extreme values. The advantage of this measure is simplicity. The disadvantage is that it does not take the intermediate values into account at all.

Chart 9.2 Range

The following two sets of data have the same range but different dispersions:



Mean deviation (Mean absolute deviation)

Mean deviation, also known as mean absolute deviation, is a measure summarising how large the extent a data set deviates from its mean, irrespective of the direction of spread of individual data points in the set. For a given set of numerical data, the mean deviation is defined as the sum of the absolute deviations (i.e. the absolute values of the deviations from the mean) of individual data points divided by the total number of data points.

$$md = \frac{|X_1 - \bar{X}| + |X_2 - \bar{X}| + \dots + |X_N - \bar{X}|}{N}$$

$$= \frac{\sum_{i=1}^N |X_i - \bar{X}|}{N}$$

where md is the mean deviation;
 \bar{X} is the mean;
 N is the total number of data points;
 X_i is the value of the i^{th} data point, for $i = 1, 2, \dots, N$; and
 $|X_i - \bar{X}|$ is the absolute value of the deviation from the mean of the i^{th} data point, for $i = 1, 2, \dots, N$

9 Measures of dispersion

For example, considering a set of data $\{13, 3, 5, 1, 8\}$ which has a mean of 6. By subtracting the mean from each of the data points in the set, the deviations⁽¹⁾ from the mean can be found, which are 7, -3, -1, -5 and 2 respectively.

The mean deviation of the set of data can then be computed by finding the simple average of the absolute deviations:

$$\frac{7 + 3 + 1 + 5 + 2}{5} = \underline{\underline{3.6}}$$

This tells that the data points within the given set lie on average 3.6 units from their mean of 6.

From the above example, it can be seen that if we simply add up individual deviations, a zero sum will be obtained despite the dispersion of the data points around the mean. This is because the negative deviations will balance the positive deviations. To avoid such problem, the absolute values of the deviations, or absolute deviations, are used in the computation of the mean deviation. With the negative signs of those negative deviations removed, only the “distances” but not the “directions” in which individual data points spread away from the mean are indeed considered.

Another point worth noting is that the sum of absolute deviations is highly sensitive to the total number of data points in the given set of data. For two sets of data with same degree of dispersion, the set which has more data points is bound to have a greater sum of absolute deviations. To enable comparisons of data sets of different sizes to be made, it is essential to discount the size effect by dividing the sum of absolute deviations by the total number of data points.

Note :

- (1) Some of the deviations derived are negative. This shows that the values of the data points concerned are smaller than the mean. Conversely, the deviations will be positive when the data points have a value larger than the mean.

9 Measures of dispersion

Variance

The average of the squared deviations from the mean is called the variance.

$$\begin{aligned}\sigma^2 &= \frac{(X_1 - \bar{X})^2 + (X_2 - \bar{X})^2 + \cdots + (X_N - \bar{X})^2}{N} \\ &= \frac{\sum_{i=1}^N (X_i - \bar{X})^2}{N}\end{aligned}$$

where σ^2 is the variance;
 \bar{X} is the mean;
 N is the total number of data points;
 X_i is the value of the i^{th} data point, for $i = 1, 2, \dots, N$; and
 $(X_i - \bar{X})^2$ is the squared deviations from the mean of the i^{th} data point, for $i = 1, 2, \dots, N$

In our example above, the variance of the data set is 17.6

(i.e. $\frac{7^2 + (-3)^2 + (-1)^2 + (-5)^2 + 2^2}{5}$).

This is another way of measuring the size of the deviations irrespective of their signs, since squares of positive and negative numbers are all positive.

9 Measures of dispersion

Standard deviation

The variance measures the scatter of the data points from their mean, but it is expressed in “squared units”. To return it to the original unit of measurement, one takes the square root of the variance. This gives a measure known as standard deviation.

$$\begin{aligned}\sigma &= \sqrt{\frac{(X_1 - \bar{X})^2 + (X_2 - \bar{X})^2 + \cdots + (X_N - \bar{X})^2}{N}} \\ &= \sqrt{\frac{\sum_{i=1}^N (X_i - \bar{X})^2}{N}}\end{aligned}$$

where σ	is the standard deviation;
\bar{X}	is the mean;
N	is the total number of data points;
X_i	is the value of the i^{th} data point, for $i = 1, 2, \dots, N$; and
$(X_i - \bar{X})^2$	is the squared deviations from the mean of the i^{th} data point, for $i = 1, 2, \dots, N$

In our example above, the standard deviation of the data set is 4.2 (i.e. $\sqrt{17.6}$).

Both variance and standard deviation are commonly used measures of the spread of data, as they can be used for other more sophisticated statistical calculations.

In general, for two sets of data with equal (or more or less similar) values of mean, the set with a higher variance and standard deviation has a distribution with bigger dispersion.

Application of some measures of dispersion

Example 1 : Standard scores (Z)

$$Z = \frac{X_i - \bar{X}}{\sigma}$$

The standard score is a transformation of raw scores for comparison purposes. It is commonly used in examinations for assessing a student's ranking among a group of students.

Consider the marks in Mathematics and English of a class with ten students :

Student	<u>Scores</u>	
	<u>Mathematics</u>	<u>English</u>
(1)	95	60
(2)	90	50
(3)	80	55
(4)	87	69
(5)	79	61
(6)	55	68
(7)	70	70
(8)	97	59
(9)	75	71
(10)	55	72

Student (4) scores 87 in Mathematics and 69 in English. In order to understand this student's ranking among his / her fellow classmates, we can separately calculate his / her standard scores in the two subjects.

	<u>Mathematics</u>	<u>English</u>
Class mean (\bar{X})	78.3	63.5
Class standard deviation (σ)	14.2	7.2
Student (4)'s standard score (Z)	$\frac{87 - 78.3}{14.2}$ $= \underline{0.61}$	$\frac{69 - 63.5}{7.2}$ $= \underline{0.76}$

Comparing his / her original score in each subject with the respective class mean score, we may already observe that he / she is doing better than the average in both subjects. If supplemented by the standard scores, we may further observe that he / she stands relatively better in English (better than the mean score by 0.76 standard deviation) among his / her classmates than he / she does in regard to Mathematics (only better than the mean score by 0.61 standard deviation).

Example 2 : Standard deviation as an indication of precision

Two balances, A and B, are used for measuring the weight of a piece of baggage of about 100 kg, each for 20 times.

There may be the thinking that a balance should always give the same reading in respect of the weight of the baggage no matter how many times weighing is done. In fact, this is not the case in reality as illustrated by the experiment below :

<u>Balance measurement</u>	<u>Balance readings (kg)</u>	
	<u>Balance A</u>	<u>Balance B</u>
1	100.3	100.3
2	100.3	100.2
3	100.0	99.7
4	99.8	100.1
5	99.7	99.8
6	100.3	100.2
7	100.1	100.2
8	99.6	99.9
9	100.2	100.4
10	100.3	100.3
11	100.2	100.0
12	99.6	100.3
13	100.4	100.2
14	99.6	99.8
15	99.7	99.9
16	100.3	100.1
17	100.0	100.4
18	99.6	100.1
19	100.4	100.2
20	99.6	99.9
Mean	100.0	100.1
Standard deviation	0.3	0.2

Balance A gives a standard deviation of 0.3 kg while Balance B gives a standard deviation of 0.2 kg. Which balance is more “precise”?

The answer is Balance B because its measurements have a smaller standard deviation. *(It should, however, be noted that we are actually not sure whether Balance B or Balance A measures weight more accurately (i.e. we do not know whether the weight of the baggage is actually closer to 100.0 kg or 100.1 kg).)*

9 Measures of dispersion

References

A.S.C. Ehrenberg, *A Primer in Data Reduction*, Chapter 2, John Wiley & Sons Ltd., 1982.

Croxtan, Frederick E., *Applied General Statistics*, P. 189-198, Prentice-Hall, 1975.

Spiegel, Murray R and Stephens, Larry J., *Schaum's outline of Theory and Problems of Statistics*, Chapter 4, Schaum Publishing Co., 2008.

The English Universities Press Limited, *Introduction to Management Statistics*, 1967.

Interactive quiz

You may test the knowledge you have learnt in this Chapter by trying this [interactive quiz](#). Answers to the questions can be found in the relevant paragraphs of this Chapter.

9 Measures of dispersion

Exercise

Measures of dispersion

1. The mean deviation of $\{2, 5, 13, 28\}$ is
- ☐ 0
 - ☐ 8.5
 - ☐ 12
 - ☐ 34

Application of standard score

2. The following are the examination marks of a class of ten students. Comparing their total standard scores, which student in the class would you consider to have attained the best overall result?

Examination scores

<u>Student</u>	<u>English</u>	<u>Chinese</u>	<u>Mathematics</u>
(1)	40	62	80
(2)	57	60	60
(3)	60	70	95
(4)	48	64	92
(5)	53	66	75
(6)	66	72	78
(7)	72	70	86
(8)	49	67	87
(9)	69	60	99
(10)	70	74	83

Student	Examination scores			Standard examination scores			
	English	Chinese	Mathematics	English	Chinese	Mathematics	Total
(1)	40	62	80				
(2)	57	60	60				
(3)	60	70	95				
(4)	48	64	92				
(5)	53	66	75				
(6)	66	72	78				
(7)	72	70	86				
(8)	49	67	87				
(9)	69	60	99				
(10)	70	74	83				
Mean							
Standard deviation							

The student in the class who has attained the best overall result is _____.

Solutions to exercises

Chapter 1 Population size and growth

- (1) From the data given below, complete the table.
(Figures given in thousands; rates expressed in “per 1 000 population”).)

Country	Mid-year population at year T	No. of births in year T	No. of deaths in year T	Crude birth rate	Crude death rate	Rate of natural increase
Country A	29 863	1 322	525	44.3	17.6	26.7
Country B	15 941	723	332	45.4	20.8	24.5
Country C	20 155	249	132	12.4	6.5	5.8
Country D	32 268	332	226	10.3	7.0	3.3
Country E	9 749	433	181	44.4	18.6	25.8
Country F	1 315 844	17 558	8 795	13.3	6.7	6.7
Country G	74 033	1 860	421	25.1	5.7	19.4
Country H	1 517	51	17	33.6	11.2	22.4
Country I	82 689	702	853	8.5	10.3	-1.8
Country J	10 098	96	132	9.5	13.1	-3.6

- (2) From the rates obtained in part (1), classify the countries into various stages of the demographic transition model.

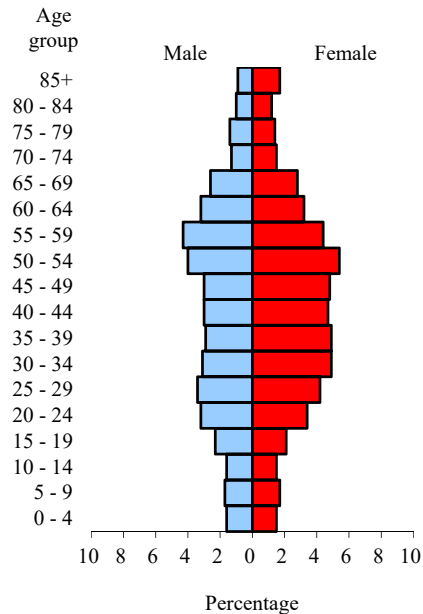
Stage (1) (High birth and death rates)	Stage (4) (Low birth and death rates)
<i>Country A</i>	<i>Country C</i>
<i>Country B</i>	<i>Country D</i>
<i>Country E</i>	<i>Country F</i>
	<i>Country I</i>
	<i>Country J</i>

Solutions to exercises

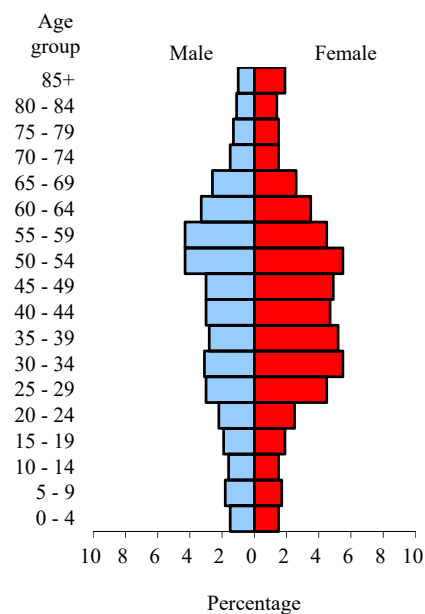
Chapter 2 Population structure

- (1) Population pyramids (in percentage) of the 18 districts in Hong Kong, June 2016

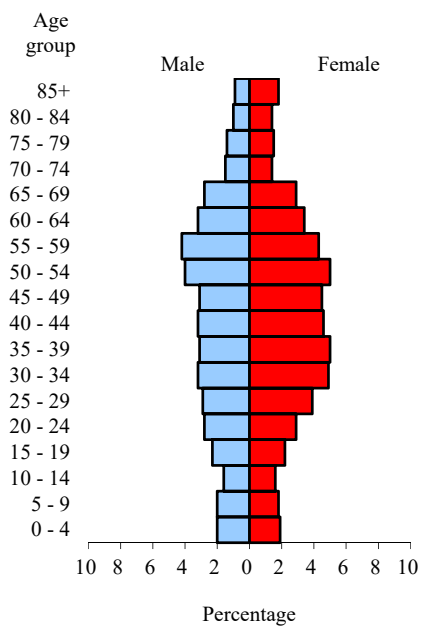
Central and Western



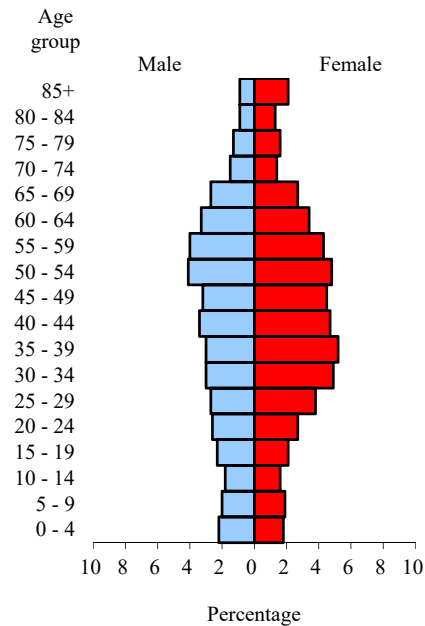
Wan Chai



Eastern



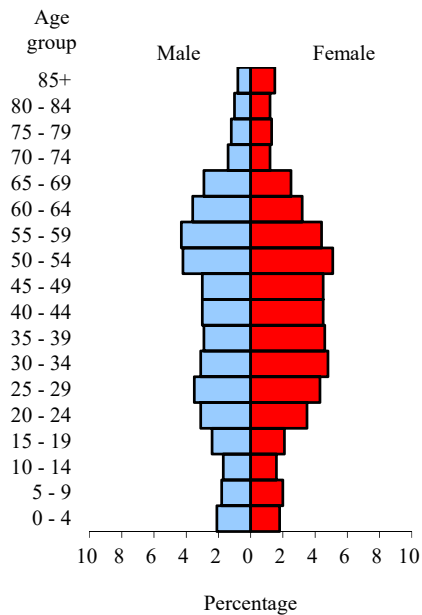
Southern



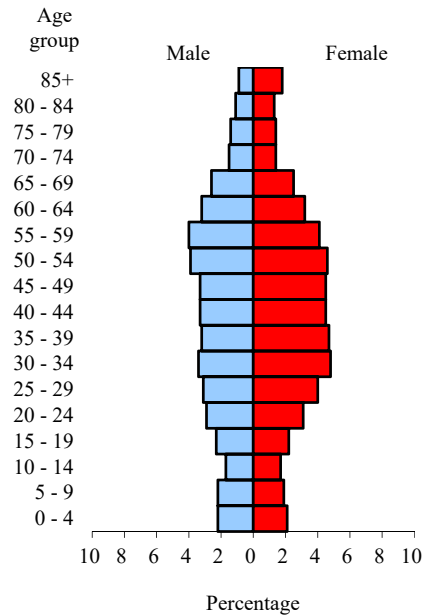
Solutions to exercises

- (1) Population pyramids (in percentage) of the 18 districts in Hong Kong, June 2016 (cont'd)

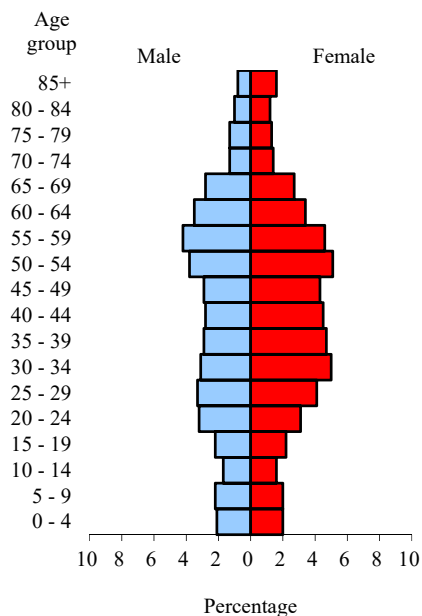
Yau Tsim Mong



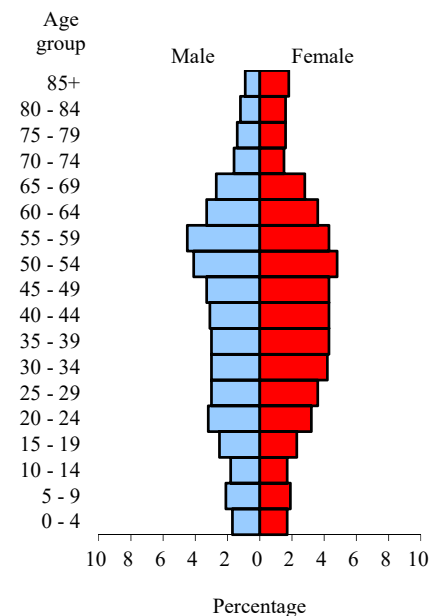
Sham Shui Po



Kowloon City



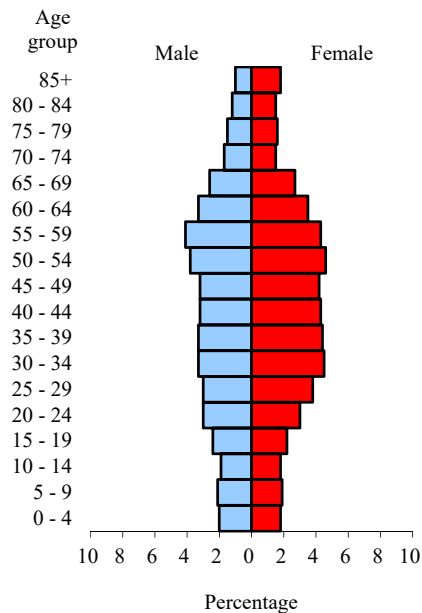
Wong Tai Sin



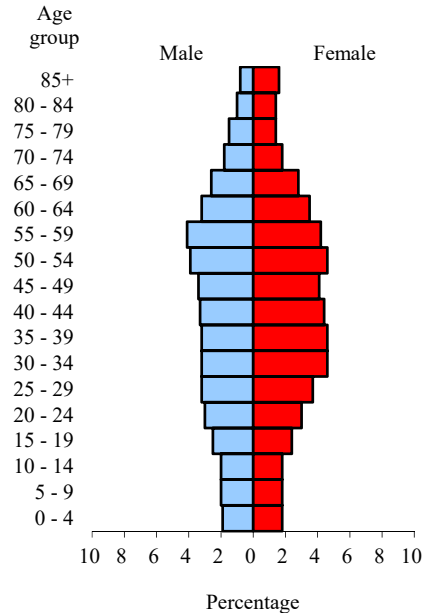
Solutions to exercises

- (1) Population pyramids (in percentage) of the 18 districts in Hong Kong, June 2016 (cont'd)

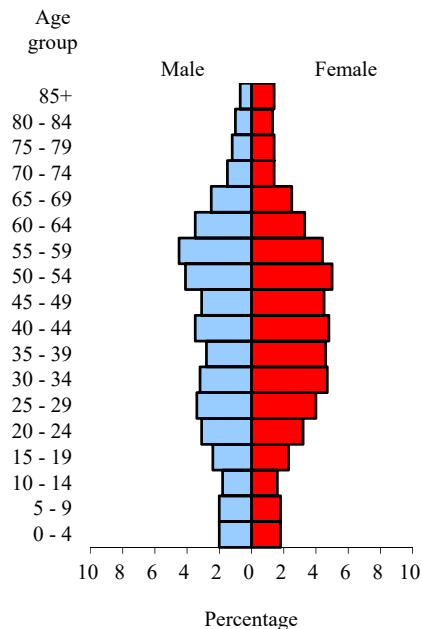
Kwun Tong



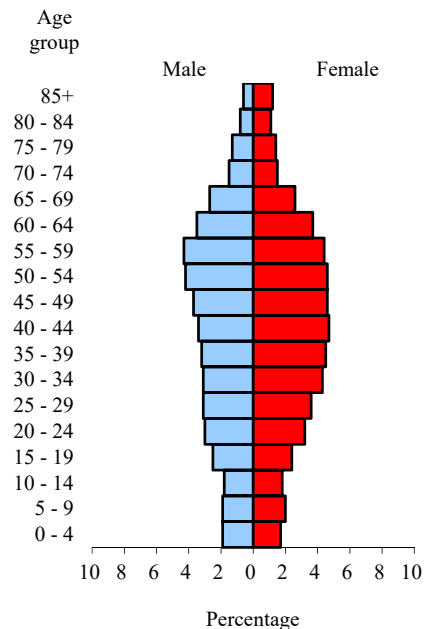
Kwai Tsing



Tsuen Wan



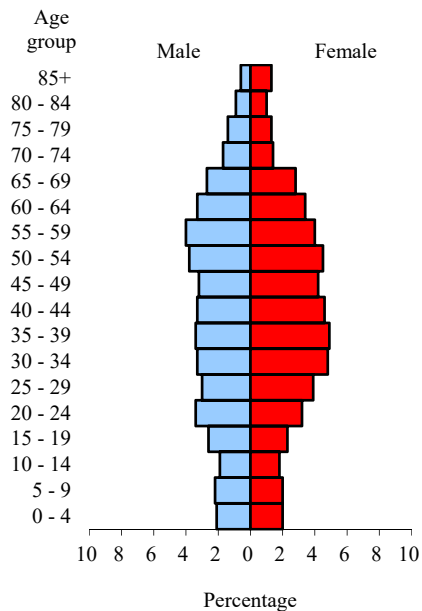
Tuen Mun



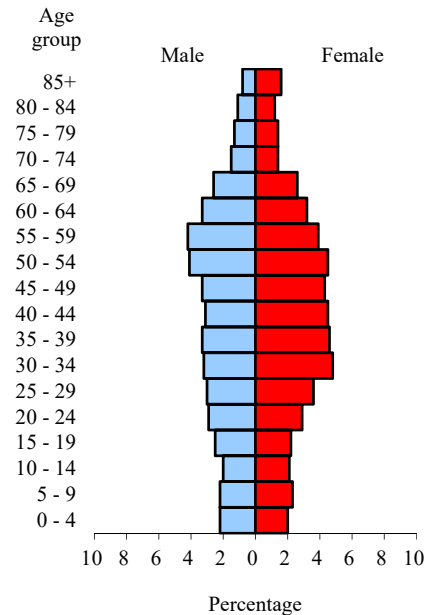
Solutions to exercises

- (1) Population pyramids (in percentage) of the 18 districts in Hong Kong, June 2016 (cont'd)

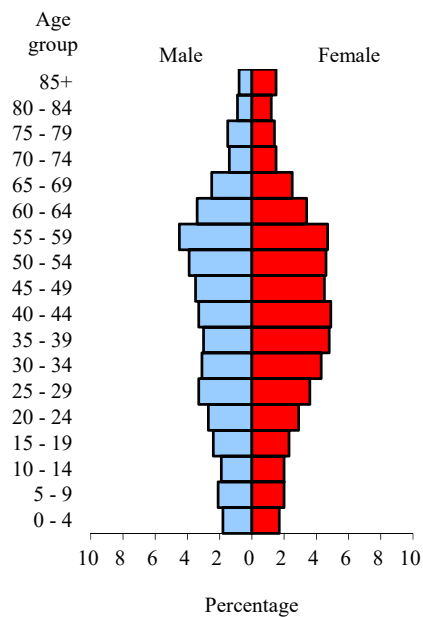
Yuen Long



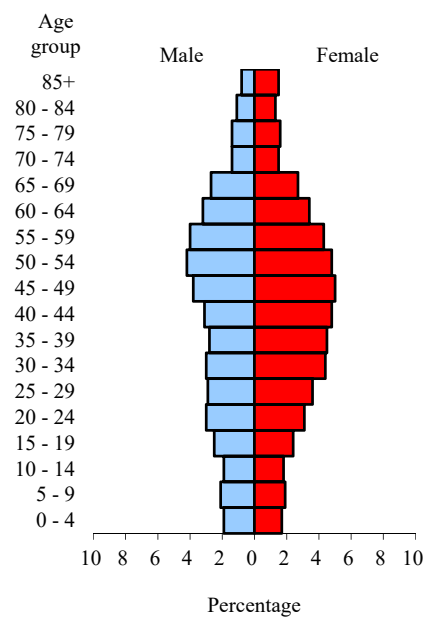
North



Tai Po

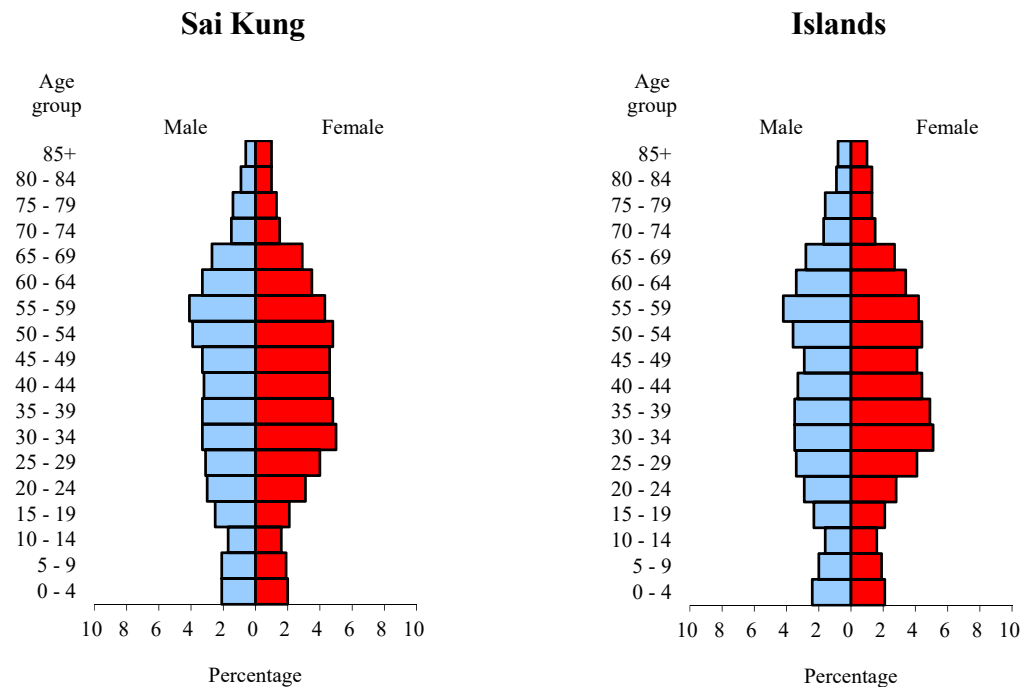


Sha Tin



Solutions to exercises

- (1) Population pyramids (in percentage) of the 18 districts in Hong Kong, June 2016 (cont'd)



Solutions to exercises

(2) Rank the ageing extent of these districts by comparing their median ages.

District Council district	Median age	Ranking for ageing extent ^(Note) ("1" for the most aged district)
Central and Western	43.8	6
Wan Chai	44.9	1
Eastern	43.8	6
Southern	43.9	4
Yau Tsim Mong	43.2	11.5
Sham Shui Po	42.9	14
Kowloon City	43.1	13
Wong Tai Sin	44.6	2
Kwun Tong	43.8	6
Kwai Tsing	43.5	10
Tsuen Wan	43.2	11.5
Tuen Mun	43.7	8
Yuen Long	42.1	18
North	42.7	16
Tai Po	43.6	9
Sha Tin	44.2	3
Sai Kung	42.8	15
Islands	42.4	17

Note : Where there are ties in rank, the tied observations are assigned the mean of the ranks which they jointly occupy.

Solutions to exercises

Chapter 4 Other official statistics

1. The population of Hong Kong in mid-2020 was

- ☐ 5.75 million
- ☐ 6.50 million
- ☒ 7.48 million
- ☐ 7.24 million

2. Crude birth rate in Hong Kong

<u>Year</u>	<u>(Number of births per 1 000 population)</u>
-------------	--

2011	13.5
------	------

2020	x
------	-----

$x =$

- ☐ 7.6
- ☒ 5.8
- ☐ 9.3
- ☐ 9.8

3. If the crude death rate in a given year was 5.0 deaths per 1 000 population and the crude birth rate was 7.2 births per 1 000 population, the rate of natural increase per 1 000 population in the period was

- ☐ -2.4
- ☒ 2.2
- ☐ -12.0
- ☐ 12.0

4. Most of the visitors visiting Hong Kong in 2020 came from

- ☐ United States of America
- ☐ Japan
- ☒ The Mainland
- ☐ Europe

Solutions to exercises

5. The population in mid-2015 = a ; and
the population in mid-2020 = b .

The compound average growth rate per annum of the population in this period was

☐ $\left(\sqrt[4]{\frac{b}{a}} - 1\right) \times 100\%$

☐ $\frac{\left(\frac{b}{a} - 1\right)}{4} \times 100\%$

☒ $\left(\sqrt[5]{\frac{b}{a}} - 1\right) \times 100\%$

☐ $\frac{\left(\frac{b}{a} - 1\right)}{5} \times 100\%$

6. In 2020 the size of the labour force in Hong Kong was

- ☐ 3.82 million
☐ 3.88 million
☐ 3.95 million
☒ 3.89 million

7. Which category of persons is regarded as economically inactive?

- ☐ Unpaid family workers
☐ Employers
☐ The unemployed
☒ Full-time home-makers

8. Which of the following is not an approach in the compilation of the Gross Domestic Product?

- ☐ Expenditure approach
☐ Production approach
☒ Industrial approach

Solutions to exercises

Chapter 6 Uses and misuses of statistics

1. The man actually received \$80,000 in cash from Bank Y and he had to repay \$100,000 on the 16th day. Therefore the interest rate should be

$$\frac{\$20,000}{\$80,000} \times 100\% = 25\%$$

or 25% per 15 days.

2. The price of an article A was \$100 in 2019 and \$50 in 2020. This means that the price of A in the period has decreased by

- ☒ 50%
- ☐ 100%
- ☐ 150%
- ☐ 200%

3. Which one of the following charts is visually distorted and should not be used?

- ☒ Chart A
- ☐ Chart B

Chart A

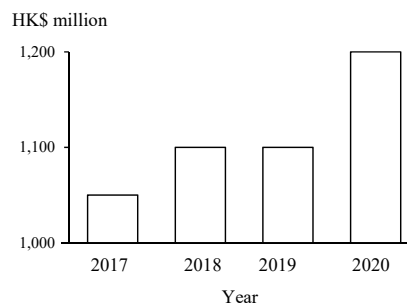
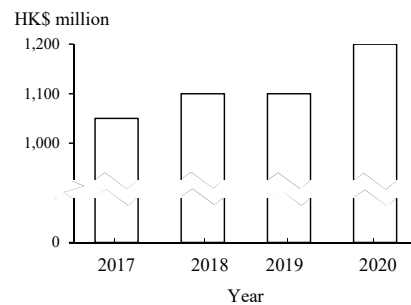


Chart B



Solutions to exercises

Chapter 7 Rate, ratio, proportion and percentage

- (i) $841\,927 / 7\,395\,900$ is just the proportion of the number of students passing the examination to the total population, irrespective of whether they had taken the examination. The accurate measure of the overall passing rate is $841\,927 / 1\,403\,211$, i.e. only those students who had taken the examination should be counted in the base used for comparison.

- (ii) The passing rates for the four districts on Hong Kong Island should be

Central and Western district	=	$(44\,014/60\,293) \times 100\%$	=	<u>73%</u>
Wan Chai district	=	$(28\,366/41\,110) \times 100\%$	=	<u>69%</u>
Eastern district	=	$(93\,943/144\,528) \times 100\%$	=	<u>65%</u>
Southern district	=	$(44\,831/63\,142) \times 100\%$	=	<u>71%</u>

The overall passing rate for Hong Kong Island should be

$$\frac{(44\,014 + 28\,366 + 93\,943 + 44\,831)}{(60\,293 + 41\,110 + 144\,528 + 63\,142)} \times 100\% = \underline{\underline{68\%}}$$

- (iii) As the increase in the number of students passing the examination might be due to the fact that there were more students in the Wan Chai district sitting for the examination in 2020, the comparison for the two years should therefore be based on the passing rate for the district in the two respective years.

As we only have limited information (data for two years only, viz. 2015 and 2020), it is difficult for us to draw the conclusion that the academic results of students in the Wan Chai district had improved during the period from 2015 and 2020. Maybe, the results in years 2015 and 2020 are outliers in the data series.

Solutions to exercises

Chapter 8 Measures of central tendency

1. Consider a set of figures :

$\{ 1, 9, 3, 7, 8, 12, 9 \}$

(i) What is the sum of these seven values? [49]

(ii) What is the mean? [7]

Note :

➤ **Mean = Sum of the figures \div Number of data points**

➤ **Sum of the figures = Mean \times Number of data points**

(iii) What is the median? [8]

(iv) What is the mode? [9]

(v) Is the median equal to the mean of the same seven values? [No]

(vi) Are the mean and median the same when the set of figures is
 $\{ 1, 3, 7, 11, 13 \}$?

[Yes; Mean = Median = 7]

(vii) When the mean and median are the same, what does this suggest?

[When the set of data is symmetrical, the mean and median will be the same. However, having the same mean and median, the set of data is not necessarily symmetrical. For example, in the set of figures $\{ 1, 7, 9, 13, 15 \}$, although both the mean and median are equal (= 9), the set of data is not symmetrical.]

2. The mean of $\{ 10, 20, 30, 40, 50 \}$ is

☒ 30

☐ 35

☐ 40

☐ 45

3. The mode of $\{ 3, 10, 14, 23, 29, 30, 31 \}$ is

☐ 20

☐ 23

☐ 31

☒ Mode does not exist in this set of figures

Solutions to exercises

4. When half of the elements of a population are smaller than a value X and half are greater than it, X is the
- ☐ Mean
 - ☒ Median
 - ☐ Mode
5. Among mean, median and mode, which one is the most easily affected by extreme values?
- ☒ Mean
 - ☐ Median
 - ☐ Mode

Solutions to exercises

Chapter 9 Measures of dispersion

1. The mean deviation of $\{2, 5, 13, 28\}$ is

- ☐ 0
☒ 8.5
☐ 12
☐ 34

2.

Student	Examination scores			Standard examination scores			
	English	Chinese	Mathematics	English	Chinese	Mathematics	Total
(1)	40	62	80	-1.8	-1.0	-0.3	-3.1
(2)	57	60	60	-0.1	-1.4	-2.2	-3.7
(3)	60	70	95	0.2	0.7	1.1	2.0
(4)	48	64	92	-1.0	-0.5	0.8	-0.7
(5)	53	66	75	-0.5	-0.1	-0.8	-1.4
(6)	66	72	78	0.7	1.2	-0.5	1.4
(7)	72	70	86	1.3	0.7	0.2	2.3
(8)	49	67	87	-0.9	0.1	0.3	-0.5
(9)	69	60	99	1.0	-1.4	1.5	1.1
(10)	70	74	83	1.1	1.6	0.0	2.7
Mean	58.4	66.5	83.5				
Standard deviation	10.3	4.7	10.6				

The student in the class who has attained the best overall result is **(10)**.

(Reason: Student (10) got the highest total standard score.)

Enquiries on Statistical Data

The following are telephone numbers, fax numbers and e-mail addresses for enquiries about various statistical data compiled by the Census and Statistics Department. In case more detailed information is needed, enquiries will be referred to the subject officers concerned.

Statistical Data	Tel No.	Fax No.	E-mail Address
▶ Merchandise trade statistics	2582 4915	2802 1101	trade@censtatd.gov.hk
▶ Trade in services and offshore trade statistics	3903 7415	2121 8296	tis@censtatd.gov.hk
▶ Shipping statistics	2582 2126	3101 9275	shipping@censtatd.gov.hk
▶ Consumer Price Indices	3903 7374	2577 6253	cpi@censtatd.gov.hk
▶ Household expenditure statistics	3903 7384	2127 4698	hes@censtatd.gov.hk
▶ Labour force and unemployment statistics	2887 5508	2508 1501	ghs@censtatd.gov.hk
▶ Persons engaged and job vacancies in establishments statistics	2582 5076	2827 2296	employment@censtatd.gov.hk
▶ Wage and labour earnings statistics	2887 5550	3579 2070	wage@censtatd.gov.hk
▶ National income statistics			
• Gross Domestic Product by expenditure component	2582 5077	2157 9295	gdp-e@censtatd.gov.hk
• Gross Domestic Product by economic activity	3903 7005	3902 3045	gdp-p@censtatd.gov.hk
• Gross National Income	3903 7054	2116 0370	gni@censtatd.gov.hk
▶ Balance of Payments statistics	3903 6981	2116 0278	bop@censtatd.gov.hk
▶ Economic statistics by industry	3903 7267	2123 1053	econ-survey@censtatd.gov.hk
▶ Population statistics	3903 6943	2716 0231	population@censtatd.gov.hk
▶ Social statistics	2887 5508	2508 1501	social@censtatd.gov.hk
▶ Other statistics	2582 5073	2827 1708	gen-enquiry@censtatd.gov.hk
▶ Statistical publications	2582 3025	2827 1708	gen-enquiry@censtatd.gov.hk